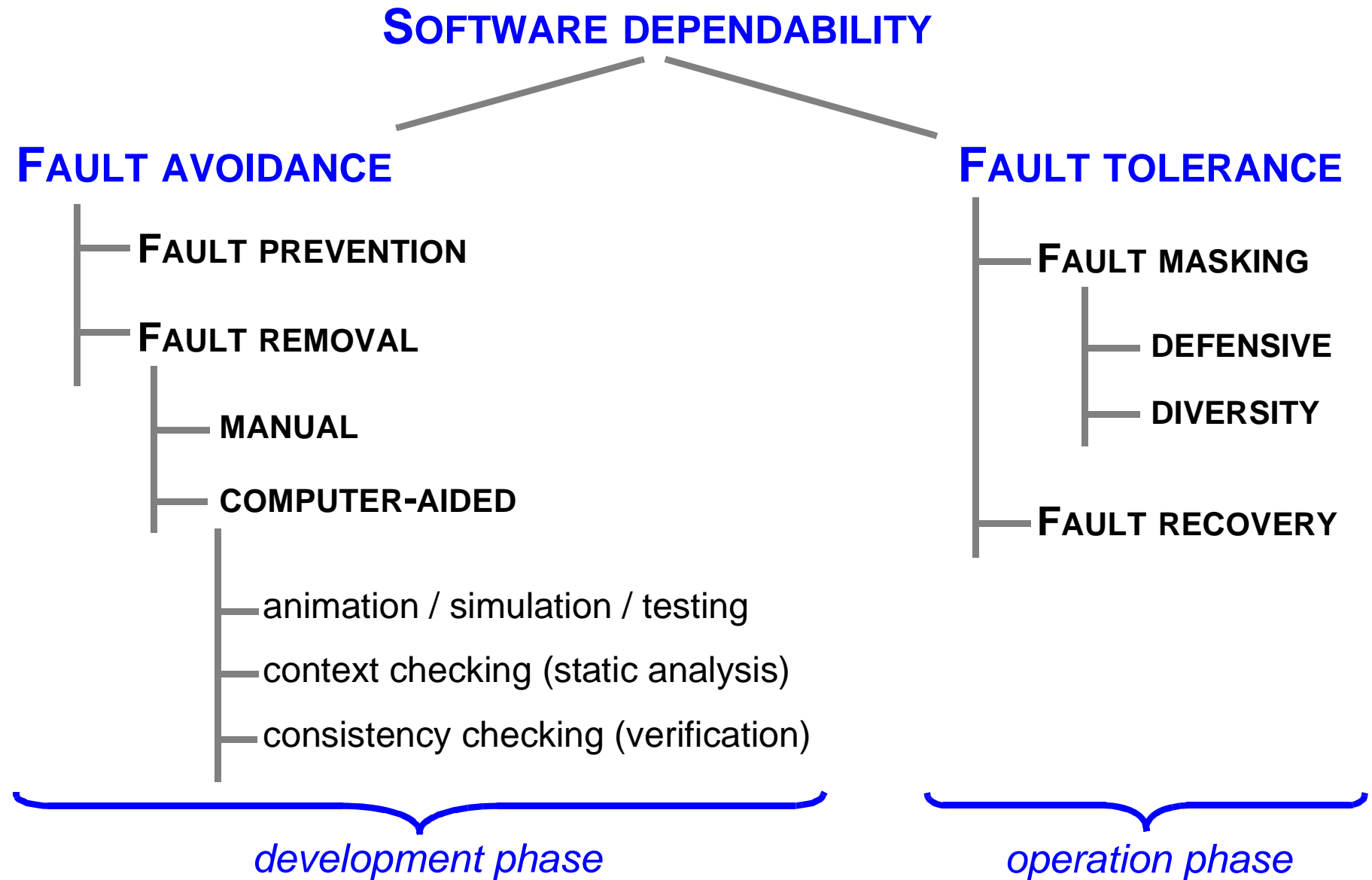
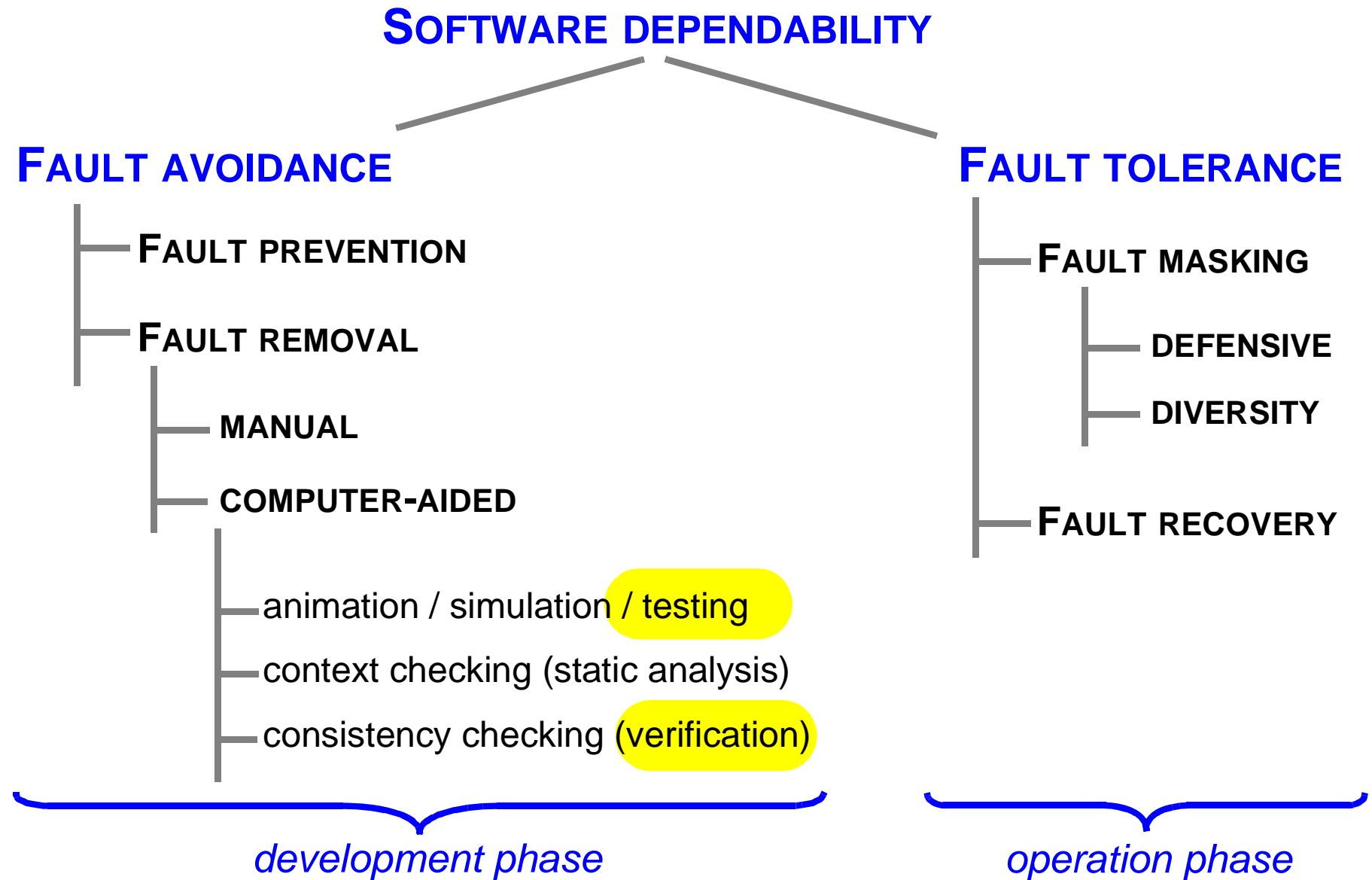


