

# EVALUATION OF CAUSE EFFECT GRAPHS BY PETRI NETS

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## WHAT ARE CAUSE EFFECT GRAPHS ?

### -> EXAMPLE [MYERS 1979, P. 58]

#### □ verbal specification

The character in column 1 must be an "A" or a "B".

The character in column 2 must be a digit.

In this situation, the file update is made.

If the first character is incorrect, message X12 is issued.

If the second character is not a digit, message X13 is issued.

#### □ causes

- 1 character in column 1 is "A"
- 2 character in column 1 is "B"
- 3 character in column 2 is a digit

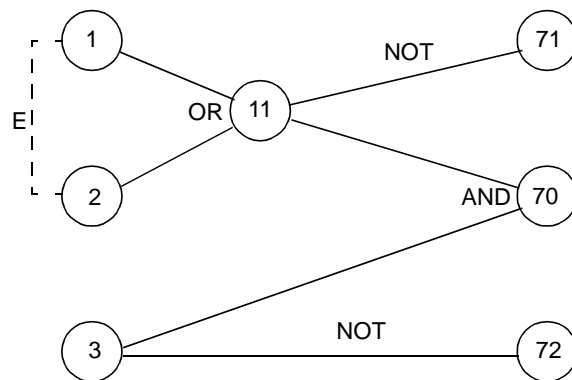
#### □ effects

70 file update, update message -> effect1

71 message X12 is issued-> effect2

72 message X13 is issued-> effect3

#### □ cause-effect graph



## STANDARD EVALUATION PROCEDURE, BASICS

#### □ objective

-> to get a characteristic set of abstract test cases

#### □ compare

-> [Myers 1979]

-> [Liggesmeyer 2002]



#### □ Select an effect to be present (TRUE).

□ Trace back through the graph, and find all **essential combinations** of causes that will set this effect to TRUE.

#### □ Doing so, consider suitable **heuristics** (next slide).

-> to be efficient

-> to eliminate situations that tend to be low-yield test cases

#### □ Create a line in the decision table for each combination of causes.

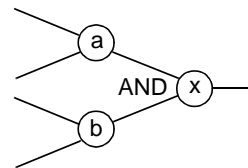
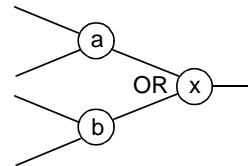
-> each line stands for a test case

#### □ Determine the states of all other effects.

#### □ Eliminate doubled lines in decision table.

## STANDARD EVALUATION PROCEDURE, HEURISTICS

- ❑ remember: backward procedure
- ❑ if x
  - then enumerate all situations, where one input is TRUE & all other inputs are FALSE
  - else set all inputs to FALSE
  - endif
- ❑ if x
  - then set all inputs to TRUE
  - else enumerate all situations, where one input is FALSE & all other inputs are TRUE
  - endif



## AN ALTERNATIVE APPROACH

**SUPPORTING**

**-> ANIMATION**

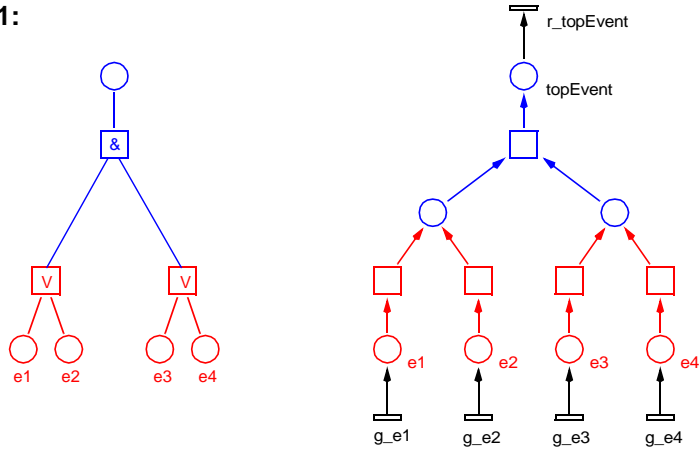
**-> AUTOMATIC COMPUTATION**

**DEFINING**

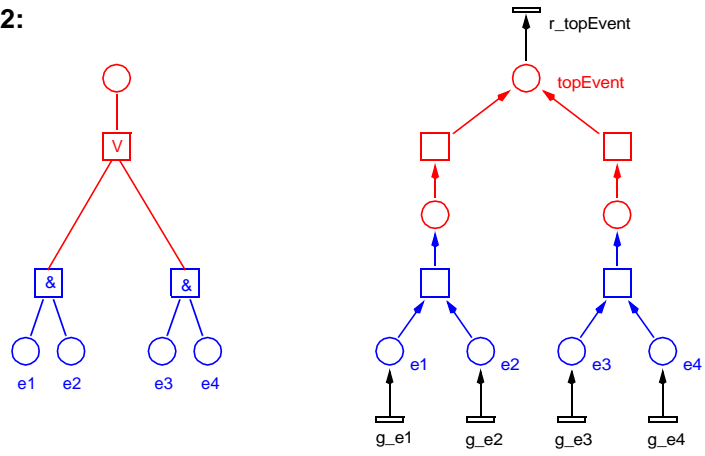
**-> A NEW COVERAGE MEASURE**

### BASIC FAULT TREES

EX1:



