

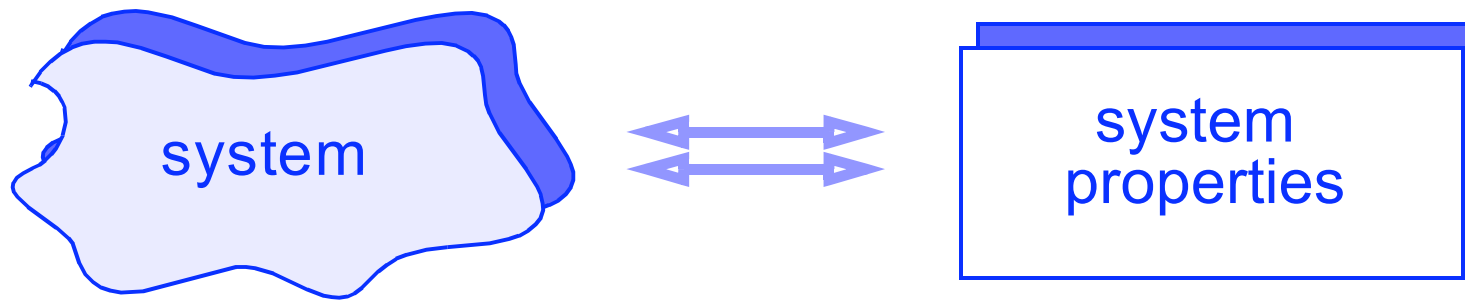
BIOCHEMICAL NETWORKS - A PETRI NET PERSPECTIVE -

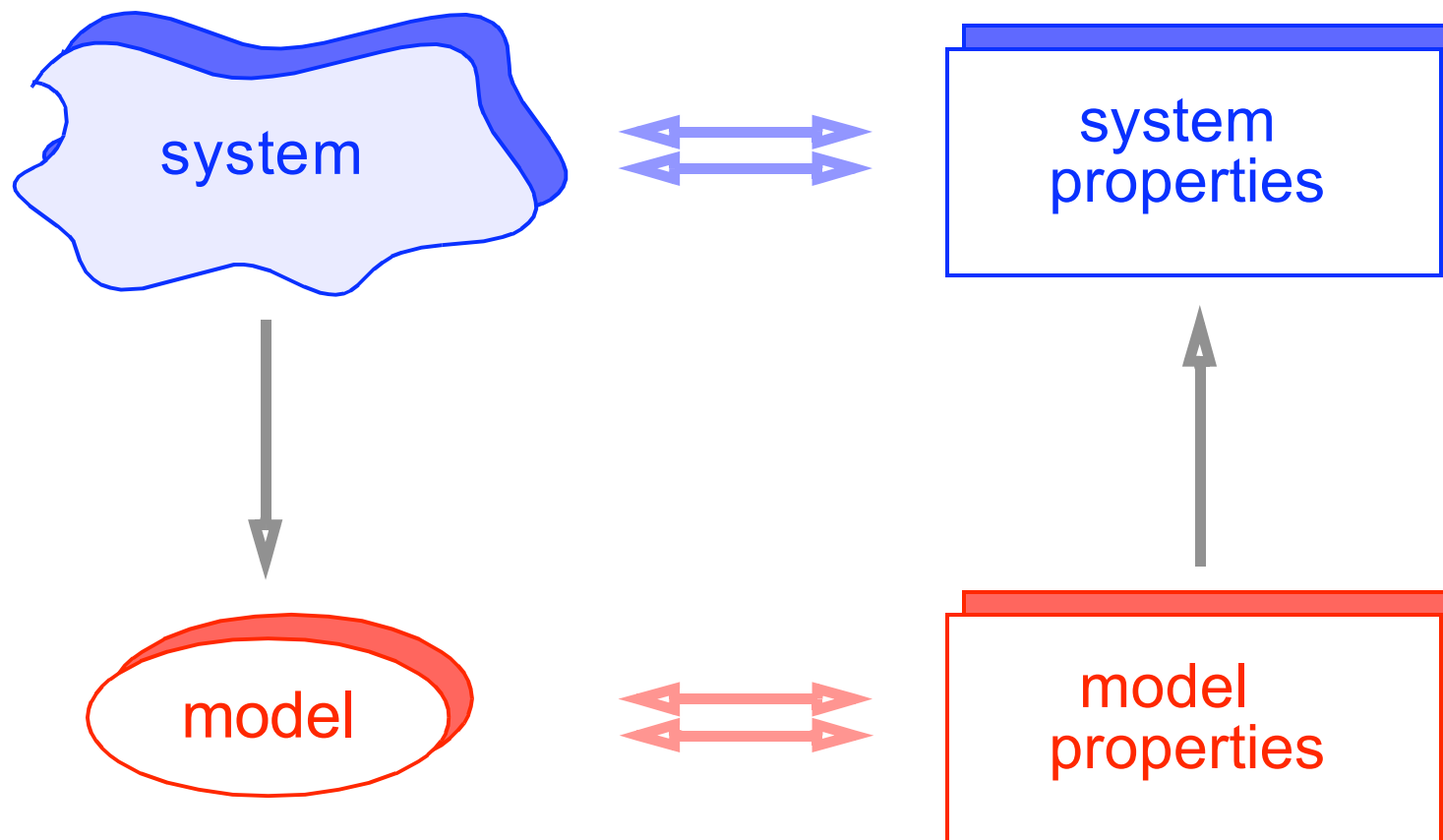
Monika Heiner

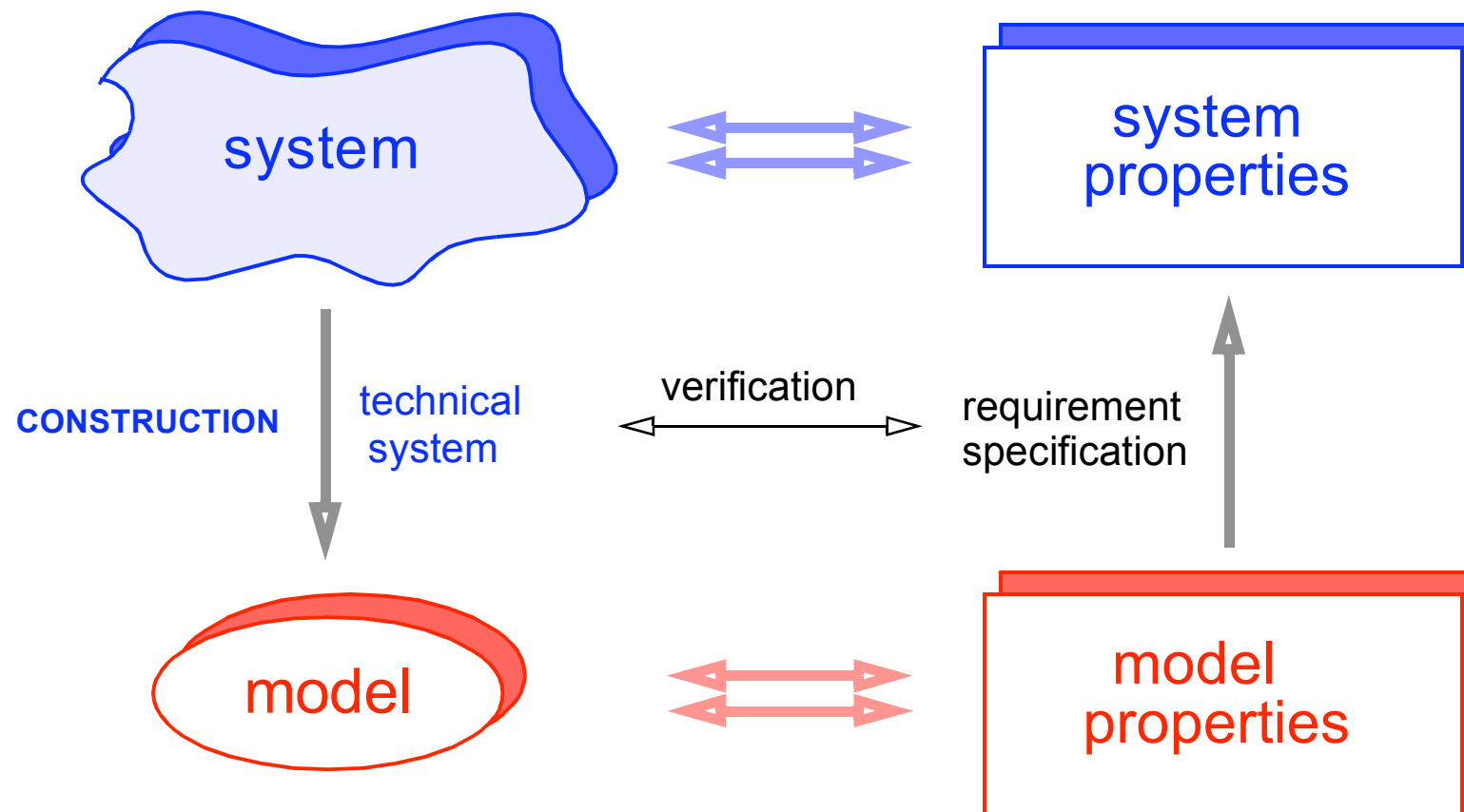
Brandenburg University of Technology