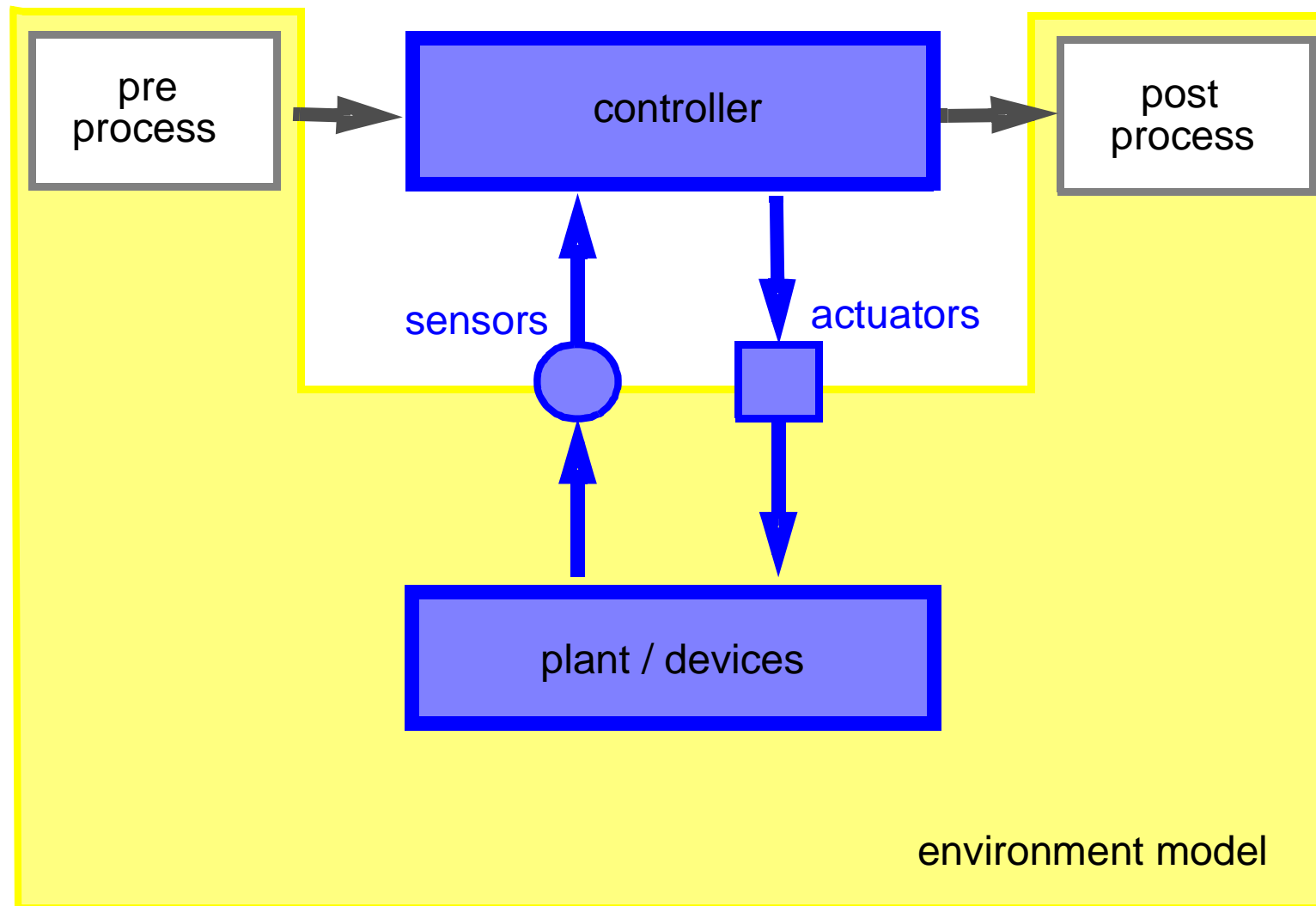
# **SYSTEMATIC TEST AND VERIFICATION OF SOFTWARE-BASED SYSTEMS**

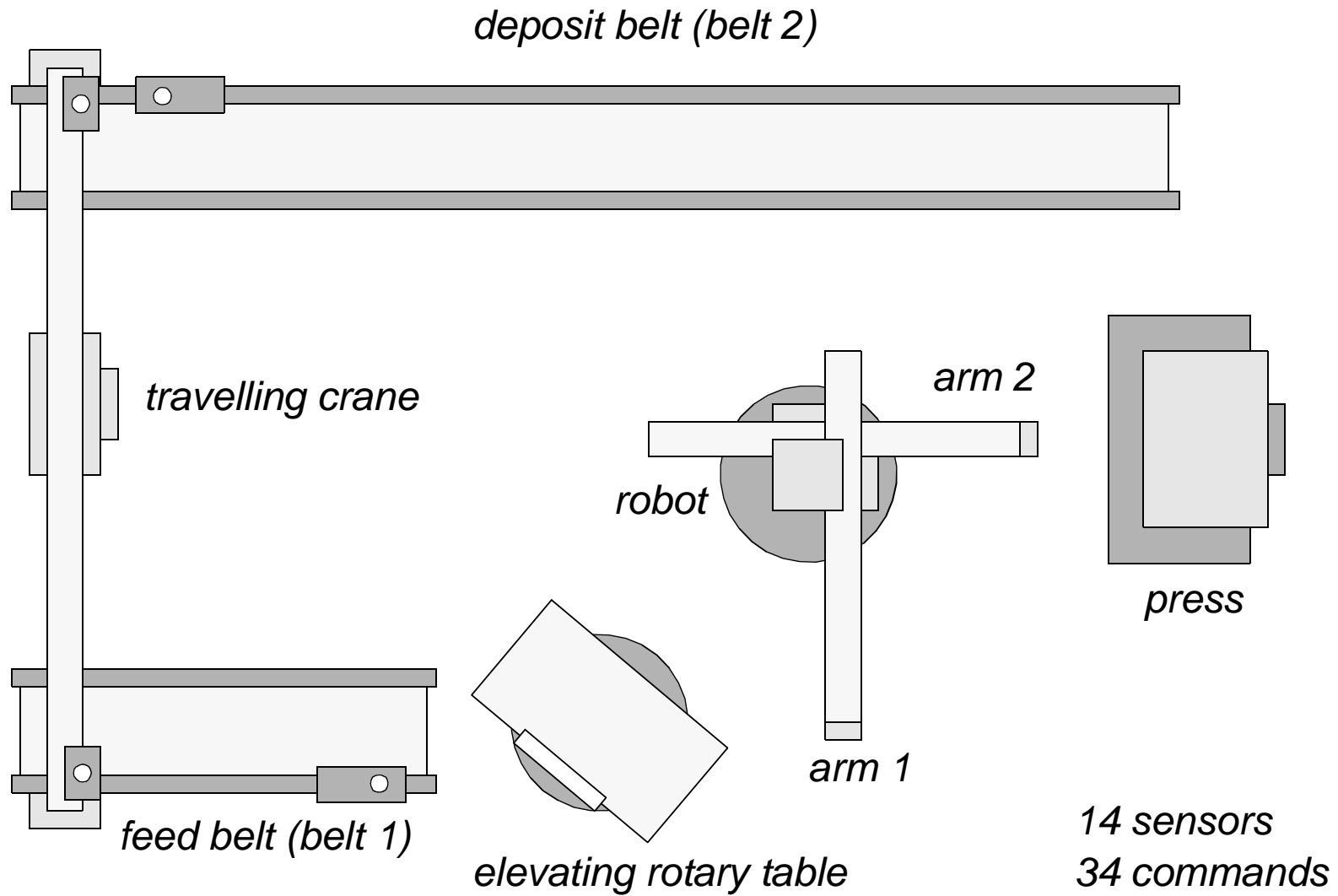
**Monika Heiner  
BTU Cottbus,  
Dep. of Computer Science**