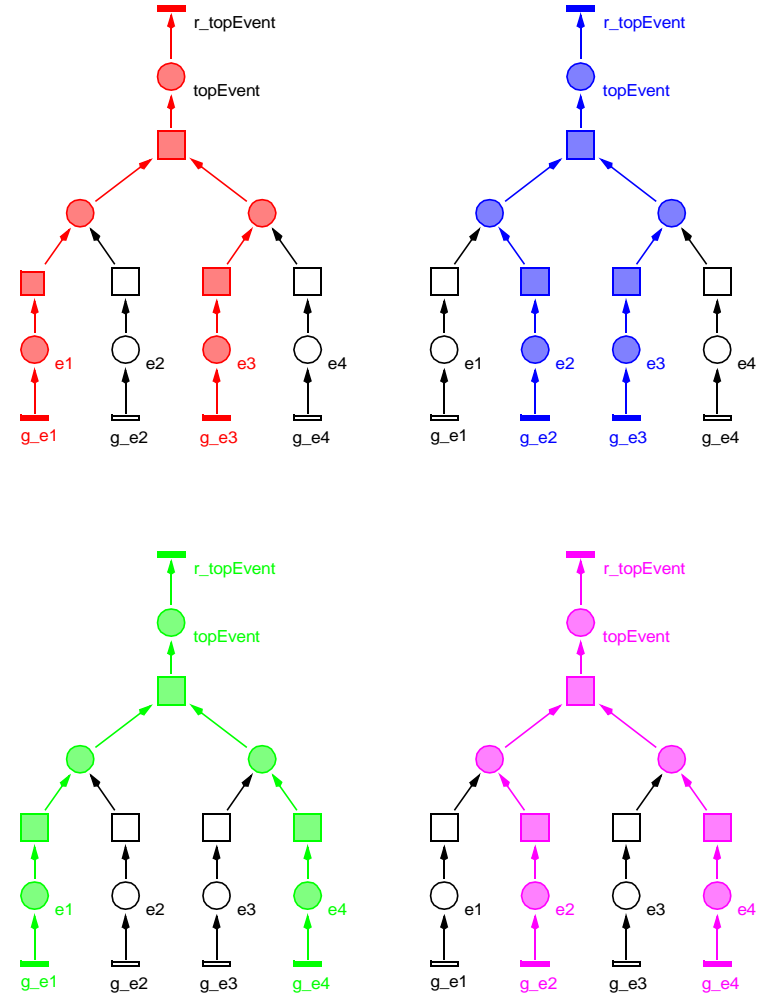
EX2:



-> minimal cuts ?

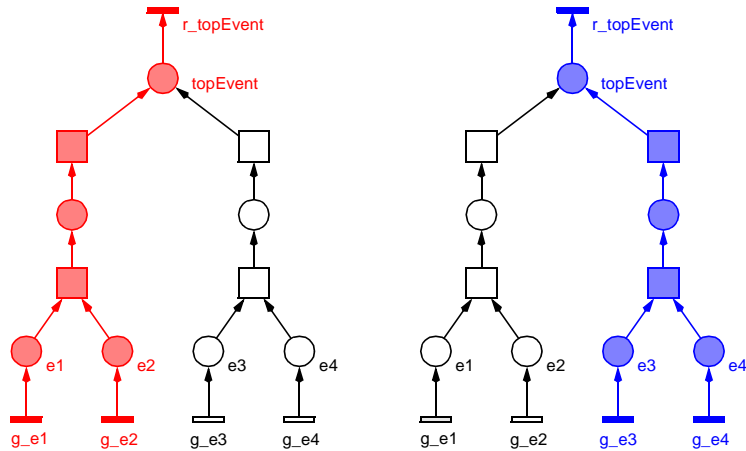
-> minimal runs (T-invariants) ?

### BASIC FAULT TREES, EX1 -> T-INVARIANTS



## BASIC FAULT TREES, EX2

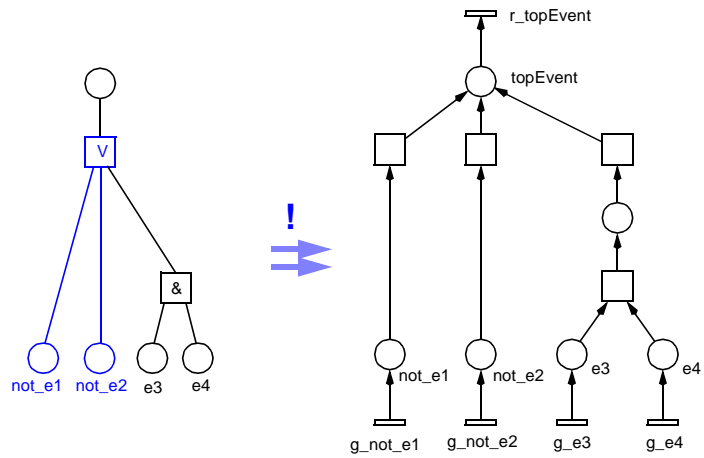
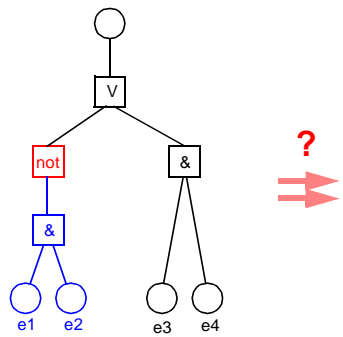
### -> T-INVARIANTS