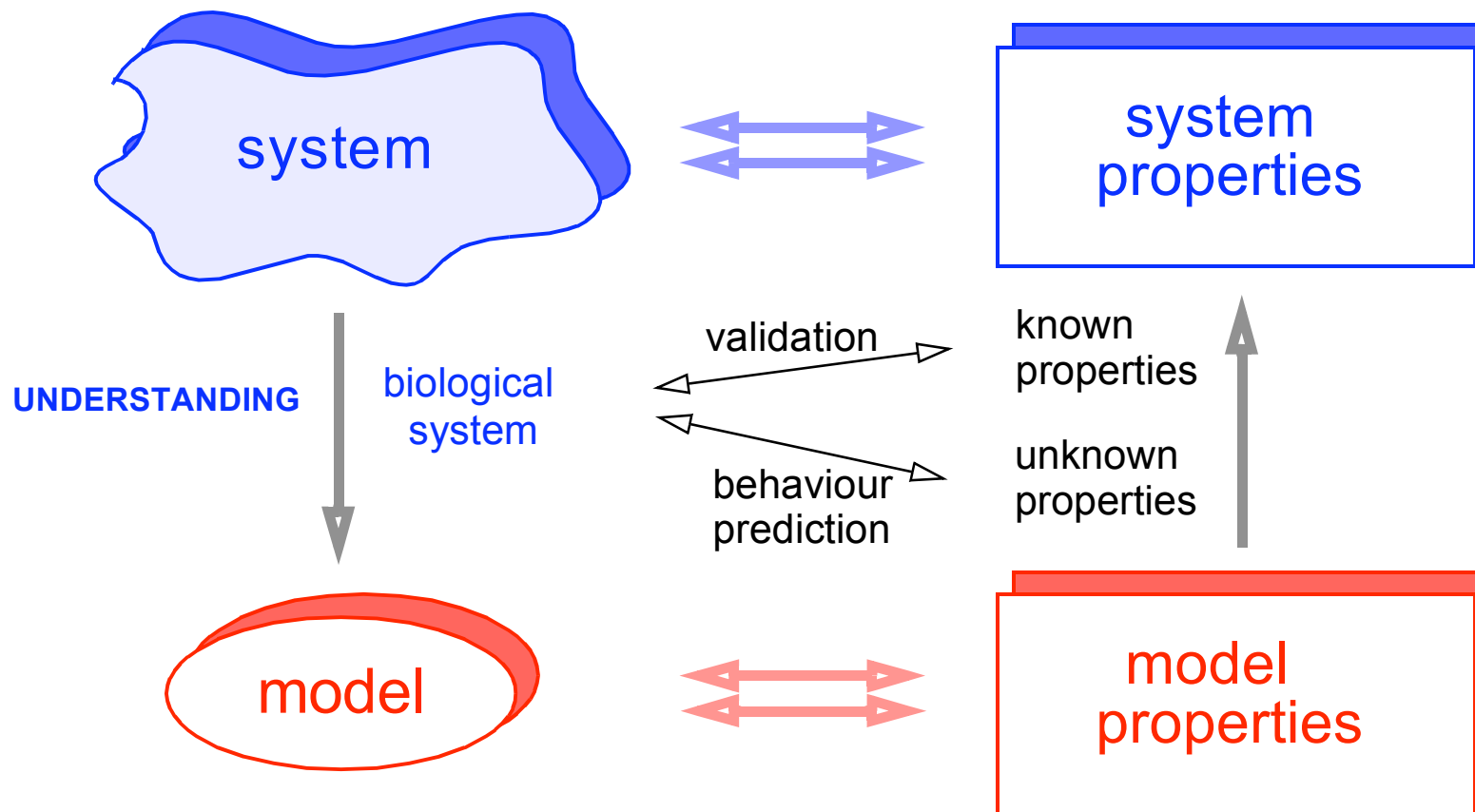
Cottbus

Dept. of CS

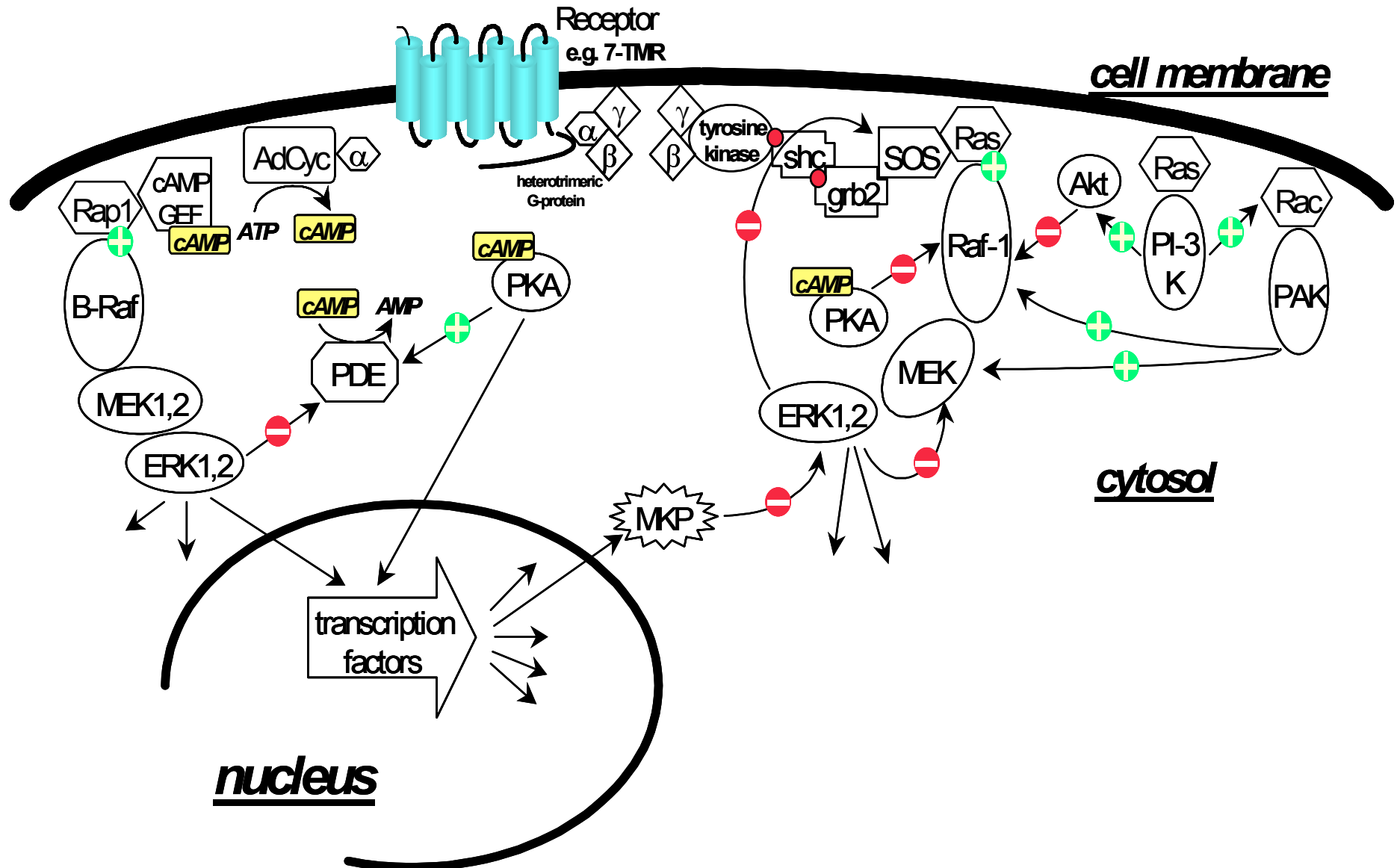


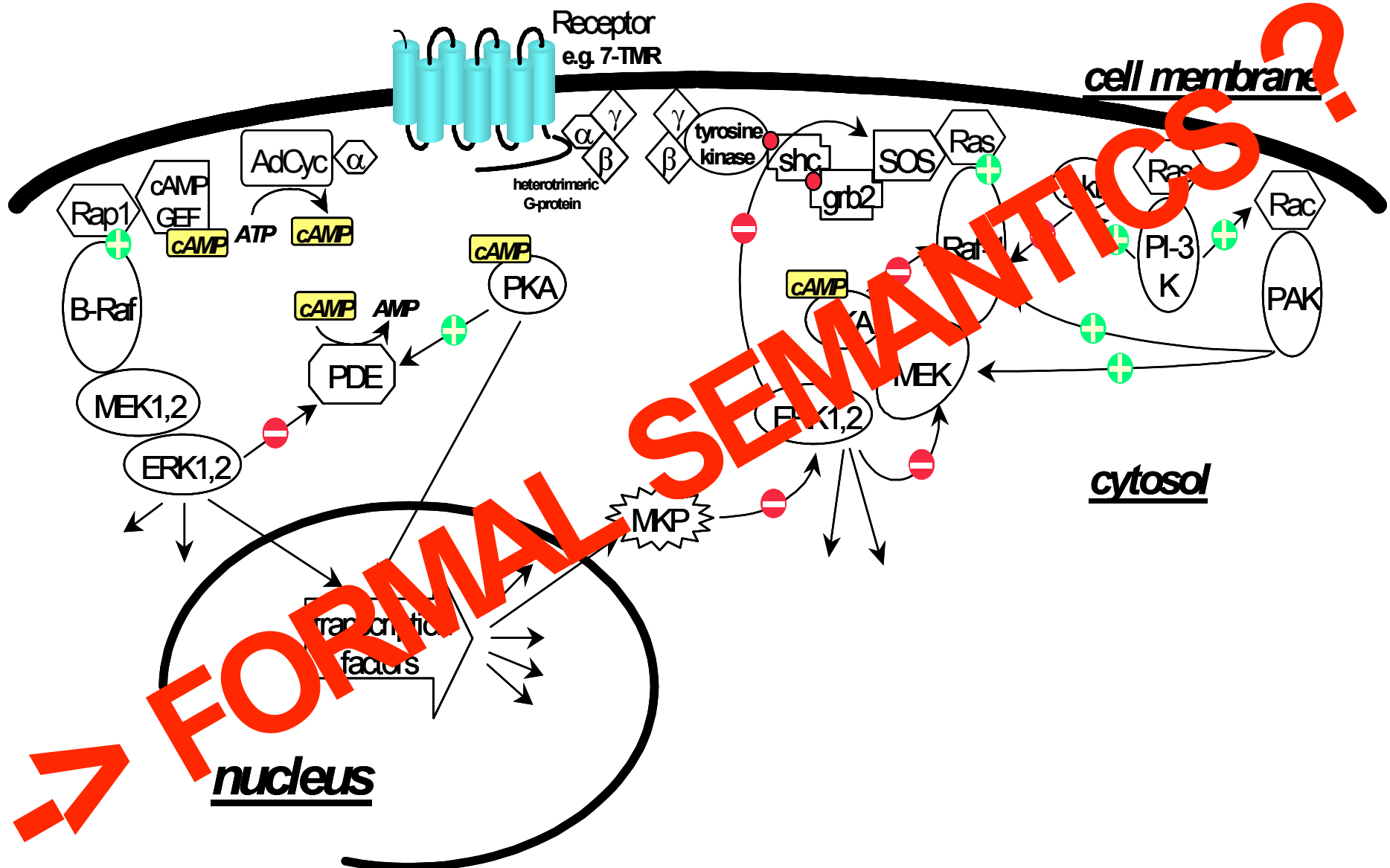






WHAT KIND OF MODEL SHOULD BE USED?