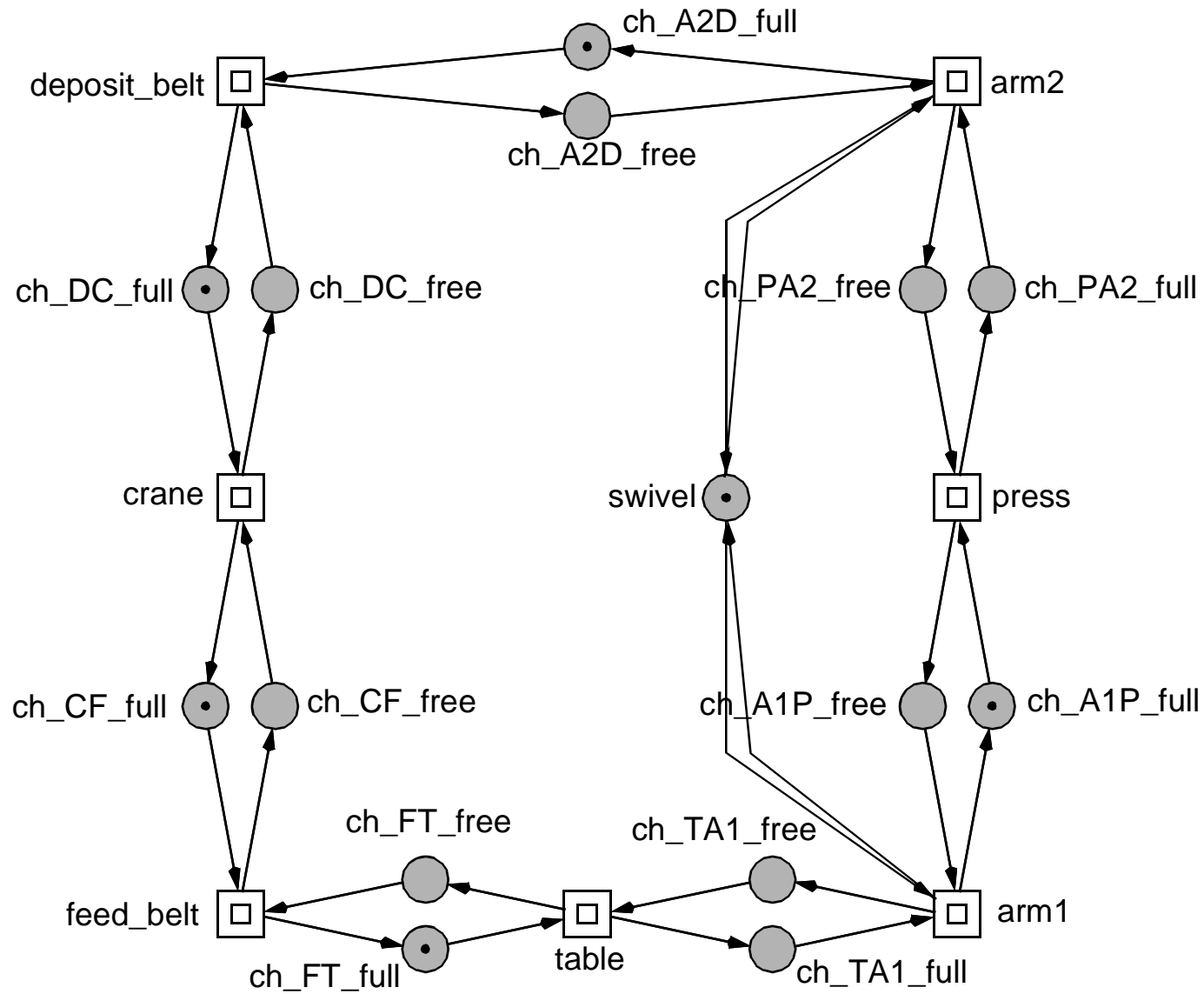




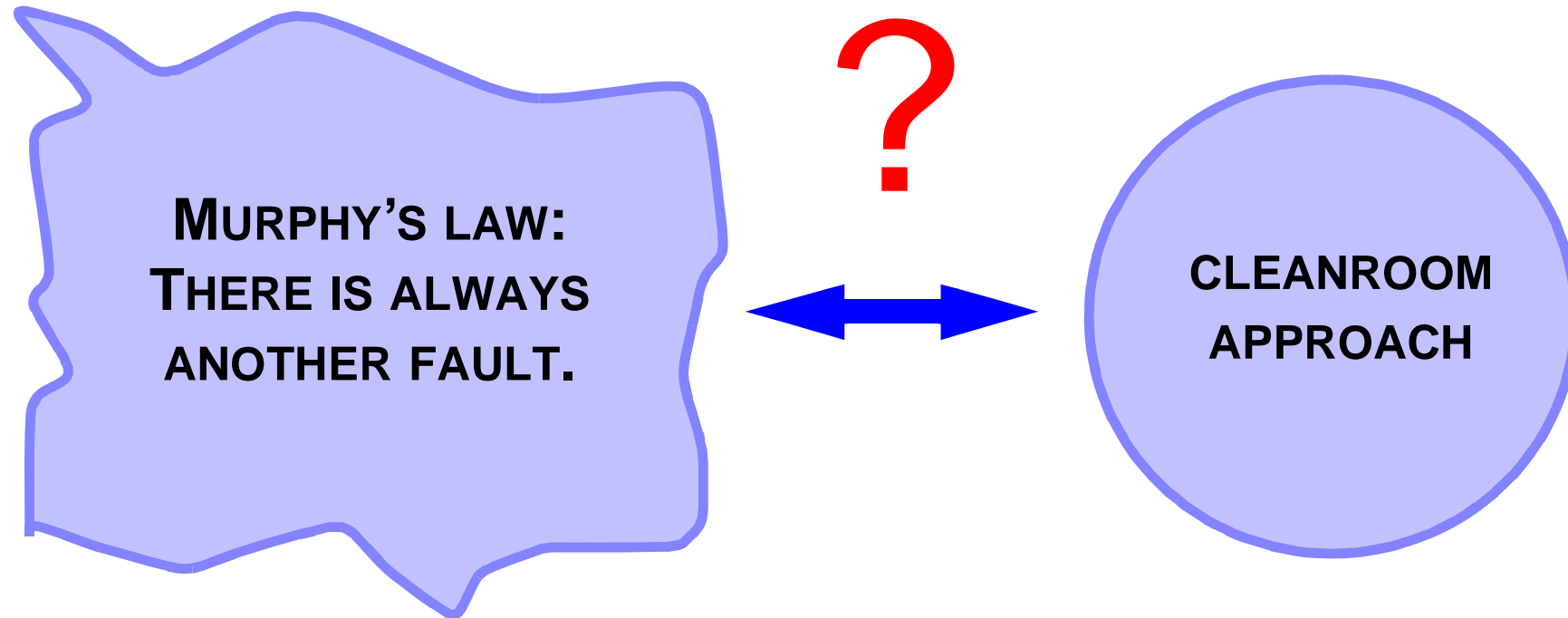
# **Application Scenario**







**231 P,  
202 T,  
65 PAGES**





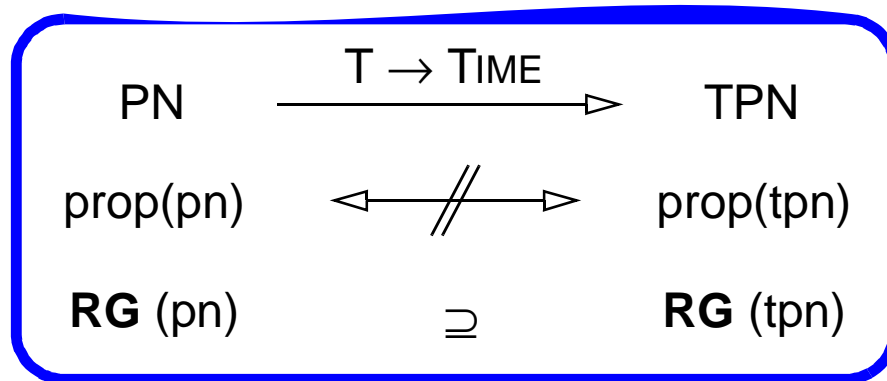
- ❑ **natural fault rate of seasoned programmers**
  - about 1-3 % of produced program lines
  
- ❑ **undecidability of basic questions in software validation**
  - > *program termination*
  - > *equivalence of programs*
  - > *program verification*
  - ...
  