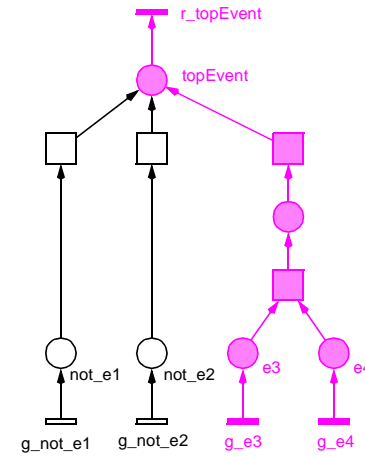
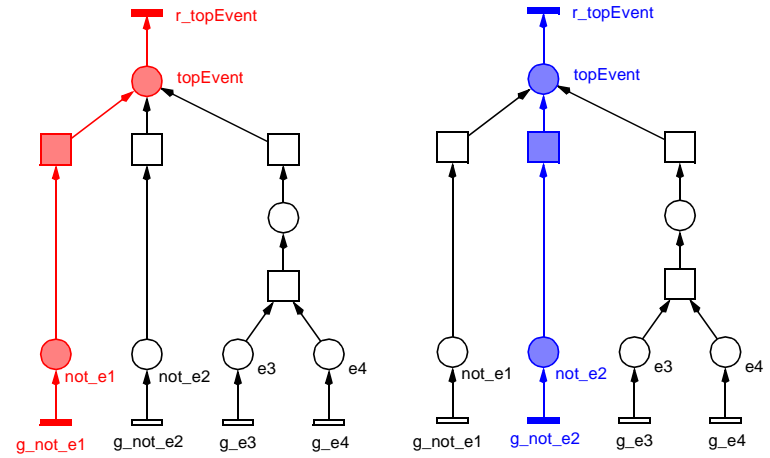
## OBSERVATIONS

- (minimal) cut:  
(minimal) set of basic events  
-> resulting into the top event
- (minimal) T-invariant:  
(minimal) multiset of transitions  
-> with zero total effect on marking  
-> reproducing a given marking  
-> potentially cyclic behaviour
- minimal T-invariants /cuts:  
-> minimal runs  
-> basic behaviour
- any behaviour is a non-negative linear combination of basic runs
- (minimal) cuts <-> (minimal) T-invariants <-> (minimal) test case
- CTI - Covered by T-Invariants:  
each transition belongs to a (minimal) T-invariant  
-> each transition contributes to system behaviour
- decomposition into minimal [ cuts / T-invariants / test cases ]  
-> node / branch coverage  
-> **basic behaviour coverage**

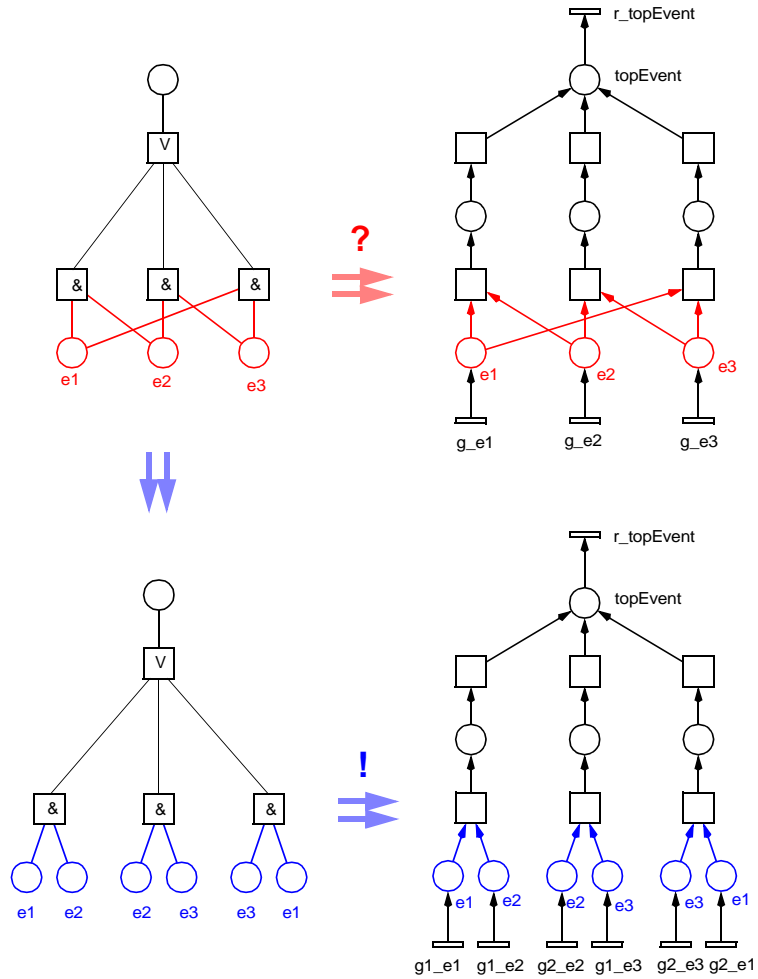
### ADVANCED FAULT TREES, EX1 -> PROBLEM: NEGATION