$$\begin{aligned}
 \frac{d\alpha}{dt} &= -v_1 \\
 \frac{dSte2}{dt} &= -v_2 + v_3 - v_5 \\
 \frac{dSte2_{active}}{dt} &= v_2 - v_3 - v_4 \\
 \frac{dSst2_{active}}{dt} &= v_{46} - v_{47} \\
 \frac{dG\alpha\beta\gamma}{dt} &= -v_6 + v_9 \\
 \frac{dG\alpha GTP}{dt} &= v_6 - v_7 - v_8 \\
 \frac{dG\alpha GDP}{dt} &= v_7 + v_8 - v_9 \\
 \frac{dG\beta\gamma}{dt} &= v_6 - v_9 - v_{10} + v_{11} + v_{21} + v_{23} + v_{25} + v_{27} + v_{32} \\
 &\quad - v_{42} + v_{43} \\
 \frac{dSte5}{dt} &= -v_{12} + v_{13} + v_{17} + v_{21} + v_{23} + v_{25} + v_{27} + v_{32} \\
 \frac{dSte11}{dt} &= -v_{12} + v_{13} + v_{17} + v_{21} + v_{23} + v_{25} + v_{27} + v_{32} \\
 \frac{dSte7}{dt} &= -v_{14} + v_{15} + v_{17} + v_{21} + v_{23} + v_{25} + v_{27} + v_{32} \\
 \frac{dFus3}{dt} &= -v_{14} + v_{15} + v_{17} + v_{21} + v_{23} + v_{25} + v_{27} - v_{29} \\
 &\quad + v_{30} + v_{33} \\
 \frac{dSte20}{dt} &= -v_{18} + v_{19} + v_{21} + v_{23} + v_{25} + v_{27} + v_{32}
 \end{aligned}$$

$$\begin{aligned}
 v_1 &= \alpha[t] \cdot Bar1_{active}[t] \cdot k_1 \\
 v_2 &= Ste2[t] \cdot \alpha[t] \cdot k_2 \\
 v_3 &= Ste2_{active}[t] \cdot k_3 \\
 v_4 &= Ste2_{active}[t] \cdot k_4 \\
 v_5 &= Ste2[t] \cdot k_5 \\
 v_6 &= Ste2_{active}[t] \cdot G\alpha\beta\gamma[t] \cdot k_6 \\
 v_7 &= G\alpha GTP[t] \cdot k_7 \\
 v_8 &= G\alpha GTP[t] \cdot Sst2_{active}[t] \cdot k_8 \\
 v_9 &= G\alpha GDP[t] \cdot G\beta\gamma[t] \cdot k_9 \\
 v_{10} &= G\beta\gamma[t] \cdot C[t] \cdot k_{10} \\
 v_{11} &= D[t] \cdot k_{11} \\
 v_{12} &= Ste5[t] \cdot Ste11[t] \cdot k_{12} \\
 v_{13} &= A[t] \cdot k_{13} \\
 v_{14} &= Ste7[t] \cdot Fus3[t] \cdot k_{14} \\
 v_{15} &= B[t] \cdot k_{15} \\
 v_{16} &= A[t] \cdot B[t] \cdot k_{16} \\
 v_{17} &= C[t] \cdot k_{17} \\
 v_{18} &= D[t] \cdot Ste20[t] \cdot k_{18}
 \end{aligned}$$

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 \frac{dG\beta\gamma}{dt} &= v_6 - v_9 - v_{10} + v_{11} + v_{21} + v_{23} + v_{25} + v_{27} + v_{32} \\
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 v_4 &= Ste2_{active}[t] \cdot k_4 \\
 v_5 &= Ste2[t] \cdot k_5 \\
 v_6 &= Ste2_{active}[t] \cdot G\alpha\beta\gamma[t] \cdot k_6 \\
 v_7 &= G\alpha GTP[t] \cdot k_7 \\
 v_8 &= G\alpha GTP[t] \cdot Sst2_{active}[t] \cdot k_8 \\
 v_9 &= G\alpha GDP[t] \cdot G\beta\gamma[t] \cdot k_9 \\
 v_{10} &= G\beta\gamma[t] \cdot C[t] \cdot k_{10} \\
 v_{11} &= D[t] \cdot k_{11} \\
 v_{12} &= Ste5[t] \cdot Ste11[t] \cdot k_{12} \\
 v_{13} &= A[t] \cdot k_{13} \\
 v_{14} &= Ste7[t] \cdot Fus3[t] \cdot k_{14} \\
 v_{15} &= B[t] \cdot k_{15} \\
 v_{16} &= A[t] \cdot B[t] \cdot k_{16} \\
 v_{17} &= C[t] \cdot k_{17} \\
 v_{18} &= D[t] \cdot Ste20[t] \cdot k_{18}
 \end{aligned}$$

❑ knowledge

-> **PROBLEM 1**

- > *uncertain*
- > *growing, changing*
- > *distributed over independent data bases, papers, journals, . . .*

❑ various, mostly ambiguous representations

-> **PROBLEM 2**

- > *verbose descriptions*
- > *diverse graphical representations*
- > *contradictory and / or fuzzy statements*

❑ network structure

-> **PROBLEM 3**

- > *tends to grow fast*
- > *dense, apparently unstructured*
- > *hard to read*

❑ knowledge

-> **PROBLEM 1**

- > *uncertain*
- > *growing, changing*
- > *distributed over independent data bases, papers, journals, . . .*

❑ various, mostly ambiguous representations

-> **PROBLEM 2**

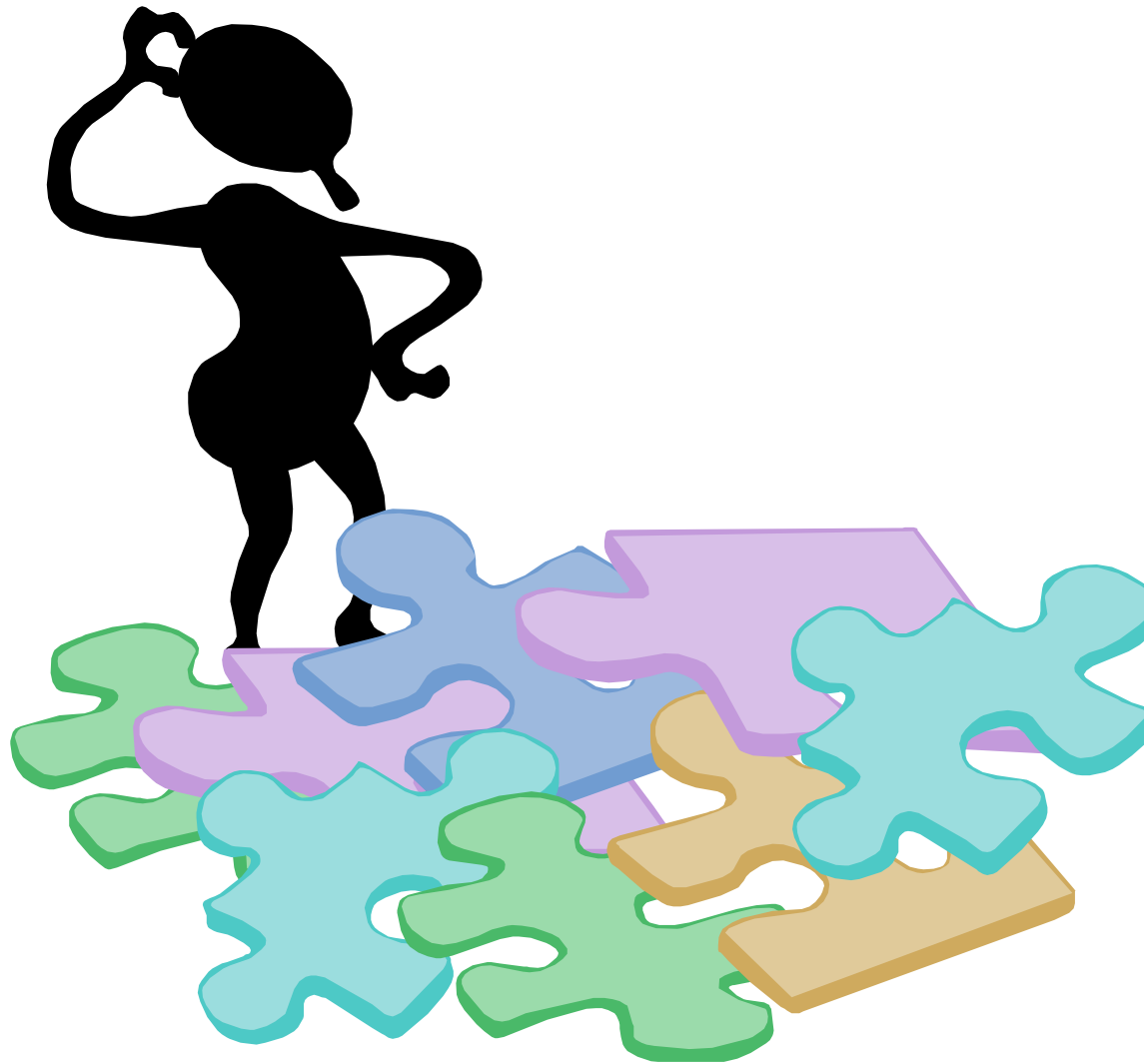
- > *verbose descriptions*
- > *diverse graphical representations*
- > *contradictory and / or fuzzy statements*