- ❑ **validation = testing**
  
- ❑ **testing portion of total software production effort**
  - > *standard system:*  $\geq 50 \%$
  - > *extreme availability demands:*  $\approx 80 \%$



- ❑ **state space explosion,**  
**worst-case: product of the sequential state spaces**

- ❑ **probe effect**

- > *system exhibits in test mode other (less) behavior than in standard mode*
- > *test means (debugger) affect timing behavior*



result:

*masking of certain types of bugs:*

$DSt (pn) \rightarrow$  not  $DSt (tpn)$

$live(pn) \rightarrow$  not  $live (tpn)$

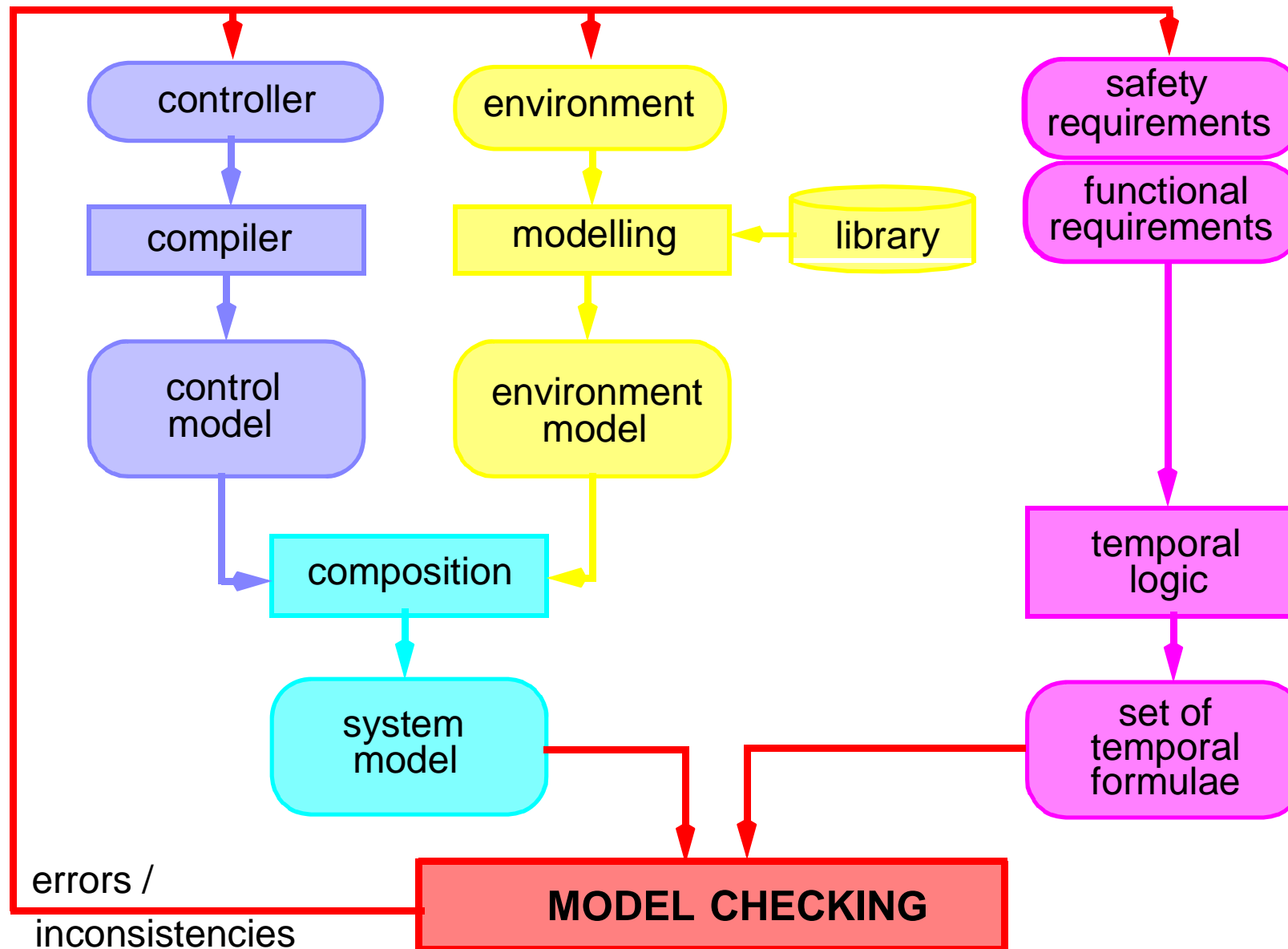
not  $BND (pn) \rightarrow$   $BND (tpn)$

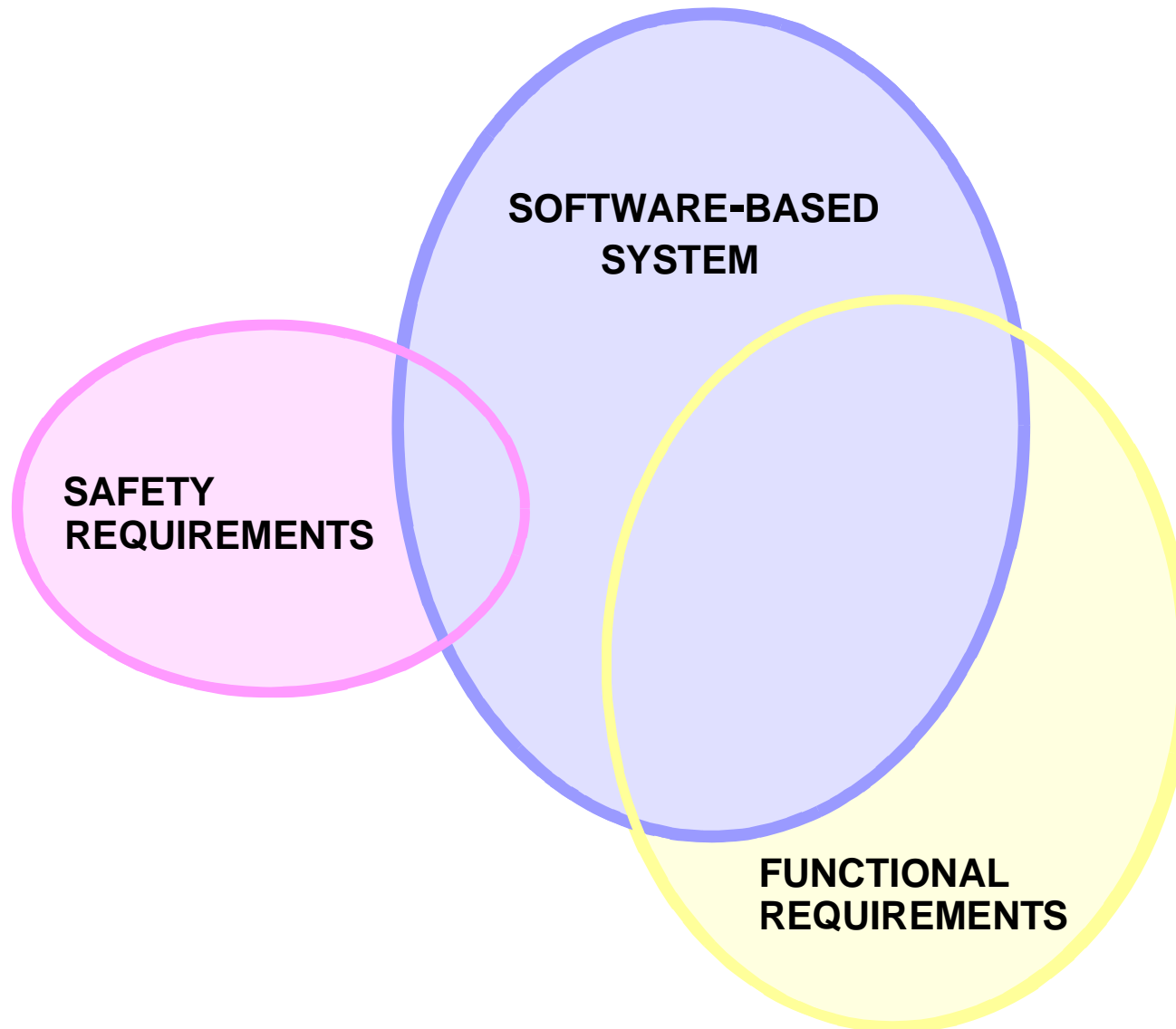
- ❑ **non-deterministic behaviour**

- > *Petri net: time-dependent dynamic conflicts*

- ❑ **dedicated testing techniques to guarantee reproducibility, e.g. Instant Replay**

# **Model Checking of Software-Based Systems**





## ❑ GENERAL PROPERTIES (REQUIREMENTS)

-> *must be valid for any system, independently of its special functionality*

-> *boundedness*

-> *liveness*

-> *reversibility*

...

## ❑ SPECIAL PROPERTIES (REQUIREMENTS)

-> *reflect the special functionality*

-> *(i) insights into system behaviour*

-> *(c) consistency properties to check the model's integrity*

-> *(s) safety properties* - *“something bad never happens”*

-> *(p) progress properties* - *“something good will happen finally”*

...