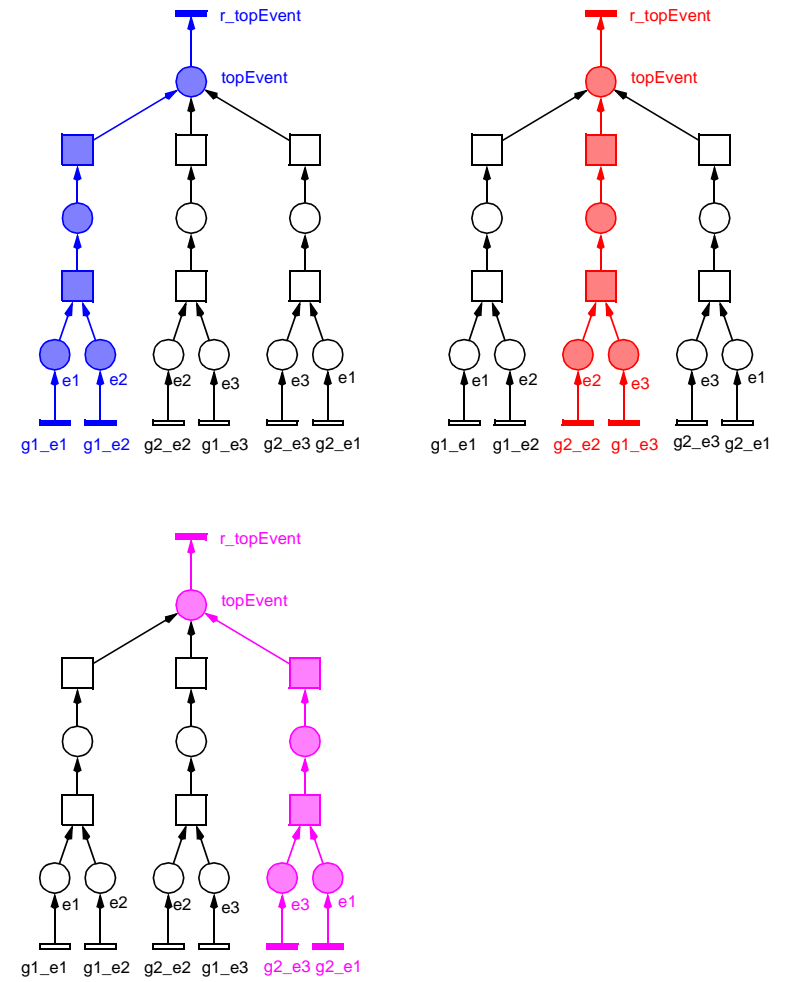
### ADVANCED FAULT TREES, EX1 -> T-INVARIANTS



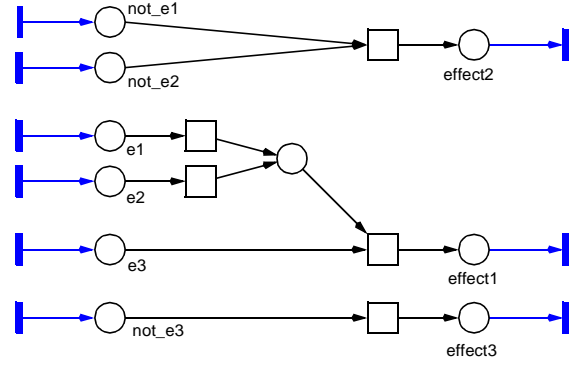
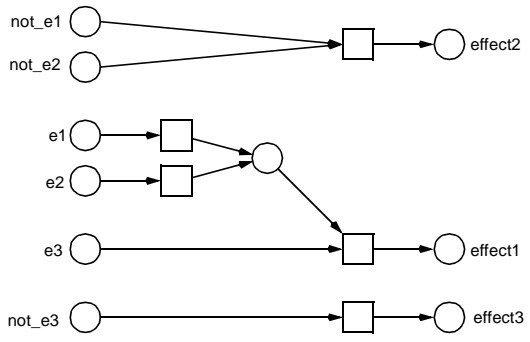
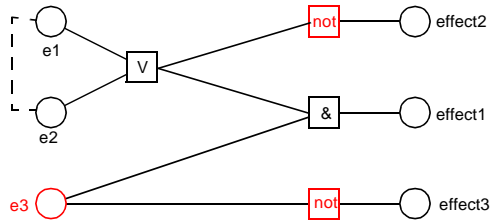
### ADVANCED FAULT TREES, EX2 -> PROBLEM: BRANCHING PLACES