❑ network structure

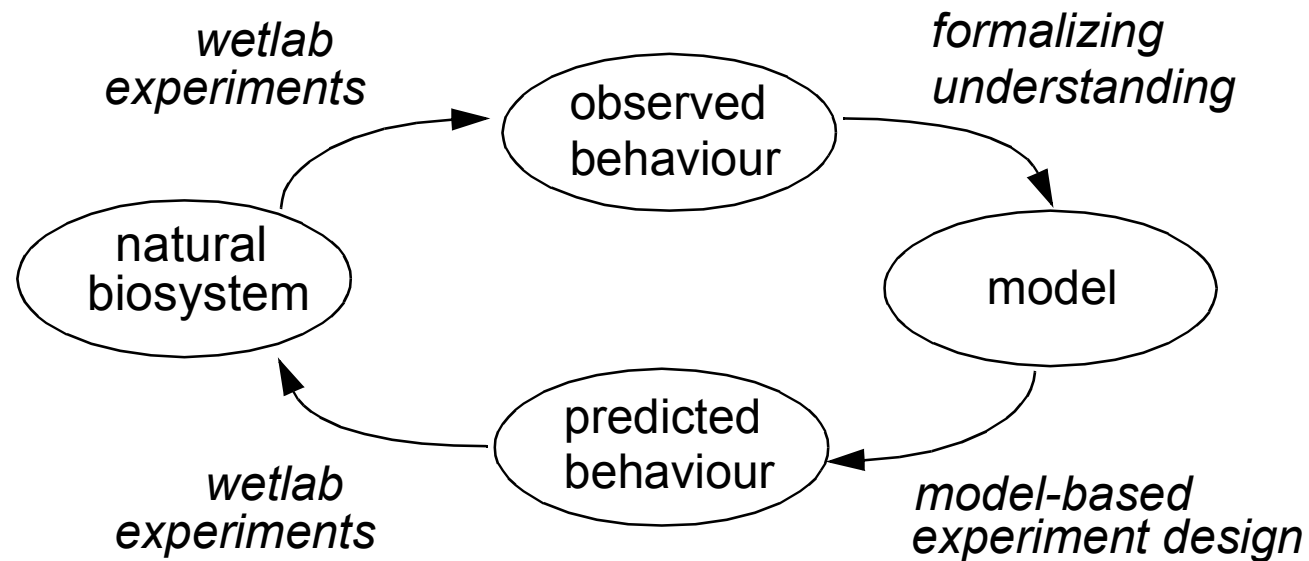
-> **PROBLEM 3**

- > *tends to grow fast*
- > *dense, apparently unstructured*
- > *hard to read*

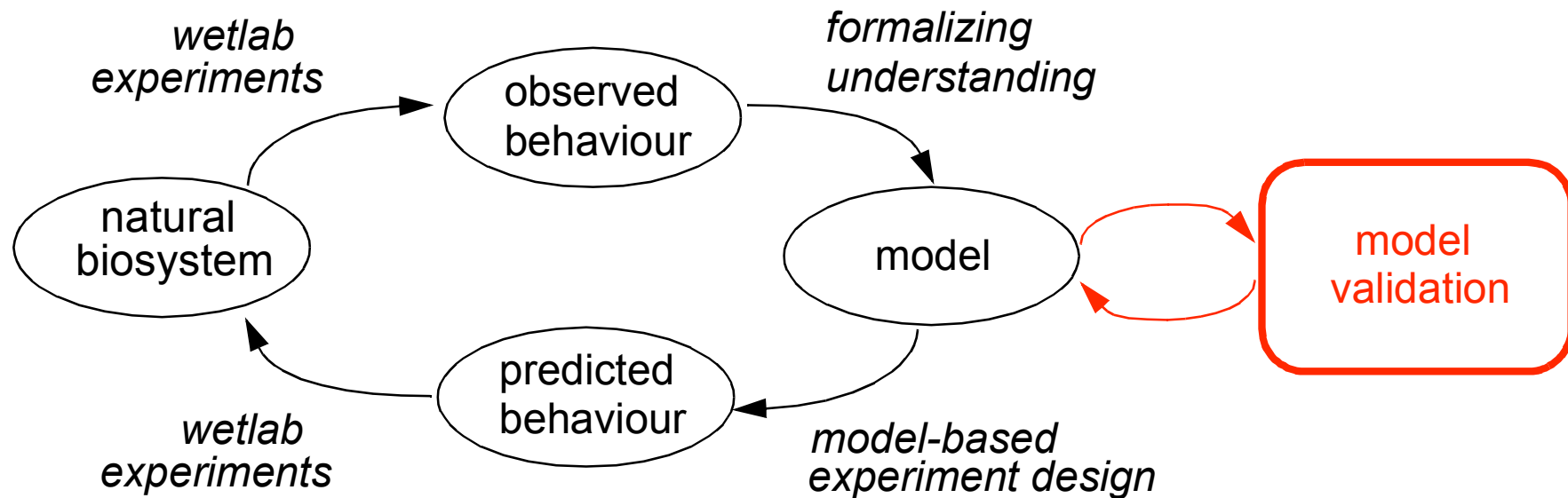
-> MODELS ARE FULL OF ASSUMPTIONS <-



MODELLING = FORMAL KNOWLEDGE REPRESENTATION



MODELLING = FORMAL KNOWLEDGE REPRESENTATION



MODEL VALIDATION = CONFIDENCE INCREASE

☐ **readable**

- > *fault avoidance*
- > *informal = cartoon-like representations ?*

☐ **analysable**

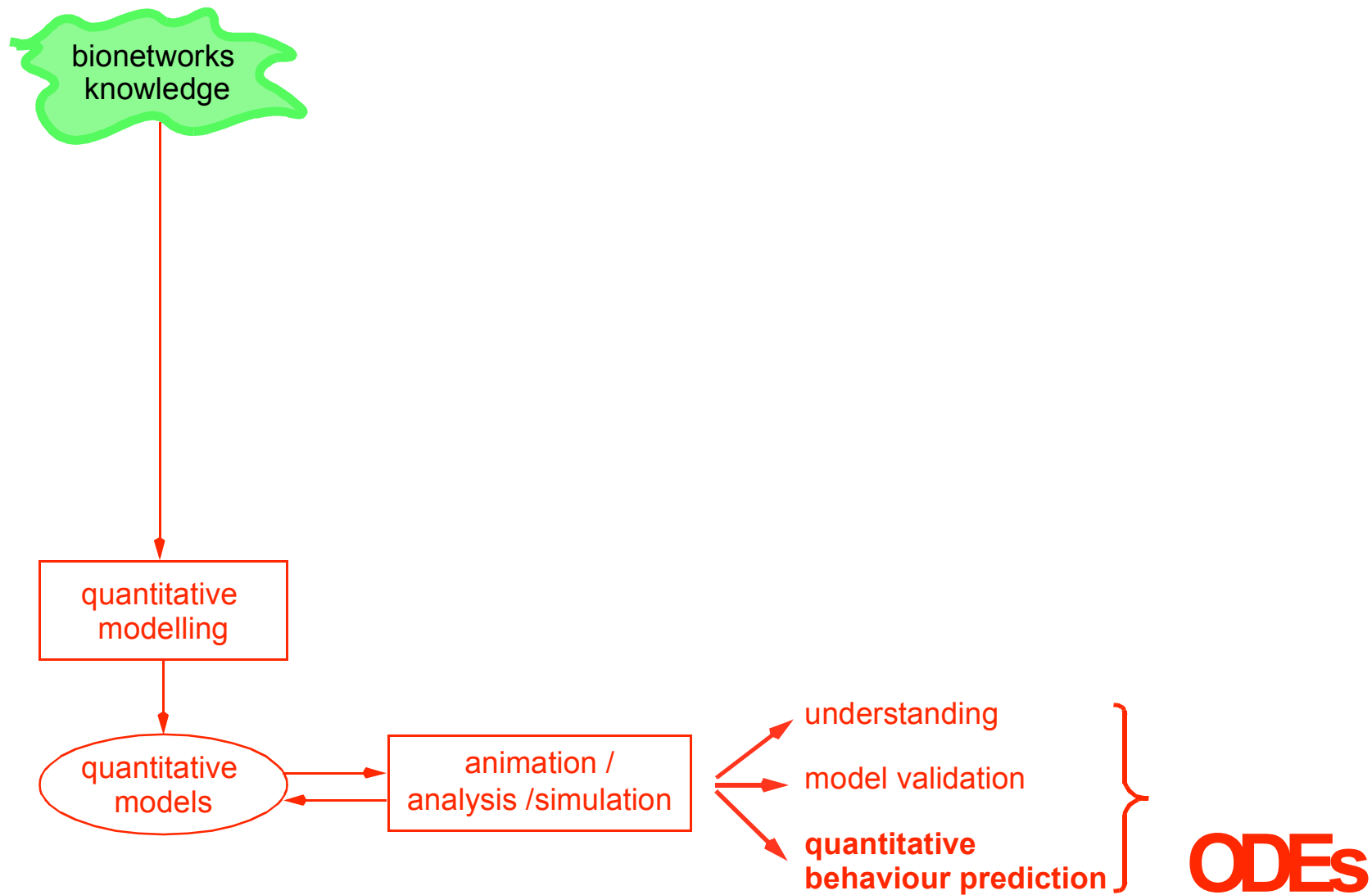
- > *formal = mathematical representations*