### ❑ insights (i)

- > *Is it possible that both robot arms hold a plate simultaneously ?*
- > *How many plates can concurrently be inside the system ?*

### ❑ consistency (c)

- > *The swivel is always positioned at exactly one angle.*
- > *At any time, a robot arm can be driven in one direction only.*

### ❑ safety (s)

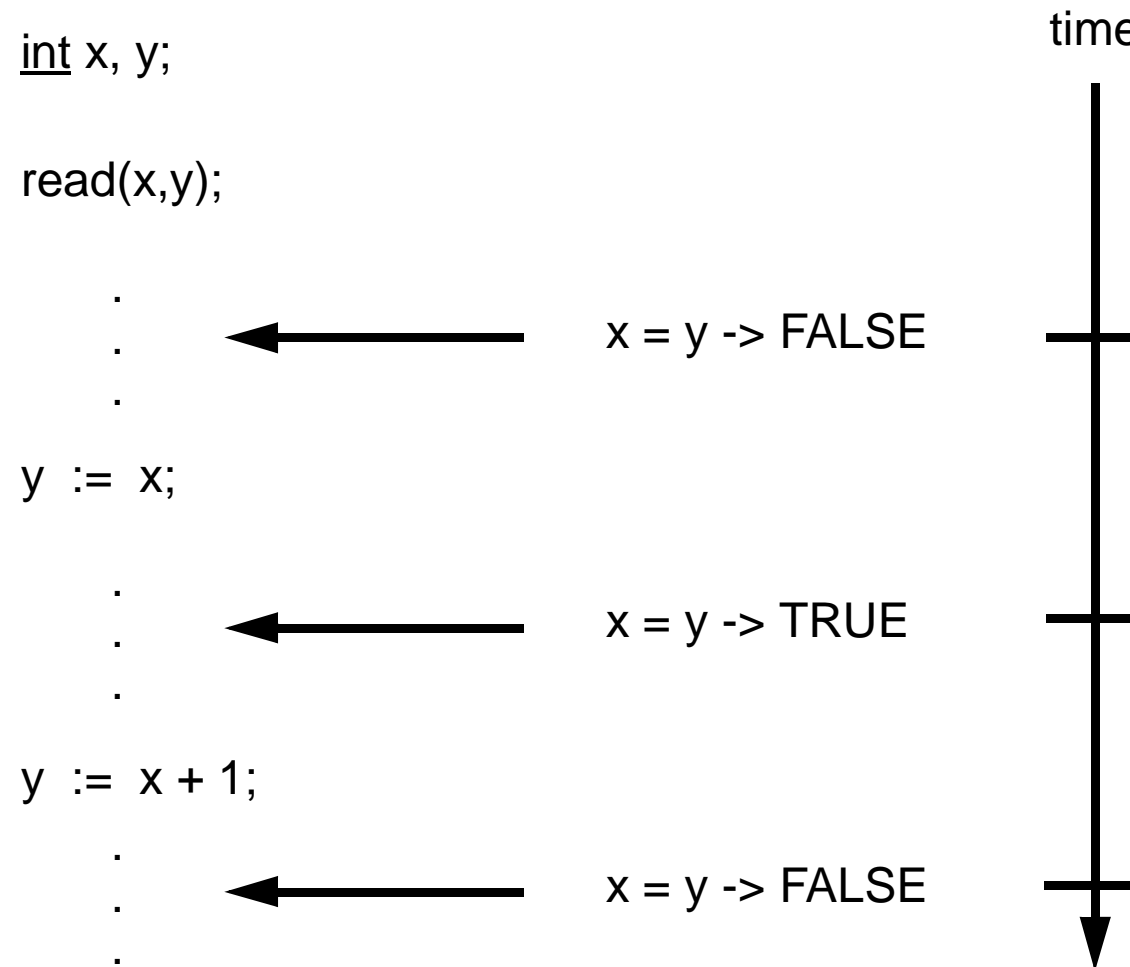
- > *To avoid machine collisions,  
two adjacent pushers will never be moved at the same time.*
- > *The press will only be closed, when no robot arm is positioned inside.*
- > *The feed belt may only convey a blank through its light barrier,  
if the table is in its loading position.*

### ❑ progress (p)

- > *Any plate at the input position will finally reach the cell's output position.*



# Temporal Logics



***How to specify logical statements  
with respect to the execution of a system ?***

- ❑ **extension of classical (propositional) logics by temporal operators**
- ❑ **atomic propositions**
  - > *elementary statements, having - in a given state - a well-defined truth value*
  - > e. g. *mutex*, *for 1-bounded Petri net* (Boolean)
  - > e. g. *buffer = 2, buffer > 2, else* (Integer)
- ❑ **constants**
  - > *TRUE, FALSE*
- ❑ **classical Boolean operators**

<i>negation</i>	<i>!</i>	<i>conjunction</i>	<i>*</i>
<i>disjunction</i>	<i>+</i>	<i>implication</i>	<i>-&gt;</i>
- ❑ **temporal operators**
  - > *to refer to sequences of states*

# CTL OPERATORS, INTERLEAVING SEMANTICS

	next f	finally f	globally f	f1 until f2
on all paths	<p><b>AX</b></p>	<p><b>AF</b></p>	<p><b>AG</b></p>	<p><b>AU</b></p>
on path some	<p><b>EX</b></p>	<p><b>EF</b></p>	<p><b>EG</b></p>	<p><b>EU</b></p>

- ❑ **reachability-related**                      **EF (  $\varphi$  )**  
-> *There exists at least one computation path to reach eventually a state, where  $\varphi$  will be true.*
  
- ❑ **safety-related**                              **AG ( !  $\varphi$  )**                      **-> equivalent to ! EF (  $\varphi$  )**  
-> *For every computation path,  $\varphi$  will never be true.*
  
- ❑ **invariant-related**                        **AG (  $\varphi$  )**                      **-> equivalent to ! EF ( !  $\varphi$  )**  
-> *For every computation path,  $\varphi$  will be true for ever.*
  
- ❑ **liveness-related**                         **AG ( EF (  $\varphi$  ) )**  
-> *What ever happens, there exists the chance (at least one path) that  $\varphi$  will be true again.*
  
- ❑ **progress-related**                         **AG ( AF (  $\varphi$  ) )**  
-> *For every computation path,  $\varphi$  will eventually be true.*

## □ insights / reachability

-> *Is it possible, that both robot arms carry a plate at the same time?*

$EF ( arm1\_mag\_on * arm2\_mag\_on )$

## □ safety property

-> *If a robot arm is loaded, its magnet is not deactivated until the robot is in its unloading position.*

$AG ( \varphi \rightarrow A ( !arm1\_mag\_off \ U \ \psi ) ),$  with

$\varphi = arm1\_mag\_on * arm1\_pickup\_angle * arm1\_pickup\_ext$

$\psi = arm1\_release\_angle * arm1\_release\_ext$

-> *The feed belt may only convey a blank through its light barrier, if the table is in its loading position.*

$G ( belt1\_light\_barrier\_true \rightarrow ( table\_load\_angle * table\_bottom\_pos ) )$

## □ consistency property

-> *The swivel is always either stopped or moves in exactly one direction.*

$G ( robot\_stop \ \underline{xor} \ robot\_left \ \underline{xor} \ robot\_right )$

**Bottleneck:  
State Explosion**  
*(no primitive recursive function ...)*

Number of places/marked places/transitions: 7,000/2,000/5,000

## Number of states:

1137517608656205162806720354362767684058541876947800011092858232169918\\  
1599595881220313326411206909717907134074139603793701320514129462357710\\  
2442895227384242418853247239522943007188808619270527555972033293948691\\  
3344982712874090358789533181711372863591957907236895570937383074225421\\  
4932997350559348711208726085116502627818524644762991281238722816835426\\  
439043702222227167126998740049615901200930144970216630268925118631696\\  
7921927977564308540767556777224220660450294623534355683154921949034887\\  
4138935108726115227535084646719457353408471086965332494805497753382942\\  
1717811011687720510211541690039211766279956422929032376885414750385275\\  
51248819240105363652551190474777411874