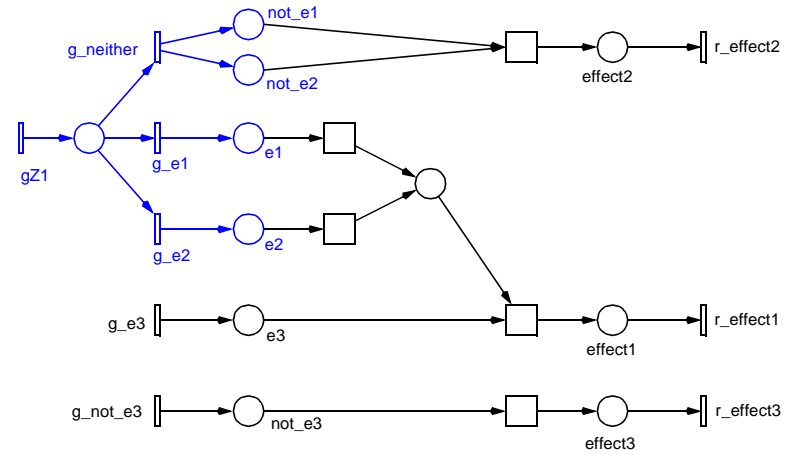
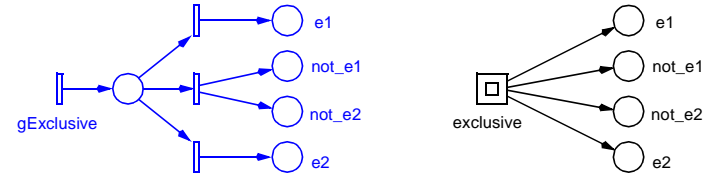
### ADVANCED FAULT TREES, EX2 -> T-INVARIANTS



### CAUSE EFFECT GRAPH, [MYERS 1979]



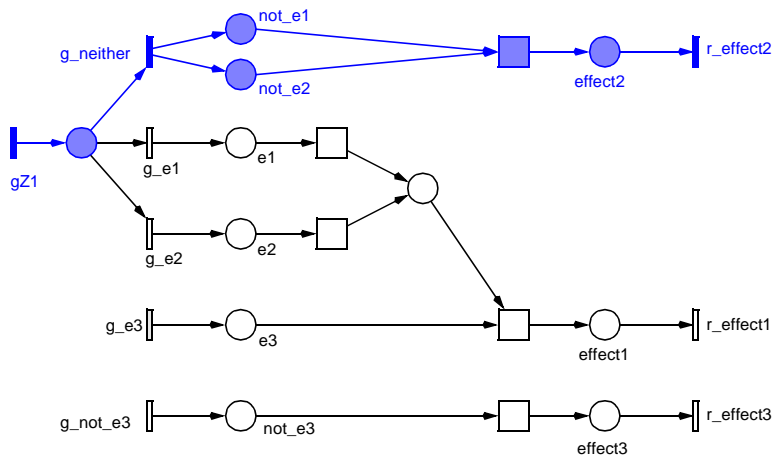
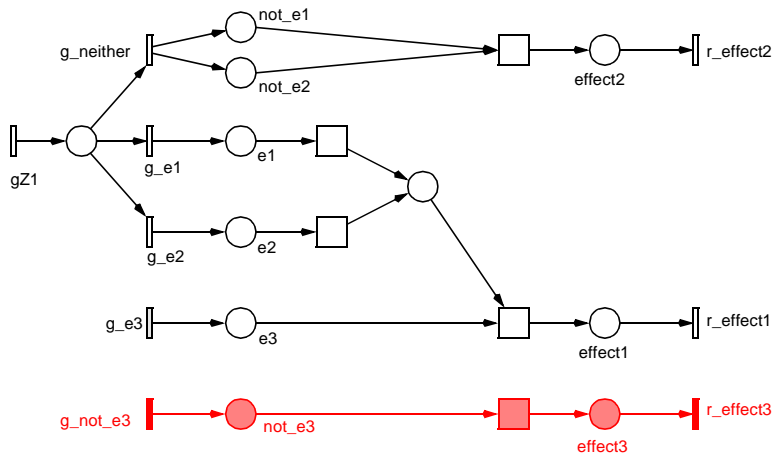
### CAUSE EFFECT GRAPH, [MYERS 1979]