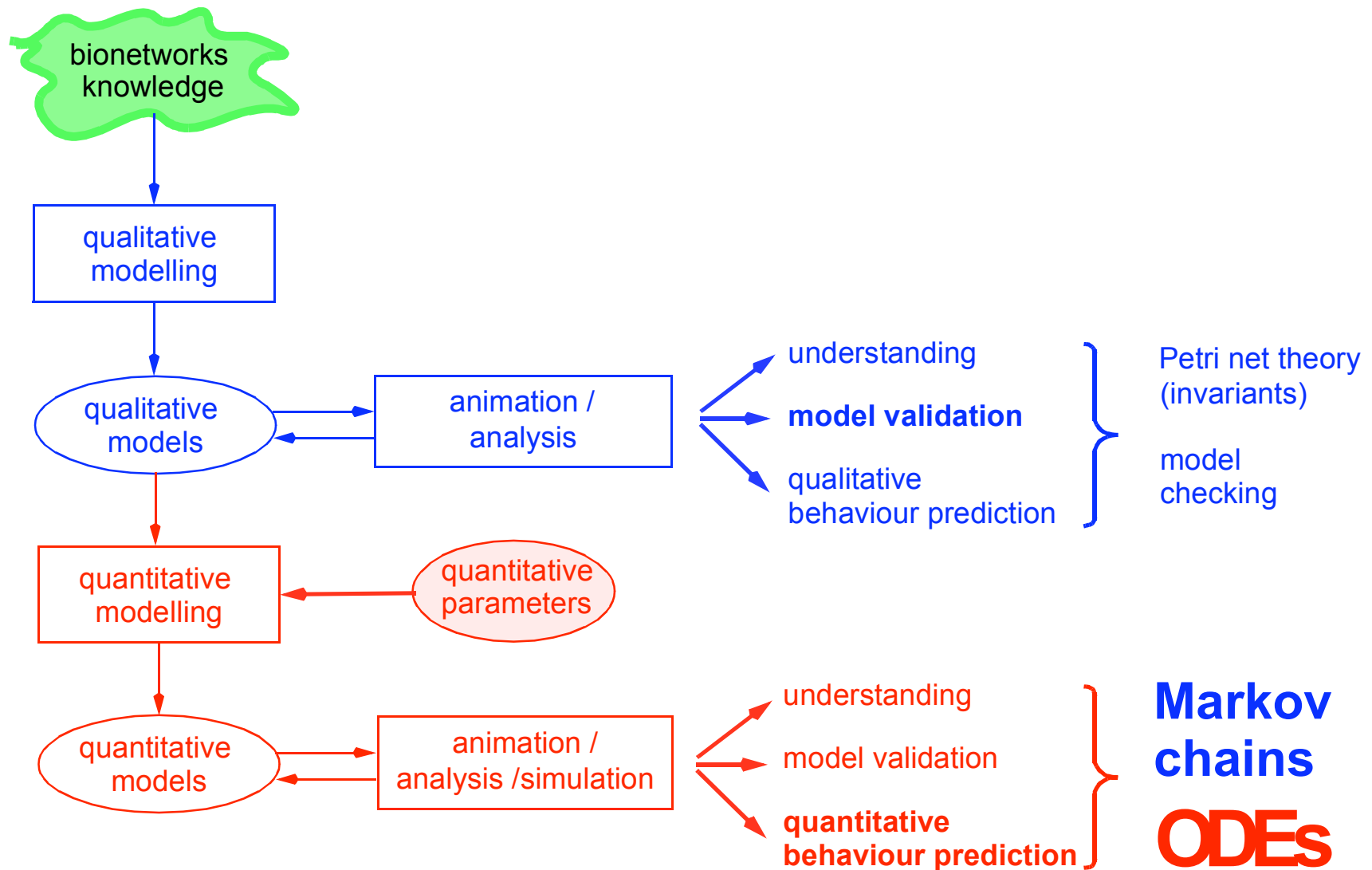
☐ **executable**

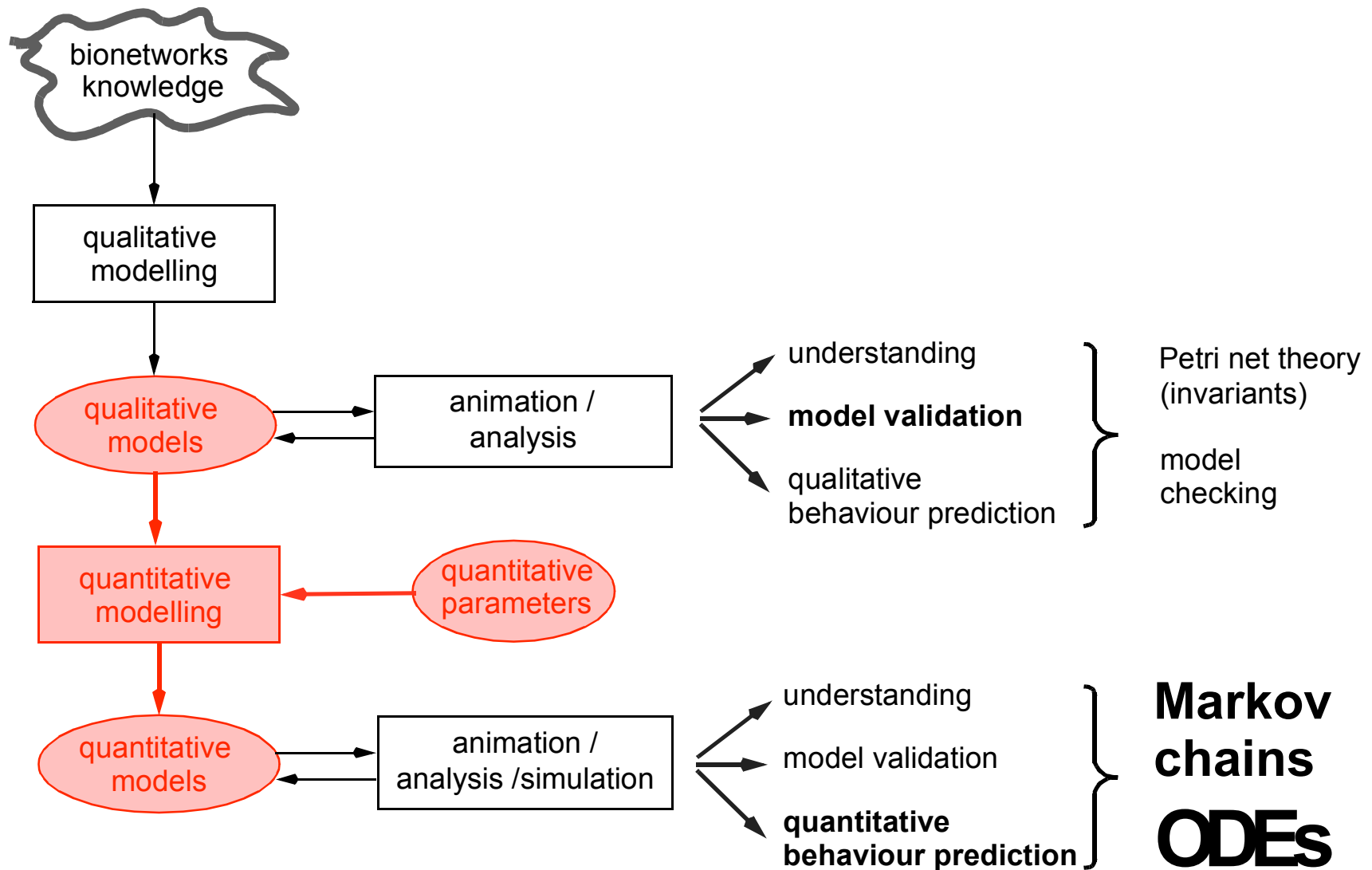
- > *to experience the model*

☐ **unifying power**

- > *high-level description for various analysis approaches*



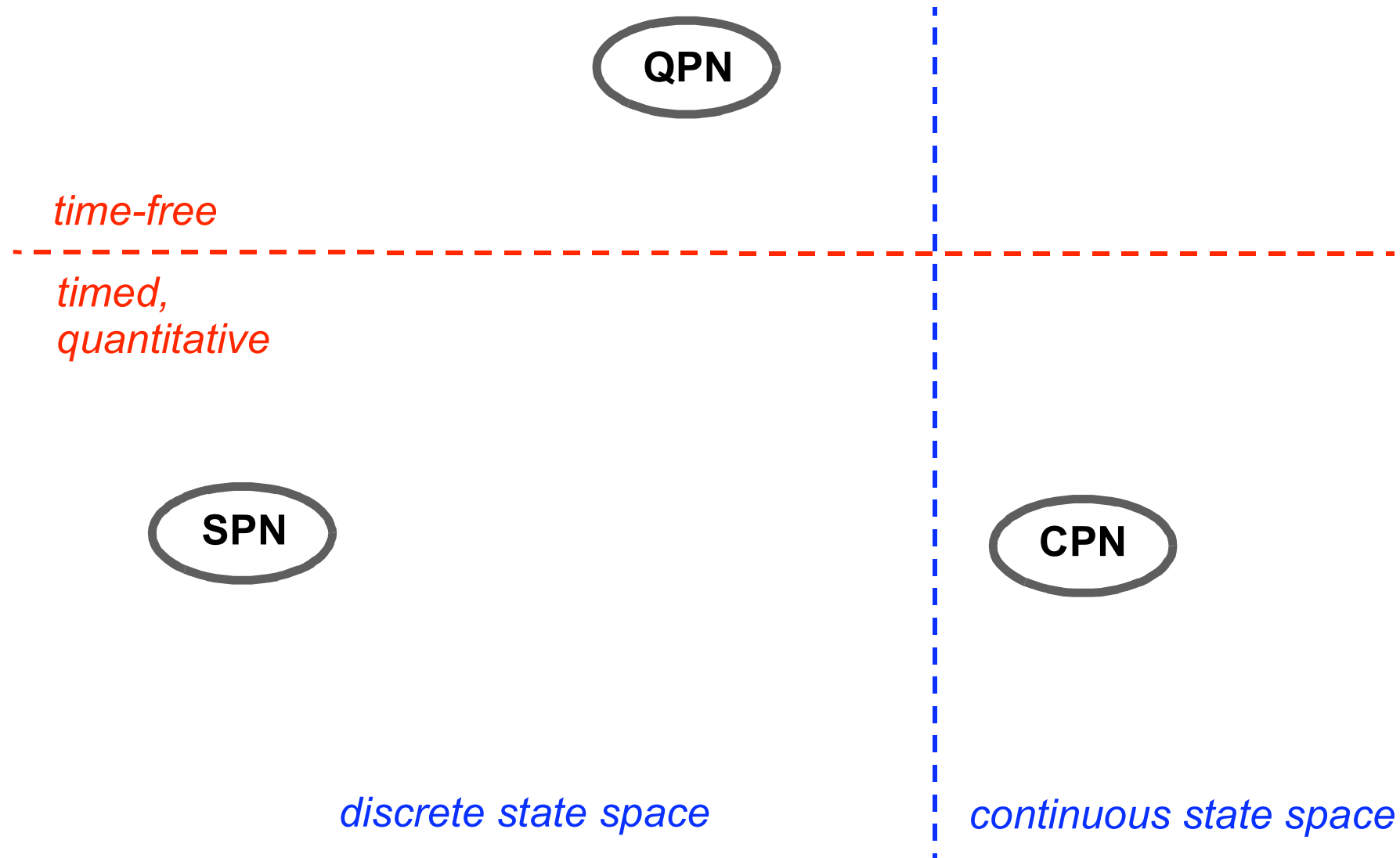


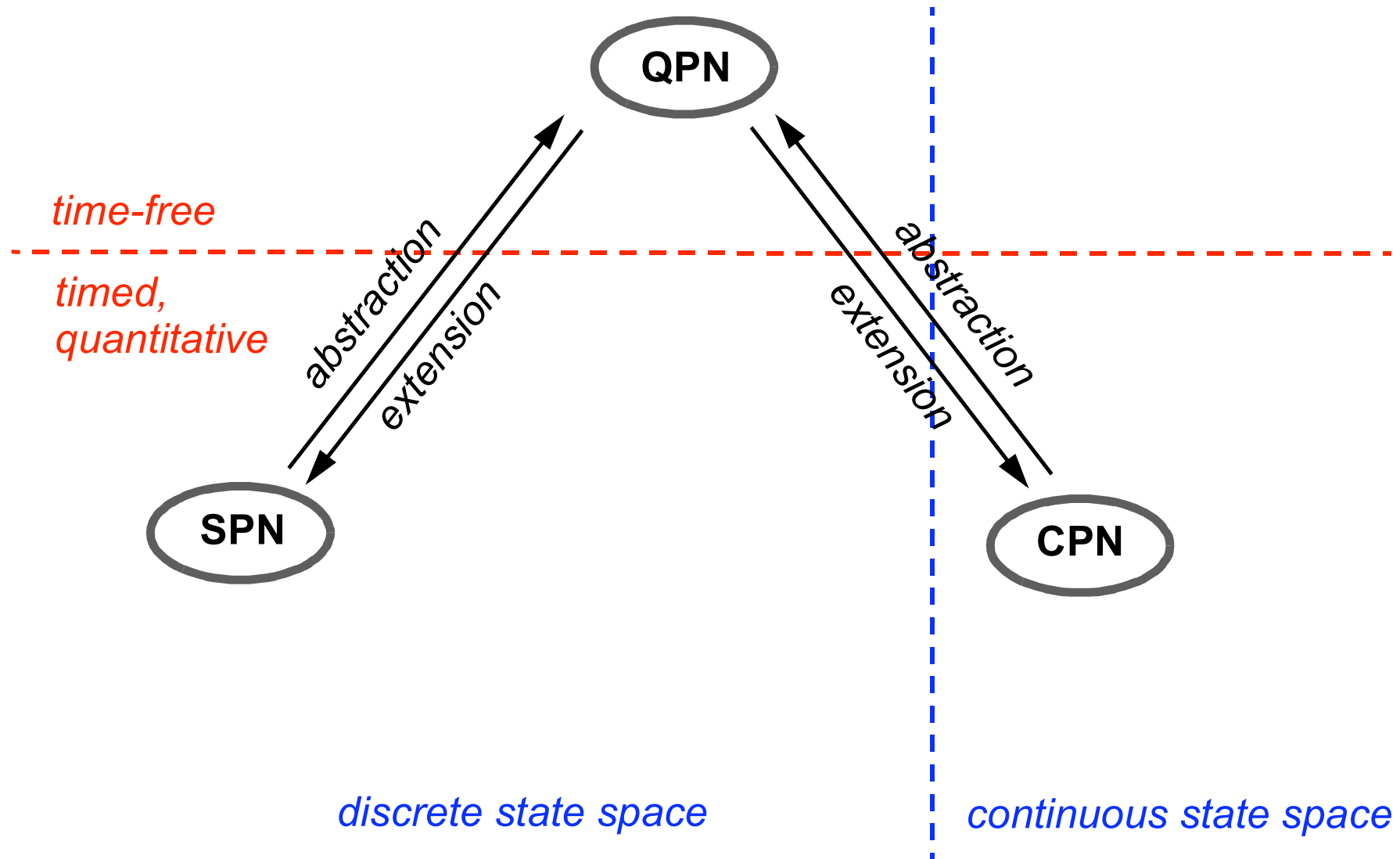


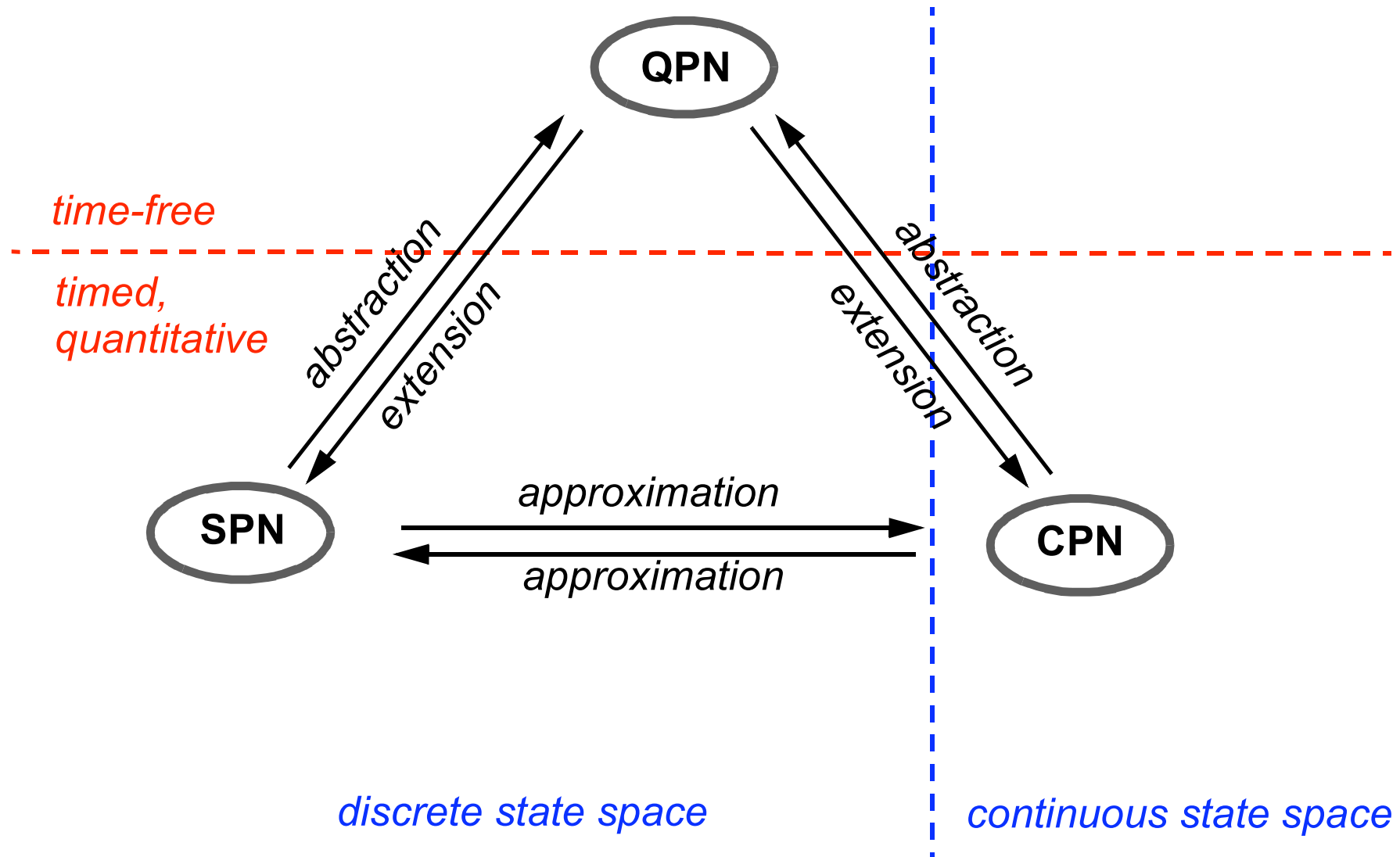
QPN

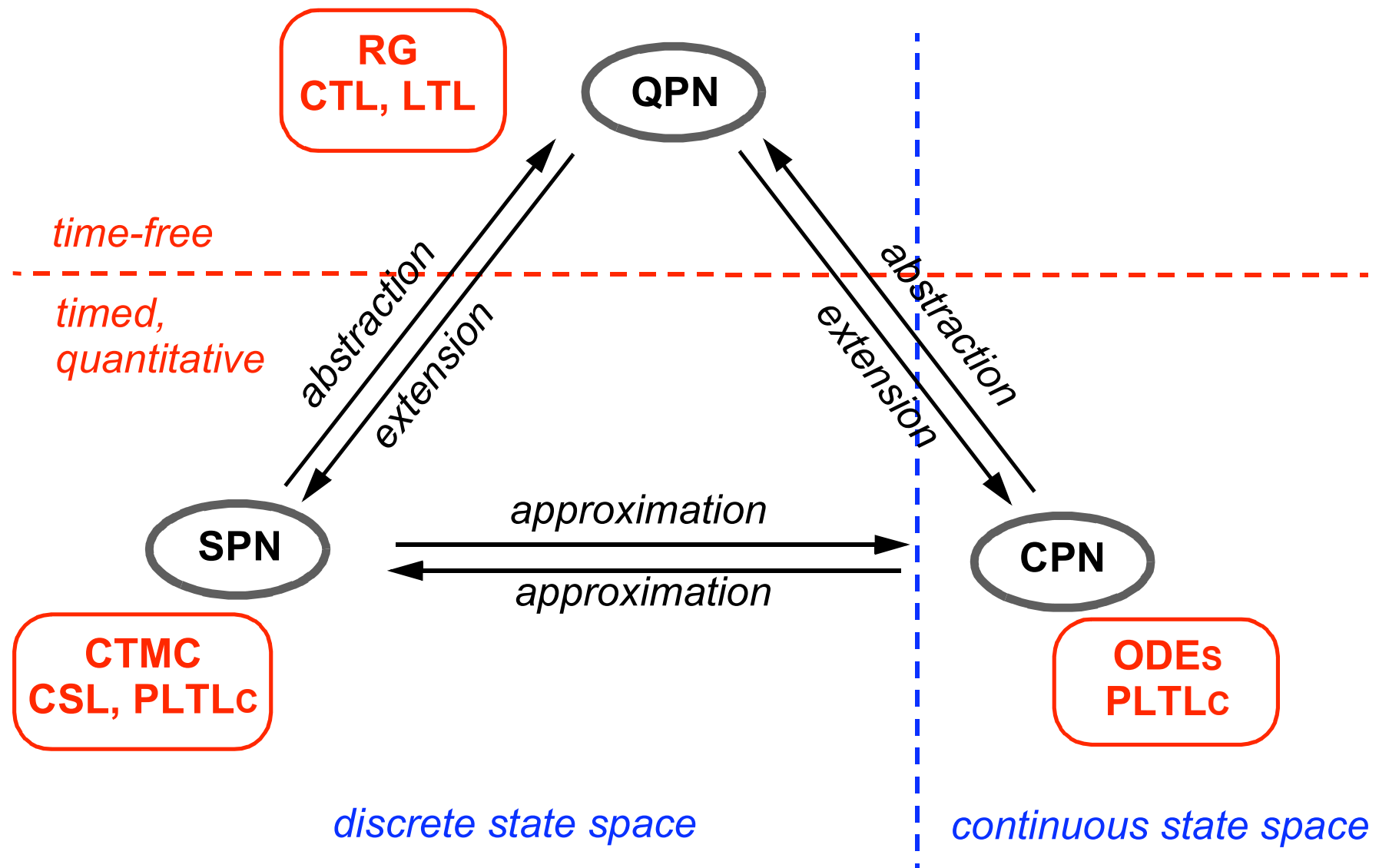
SPN

CPN

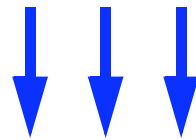








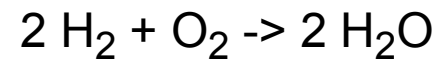
THREE MODELS SHARING STRUCTURE

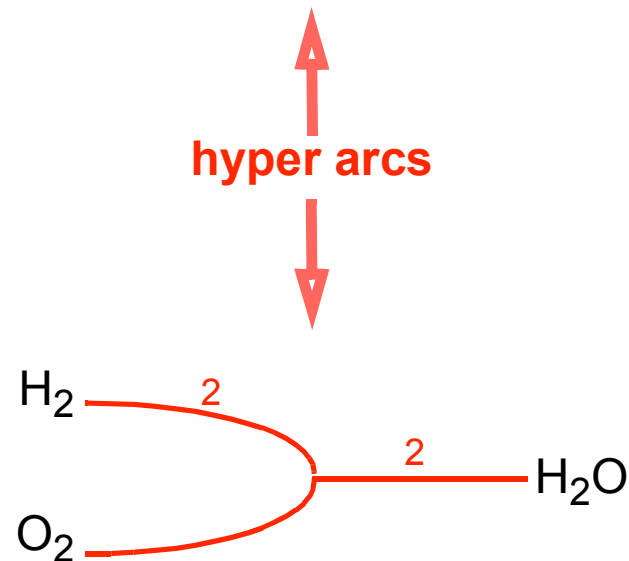
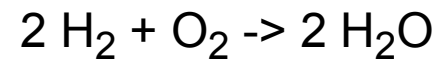


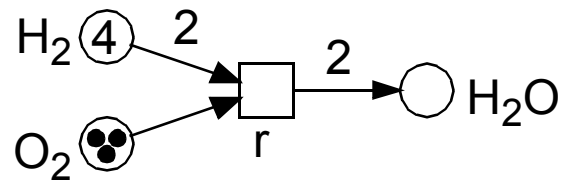