**ca.  $1.1 * 10^{667}$**

*Number of places/marked places/transitions: 7000/2000/5000*

*Time to compute P-Invariants: 45885.66 sec*

*Number of P-Invariants: 3000*

*Time to compute compact coding: 385.59 sec*

*Number of Clusters: 3000*

*Number of Variables: 4000*

*Time: 3285.73 sec, ca. 54.75 min*



- ❑ **compositional methods**  
-> *simple interfaces between modules*
  - ❑ **abstraction by ignoring some state information**  
-> *conservative approximation*
  - ❑ **different logics -> different algorithms, e.g. LTL**
  - ❑ **integer programming**
  - ❑ **compressed state space representations**  
-> *BDD, IDD, ...*
  - ❑ **lazy state space construction**  
-> *partial order methods*
  - ❑ **alternative state spaces**  
-> *partial order representations, e.g. prefix*
- 
- 'BASE CASE' TECHNIQUES**
- 'ALTERNATIVE' METHODS (PN)**

semantics time	interleaving	partial order
linear (LTL)	<p><b>traces</b> (no conflict, no concurrency)</p> <p>Manna &amp; Pnueli, Kröger, jsp 2001</p> <p><i>BDD/IDD-LTL, ...</i></p>	<p><b>runs</b> (no conflict, but concurrency)</p> <p>Reisig</p> <p><i>tools: ?</i></p>
branching (CTL)	<p><b>reachability graph</b> (conflict &amp; concurrency not distinguishable)</p> <p>Emmerson, Clarke</p> <p><i>PROD, Charlie, BDD/IDD-CTL, ...</i></p>	<p><b>prefix</b> (conflicts &amp; concurrency)</p> <p>McMillan, Esparza, pd 2001</p> <p><i>PEP</i></p>

technique	CTL	LTL
reachability graph	INA, Charlie	PROD, MARIA
stubborn set reduced reachability graph	LoLA	PROD (LTL\X)
symmetrically reduced reachability graph	LoLA (symmetric formulas)	?
BDD, NDD, ..., xDD	BDD-CTL, SMART, IDD-CTL	BDD-LTL
Kronecker algebra	[Kemper]	?
prefix	PEP (CTL <sub>0</sub> )	QQ (LTL\X)
process automata	[pd]	?

requirement formula	# states generated	time effort
8 a	2259	4.16'
8 b	1775	3.76'
9	2305	4.34'
10	1879	3.10'
15	1184	2.55'
29	704	2.16'
30	703	2.46'
31 a	27104	23.80'
31 b	6433	4.02'

-> control model, 5 plates, full state space: 1,657,242 [7,185,779]

case study	net size	# of states
production cell, 5 plates	231 P / 202 T	$1.6 * 10^6$
production cell, 3 plates		$7.1 * 10^6$
1000 dining philosophers	7,000 P / 5,000 T	$1.1 * 10^{667}$
solitaire, standard		
solitaire, non-standard		
Halobacterium, motor 44		
MAPK cascade, 80 levels		
MAPK cascade, 120 levels		
gene regulation, 6 cells, m01		
gene regulation, 6 cells, m02		

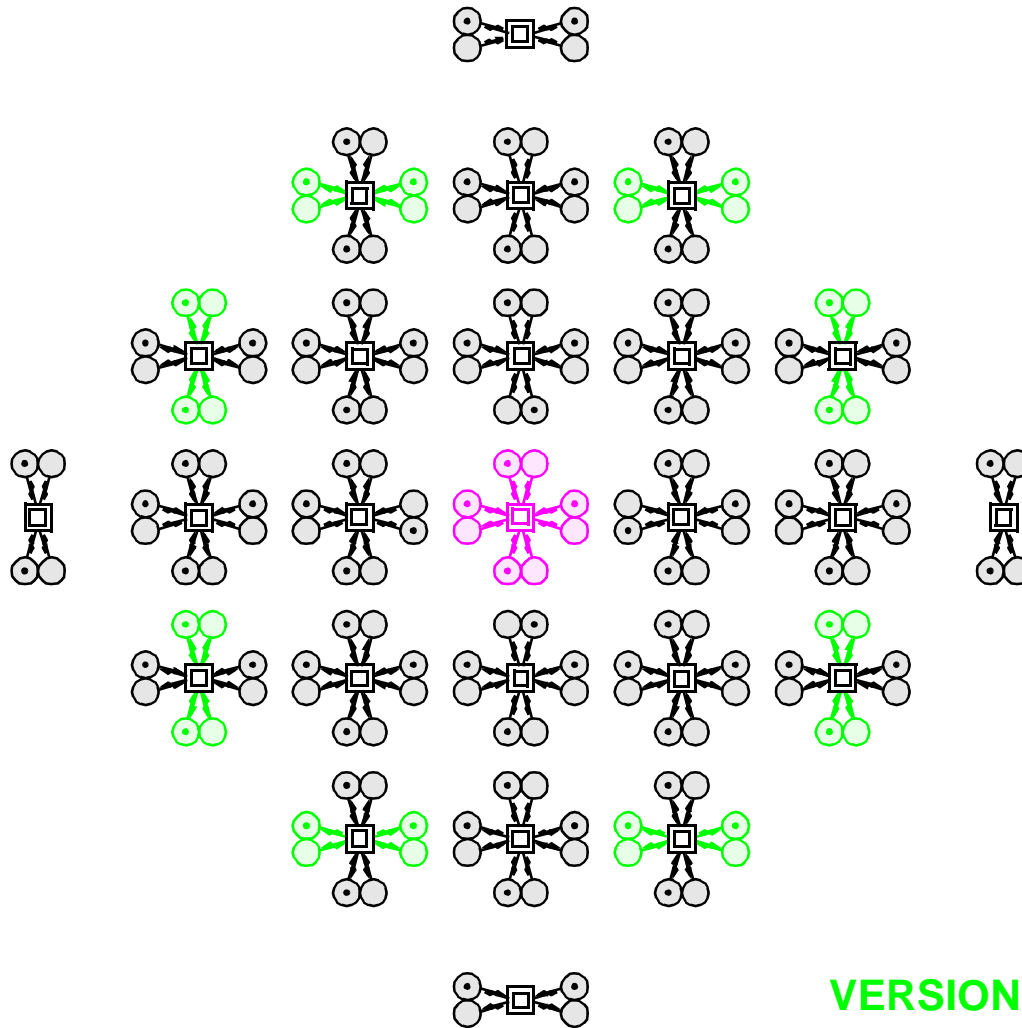
## SOLITAIRE

- two versions,  
green squares Y/N
- all but one squares  
carry tokens
- remove tokens  
by jumbing over them
- goal of the game:  
only one token left
- questions:  
is there a solution ?
- always ?

11	12	13	14	15	16	17
21	22	23	24	25	26	27
31	32	33	34	35	36	37
41	42	43	44	45	46	47
51	52	53	54	55	56	57
61	62	63	64	65	66	67
71	72	73	74	75	76	77