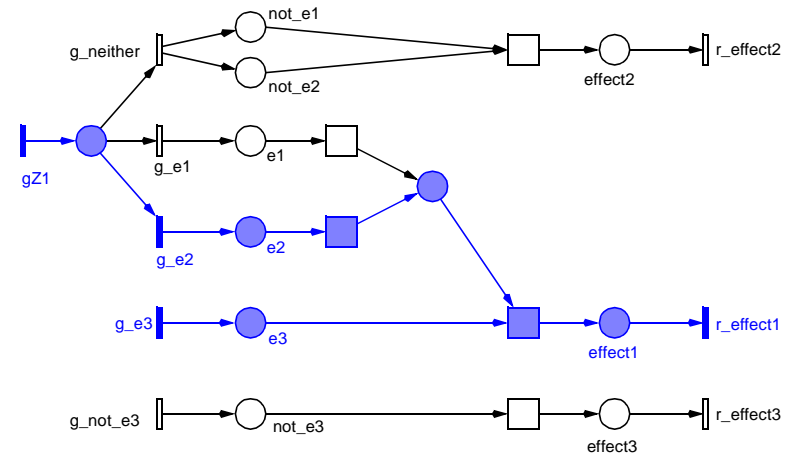
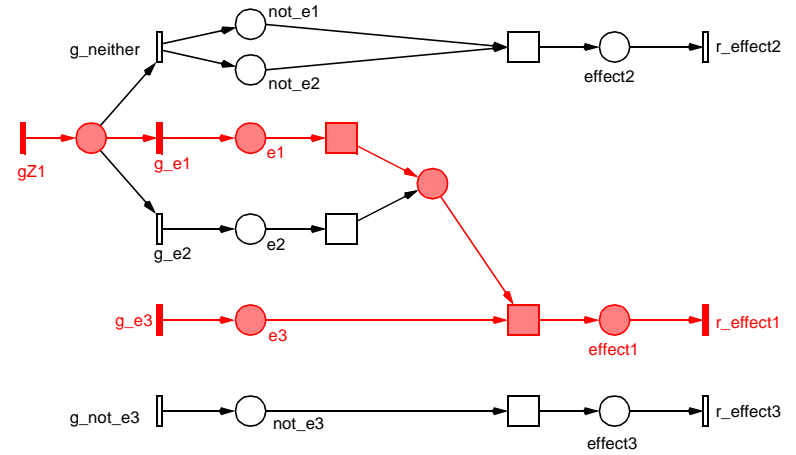
### CAUSE EFFECT GRAPH, [MYERS 1979]

-> T-INVARIANTS 1, 2



### CAUSE EFFECT GRAPH, [MYERS 1979]

-> T-INVARIANTS 3, 4

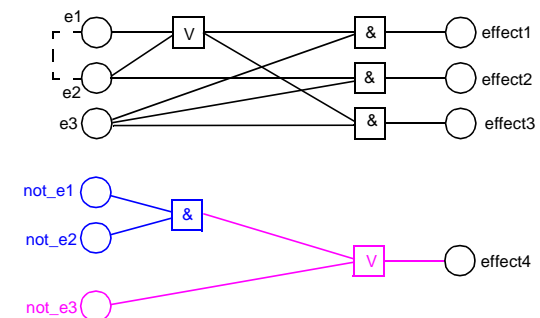
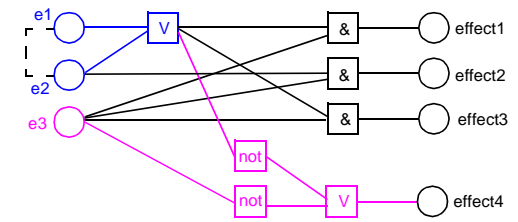
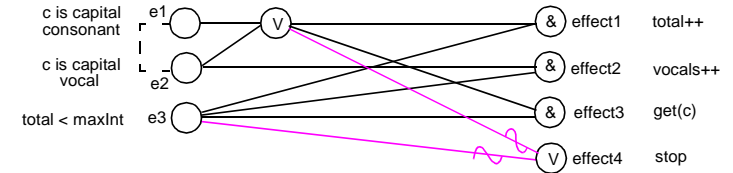