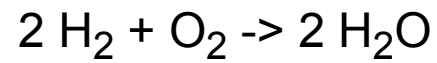
**QUANTITATIVE MODEL = QUALITATIVE MODEL
+
QUANTITATIVE PARAMETERS
(KINETICS)**

QUALITATIVE PETRI NETS - QPN -

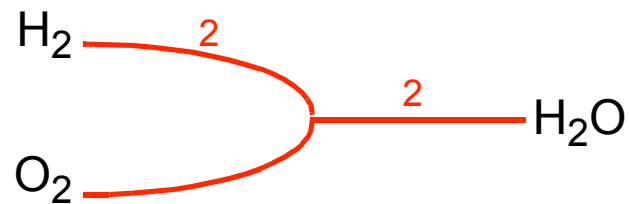
***. . . ARE
NETWORKS OF
(BIO-) CHEMICAL REACTIONS***



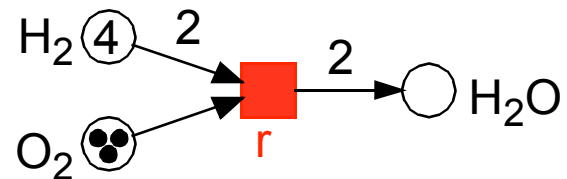
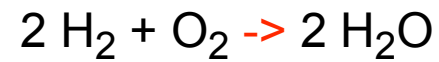




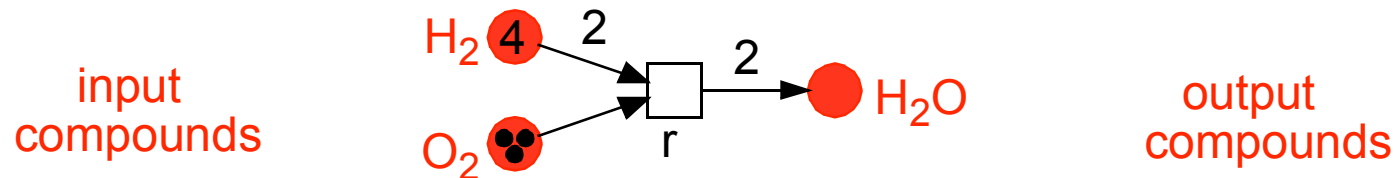
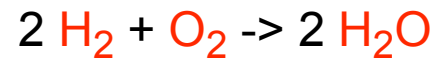
hyper arcs



□ **atomic actions** **-> Petri net transitions** **-> chemical reactions**

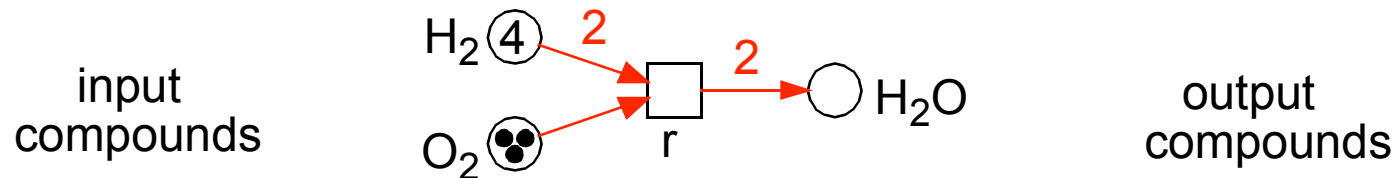
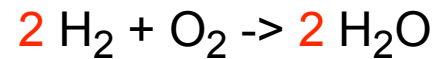