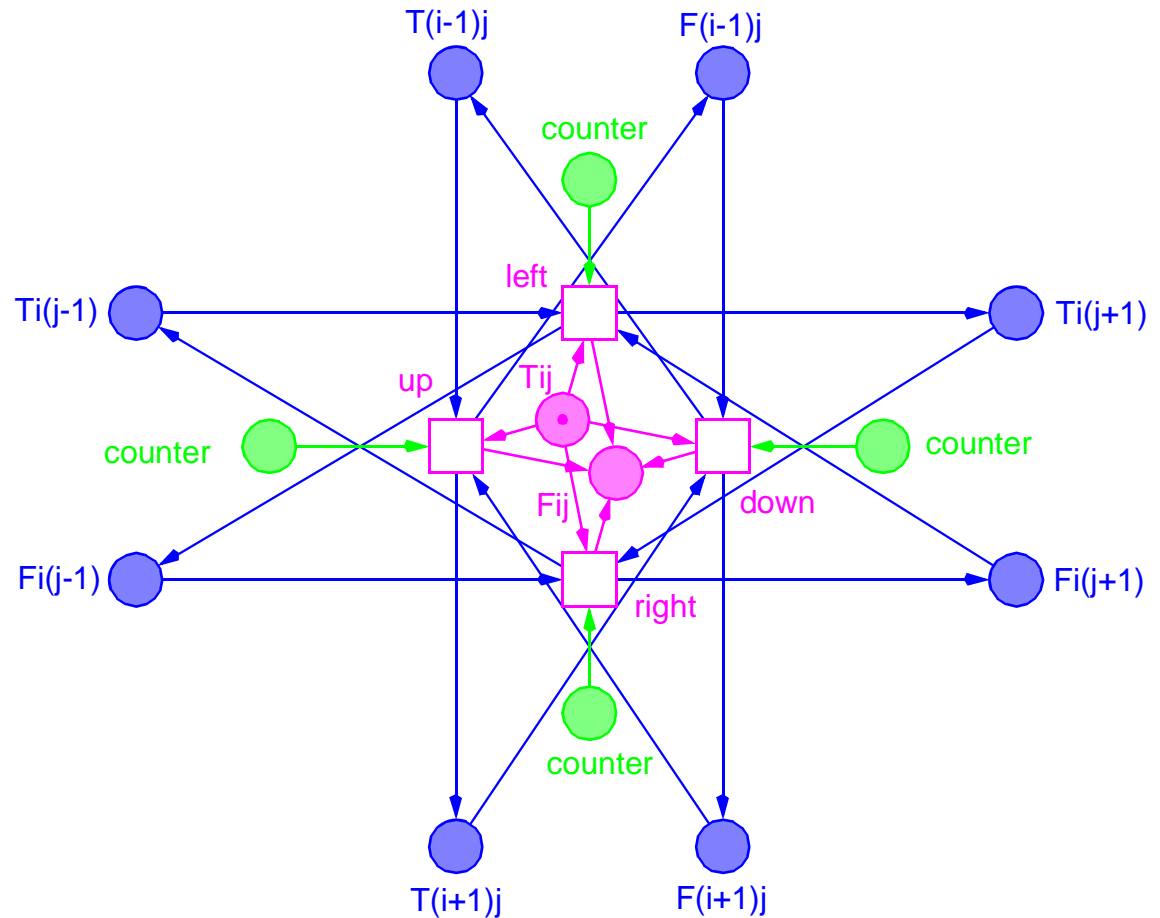
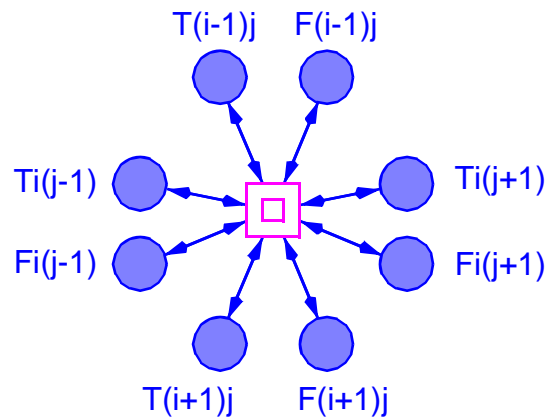
## SOLITAIRE

- ❑ two-level hierarchical pn
- ❑ only one square net component
- ❑ two states for each square  $i$ :  $T(i)$ ,  $F(i)$
- ❑ goal of the game: dead state(s) with  $\sum T(i) = 1$
- ❑ reachable ?
- ❑ for any initial marking ?



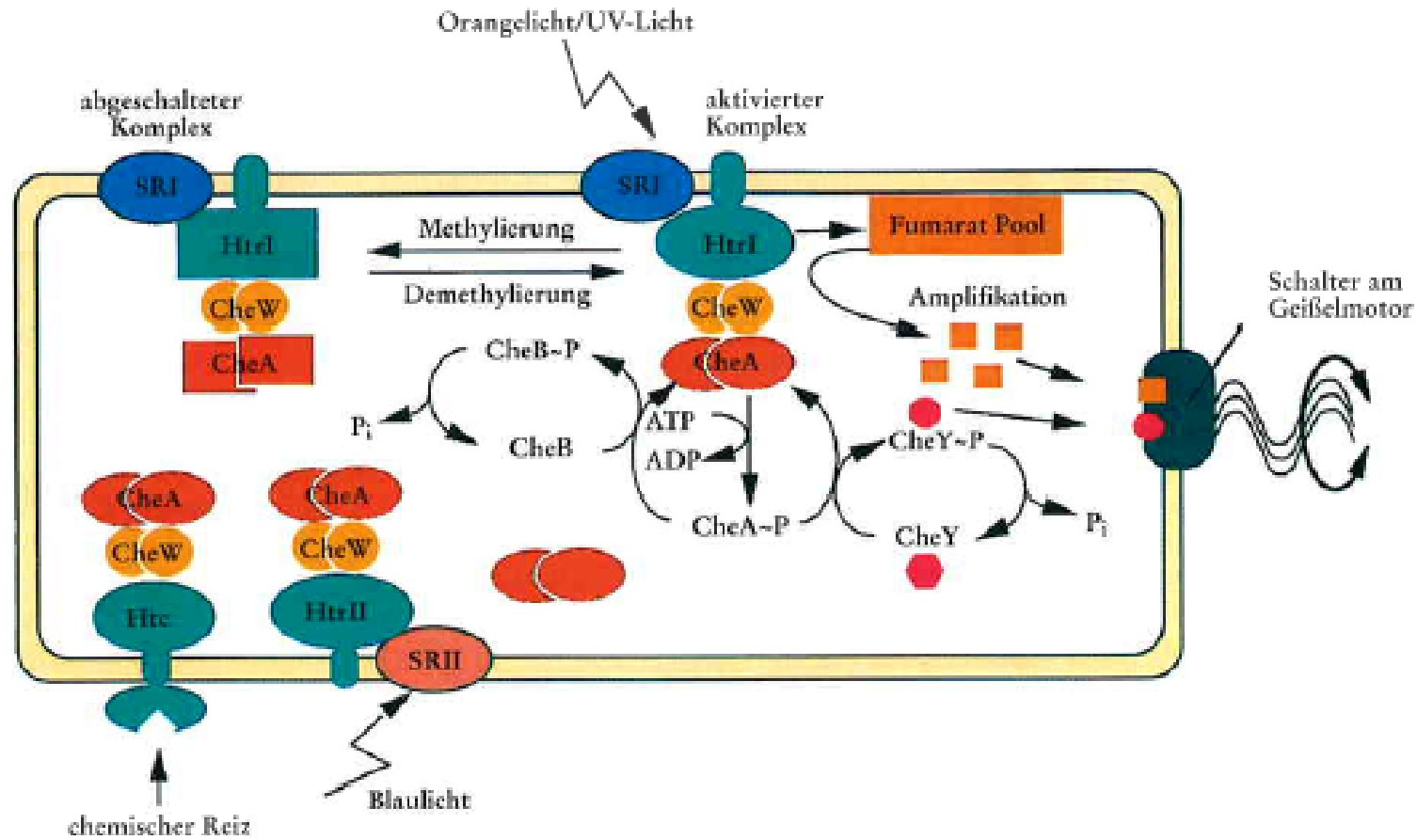
## SOLITAIRE

- square component
- counter facilitates reachability question, but hinders analysis