## CAUSE EFFECT GRAPH, [MYERS 1979]

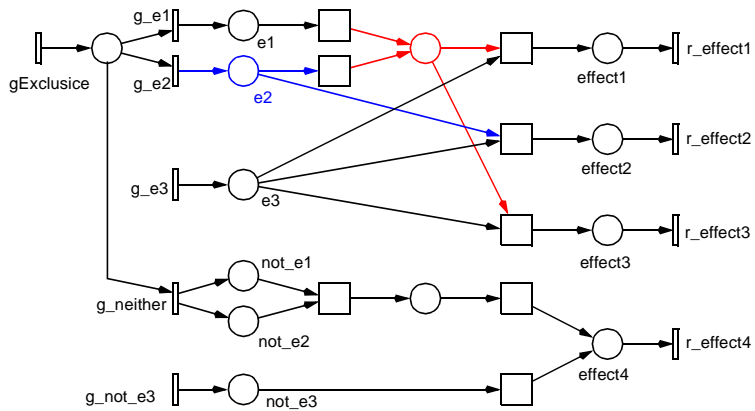
### -> EVALUATION OF TEST CASES

- ❑ **T-invariant 1** -> test case 1:  
*abstract test case:* not\_e3, don't-care: e1/e2 -> effect3  
*real test case:* A, A -> X13 message
- ❑ **T-invariant 2** -> test case 2  
*abstract test case:* not\_e1 and not\_e2, don't-care: e3 -> effect2  
*real test case:* C, 1 -> X12 message
- ❑ **T-invariant 3** -> test case 3  
*abstract test case:* e1 and e3 -> effect1  
*real test case:* A, 1 -> update message
- ❑ **T-invariant 4** -> test case 4  
*abstract test test case:* e2 and e3 -> effect1  
*real test case:* B, 1 -> update message
- ❑ these four test cases guarantee basic behaviour coverage
- ❑ don't care's: prefer TRUE assignment;  
 -> to avoid fault masking
- ❑ **THESE ARE EXACTLY THE FOUR TEST CASES WE GET BY THE STANDARD EVALUATION PROCEDURE**

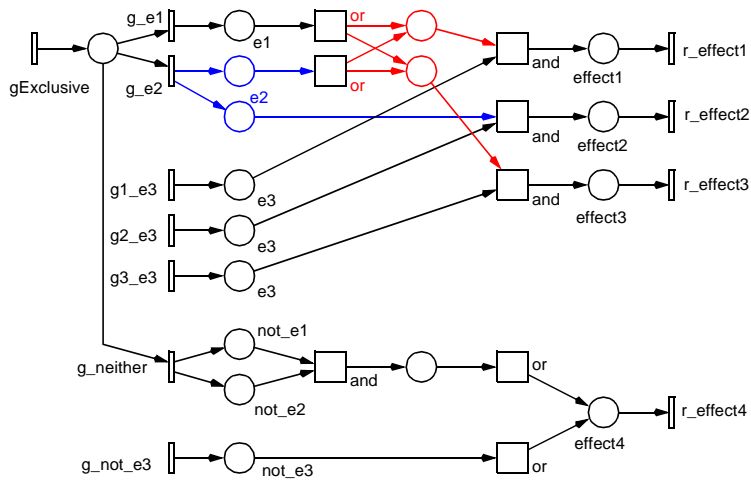
## CAUSE EFFECT GRAPH, [LIGGESMEYER 2002]



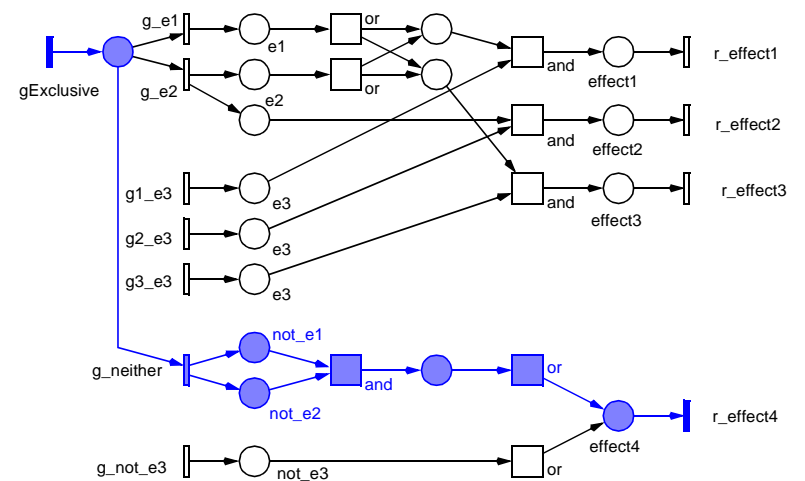
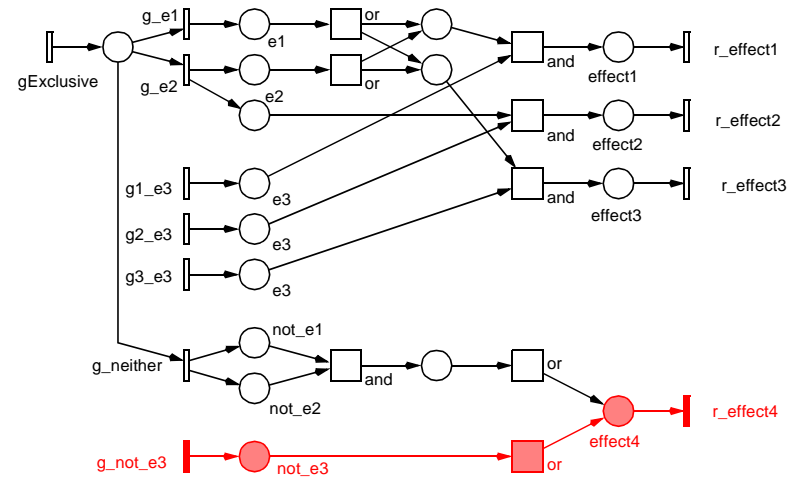
### CAUSE EFFECT GRAPH, [LIGGESMEYER 2002]