❑ **atomic actions** -> **Petri net transitions** -> **chemical reactions**



❑ **local conditions** -> **Petri net places** -> **chemical compounds**

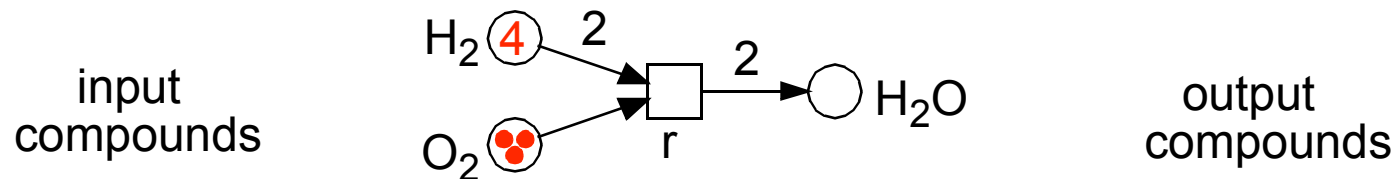
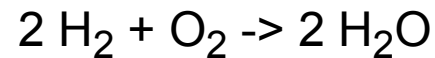
❑ atomic actions -> Petri net transitions -> chemical reactions



❑ local conditions -> Petri net places -> chemical compounds

❑ multiplicities -> Petri net arc weights -> stoichiometric relations

❑ atomic actions -> Petri net transitions -> chemical reactions



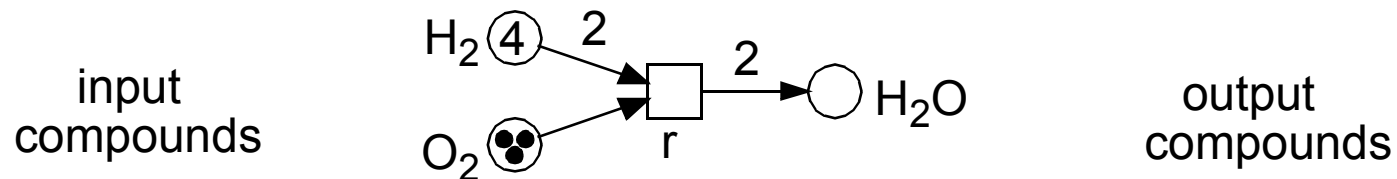
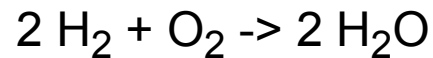
❑ local conditions -> Petri net places -> chemical compounds