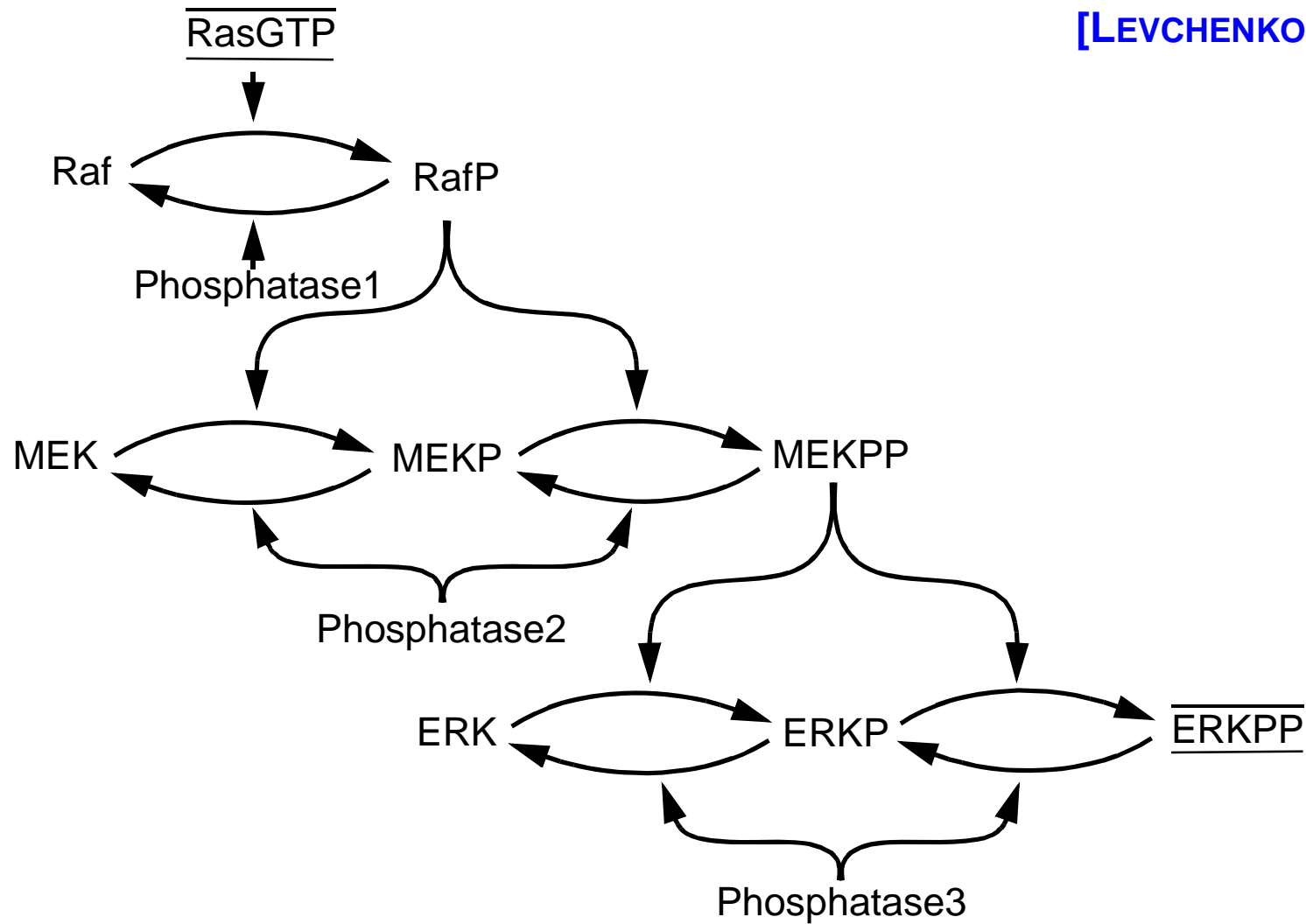
# EXAMPLE - SWITCH CYCLE HALOBACTERIUM SALINARUM



[Marwan; Oesterhelt 1999]



[LEVCHENKO 2000]





case study	net size	# of states
production cell, 5 plates	231 P / 202 T	$1.6 * 10^6$
production cell, 3 plates		$7.1 * 10^6$
1000 dining philosophers	7,000 P / 5,000 T	$1.1 * 10^{667}$
solitaire, standard	65 P / 75 T	$1.8 * 10^8$
solitaire, non-standard	73 P / 91 T	$2.9 * 10^9$
Halobacterium, motor 44	38 P / 60 T	$4.8 * 10^7$
MAPK cascade, 80 levels	22 P / 30 T	$5.6 * 10^{18}$
MAPK cascade, 120 levels		$1.7 * 10^{21}$
gene regulation, 6 cells, m01	144 P / 307 T / 2146 A	$7.4 * 10^{21}$
gene regulation, 6 cells, m02		$3,3 * 10^{25}$

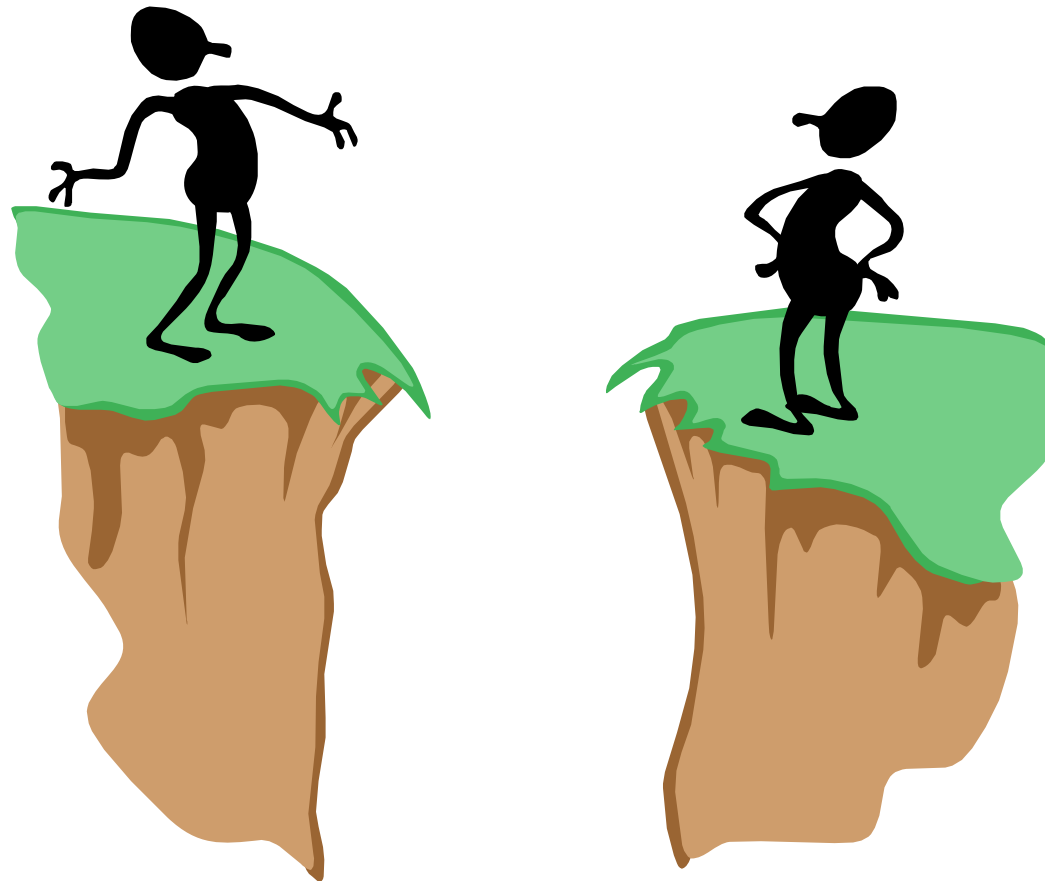
- ❑ **correct model checking requires correct requirement specifications**
  - > *take your time, think twice*
  
- ❑ **model checking proves consistency of**
  - > *model & specification*
  
- ❑ **if the answer is NO (-> FALSE)**
  - > *the model can be wrong*
  - > *the specification can be wrong*
  - > *or both*
  
- ❑ **if the answer is YES (-> TRUE)**
  - > *model & specification can still contain (same) logical faults*
  - > *unlikely !?*
  
- ❑ **Model checking is no substitute for thinking !**

- ❑ **validation can only be as good as the specification**
  - > *readable <-> unambiguous*
  - > *complete <-> limited size*
  
- ❑ **validation is extremely time and resource consuming**
  - > *'external' quality pressure*
  
- ❑ **sophisticated validation is not manageable without theory supported by tools**
  
- ❑ **validation needs knowledgeable professionals**
  - > *study / job specialization*
  - > *profession of "software validator", "software tester"*
  
- ❑ **There is no such thing as a fault-free program !**
  - > *sufficient dependability for a given user profile*
  
- ❑ **Validation is no substitute for thinking !**

**THERE IS NO SUBSTITUTE  
FOR THINKING !**



- ❑ E.M. Clarke, O. Grumberg, and D.A. Peled:  
Model checking;  
MIT Press 1999, third printing, 2001.
  
- ❑ M. Heiner, P. Deussen, S. Spranger:  
A Case Study in Design and Verification of Manufacturing Systems with Hierarchical  
Petri Nets;  
Journal of Advanced Manufacturing Technology (1999), 15, pp. 139-152.
  
- ❑ C. Schröter, S. Schwoon, and J. Esparza:  
The Model Checking Kit.  
In Proc. ICATPN, LNCS 2679, Springer, 2003, pp. 463-472.
  
- ❑ A. Tovchigrechko:  
Model checking using interval decision diagrams;  
PhD thesis, BTU Cottbus, Dep. of CS, 2008.



**Thanks !**

**<http://www-dssz.informatik.tu-cottbus.de>**