resolving of branching places

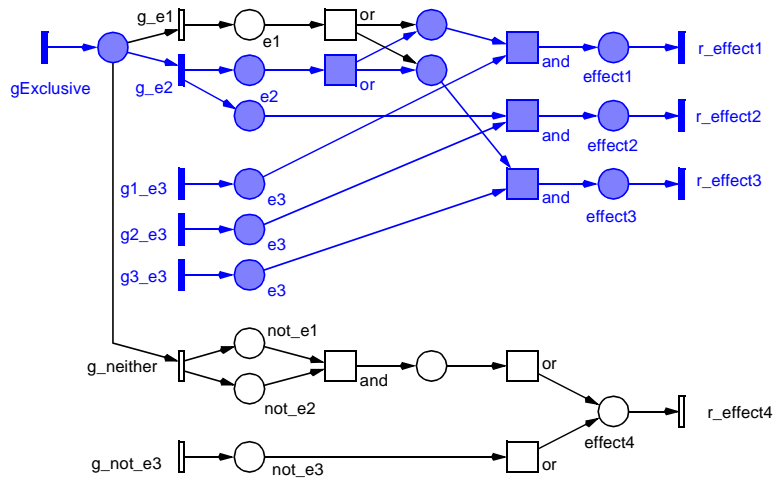
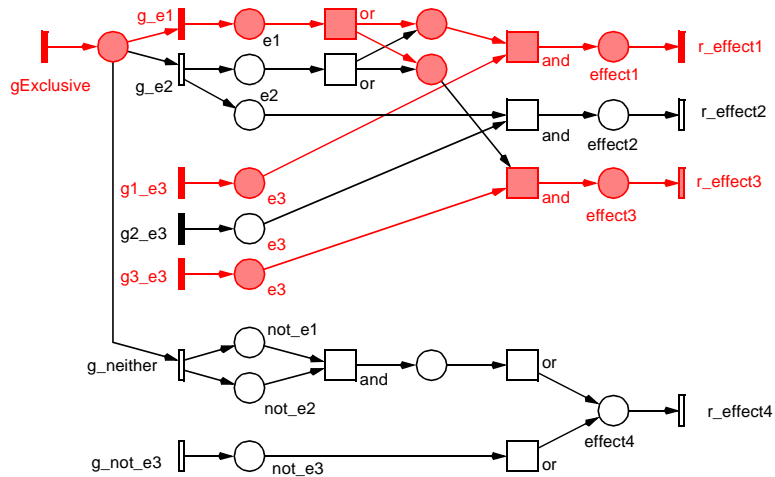


### CAUSE EFFECT GRAPH, [LIGGESMEYER 2002] -> T-INVARIANTS 1, 2



### CAUSE EFFECT GRAPH, [LIGGESMEYER 2002]

#### -> T-INVARIANTS 3, 4



### CAUSE EFFECT GRAPH, [LIGGESMEYER 2002]

#### -> EVALUATION OF TEST CASES

- T-invariant 1** -> test case 1:  
*abstract test case:* not\_e3, don't-care: e1/e2 -> effect4  
*real test case:* total = MAXINT; B
  
- T-invariant 2** -> test case 2  
*abstract test case:* not\_e1 and not\_e2, don't care: e3 -> effect4  
*real test case:* total < MAXINT; 0
  
- T-invariant 3** -> test case 3  
*abstract test case:* e1 and e3 -> effect1, effect3  
*real test case:* total < MAXINT; B
  
- T-invariant 4** -> test case 4  
*abstract test case:* e2 and e3 -> effect1, effect2, effect3  
*real test case:* total < MAXINT; A
  
- these four test cases guarantee basic behaviour coverage
  
- again: don't care's get TRUE assignment;
  
- standard evaluation procedure splits test case 1 into two cases:  
e1 and not\_e3 (and not\_e2) -> effect4  
e2 and not\_e3 (and not\_e1) -> effect4  
-> compare [Liggesmeyer 2002, p. 68]

## FINAL QUESTION

**How  
TO  
COMPUTE**

**MINIMAL  
T-INVARIANTS ?**

**-> BASICS OF  
PETRI NET THEORY  
[LAUTENBACH 1973]**

**-> RELIABLE TOOL SUPPORT  
AVAILABLE, E. G. CHARLIE**

## SUMMARY

- ❑ cause effect graphs can be represented adequately by Petri nets
- ❑ straightforward transformation
  - > automatic translation
- ❑ minimal T-invariants in Petri net representation correspond to minimal abstract test cases in cause effect graph representation

-> input transitions - causes  $g\_cause \parallel \rightarrow \bigcirc \text{ cause}$

-> output transitions - effects  $\text{effect } \bigcirc \rightarrow \parallel r\_effect$

- ❑ covering by T-invariants corresponds to covering by abstract test cases
  - > **BASIC BEHAVIOUR COVERAGE**
- ❑ computation of all minimal T-invariants
  - > there can be exponentially many
  - > reliable tool support available, e. g. Charlie (inspired by INA)

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