❑ multiplicities -> Petri net arc weights -> stoichiometric relations

❑ condition's state -> token(s) in its place -> available amount (e.g. mol)

❑ system state -> marking -> compounds distribution

❑ atomic actions -> Petri net transitions -> chemical reactions



❑ local conditions -> Petri net places -> chemical compounds

❑ multiplicities -> Petri net arc weights -> stoichiometric relations

❑ condition's state -> token(s) in its place -> available amount (e.g. mol)

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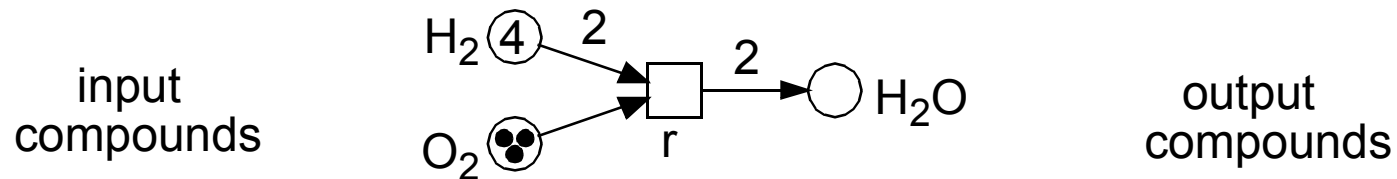
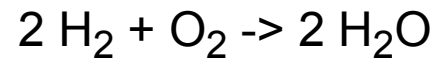
❑ $\text{PN} = (\text{P}, \text{T}, \text{F}, m_0)$, $\text{F}: (\text{P} \times \text{T}) \cup (\text{T} \times \text{P}) \rightarrow \mathbb{N}_0$, $m_0: \text{P} \rightarrow \mathbb{N}_0$

- ❑ **an action may happen, if** -> prerequisite
 - > *all preconditions are fulfilled*
(corresponding to the arc weights);

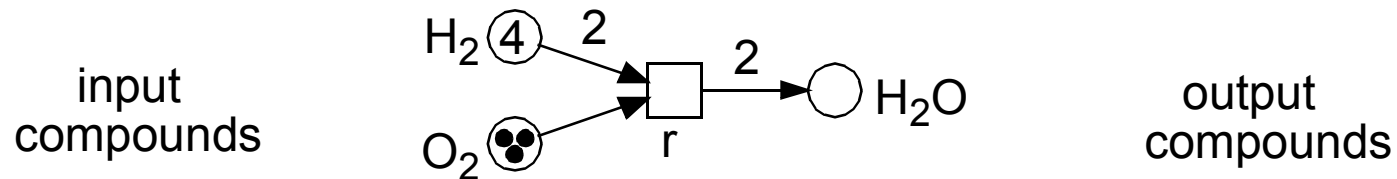
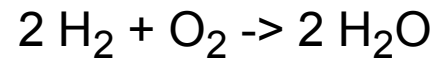
- ❑ **if an action happens, then** -> firing behaviour
 - > *tokens are removed from all preconditions*
(corresponding to the arc weights), and
 - > *tokens are added to all postconditions*
(corresponding to the arc weights);

- ❑ **action happens (firing of a transition)** -> model assumptions
 - > *atomic*
 - > *time-less*

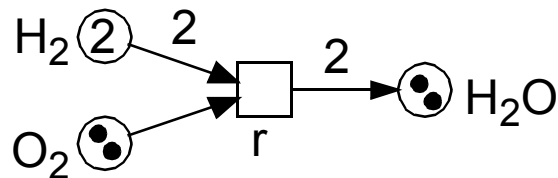
□ atomic actions -> Petri net transitions -> chemical reactions



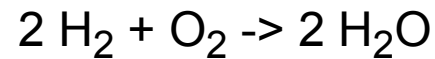
□ atomic actions -> Petri net transitions -> chemical reactions



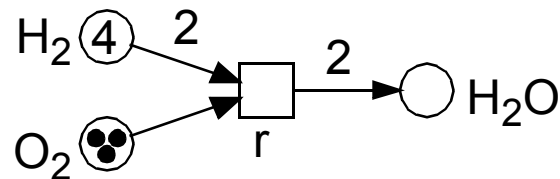
FIRING



□ atomic actions -> Petri net transitions -> chemical reactions

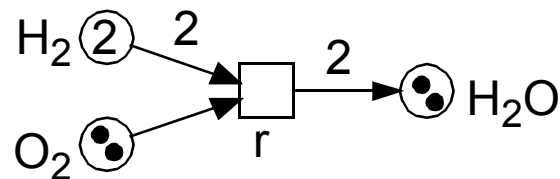


input
compounds



output
compounds

FIRING



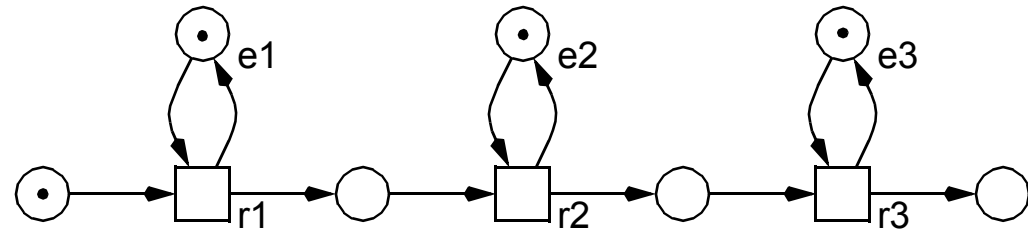
TOKEN GAME

DYNAMIC BEHAVIOUR
(substance/signal flow)

STATE SPACE

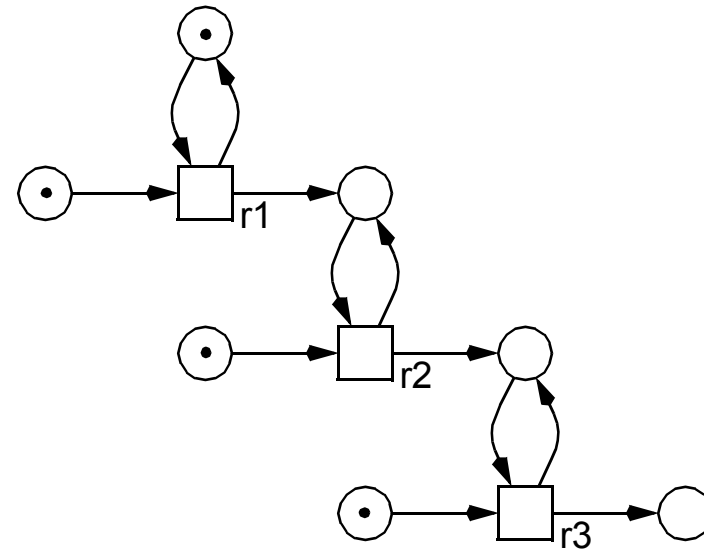
□ metabolic networks

-> *substance flows*



□ signal transduction networks

-> *signal flows*



❑ **metabolic networks**

signal transduction networks

gene regulatory networks

❑ **transitions**

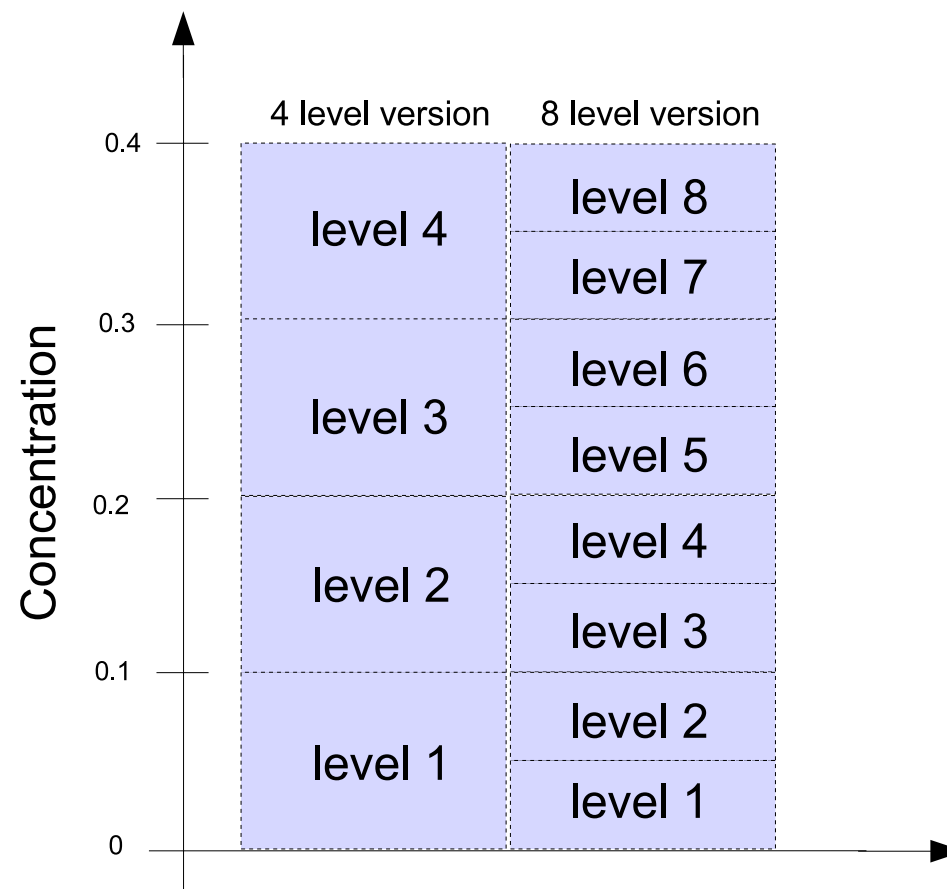
- > *(reversible, stoichiometric, enzyme-catalyzed) chemical reactions,*
- > *conversions/transport of metabolites, proteins, . . .*
- > *complexations/decomplexations, de-/phosphorylations, . . .*

❑ **places**

- > *(primary, secondary) chemical compounds,*
- > *(various states of) proteins, protein complex, genes, . . .*

❑ **tokens**

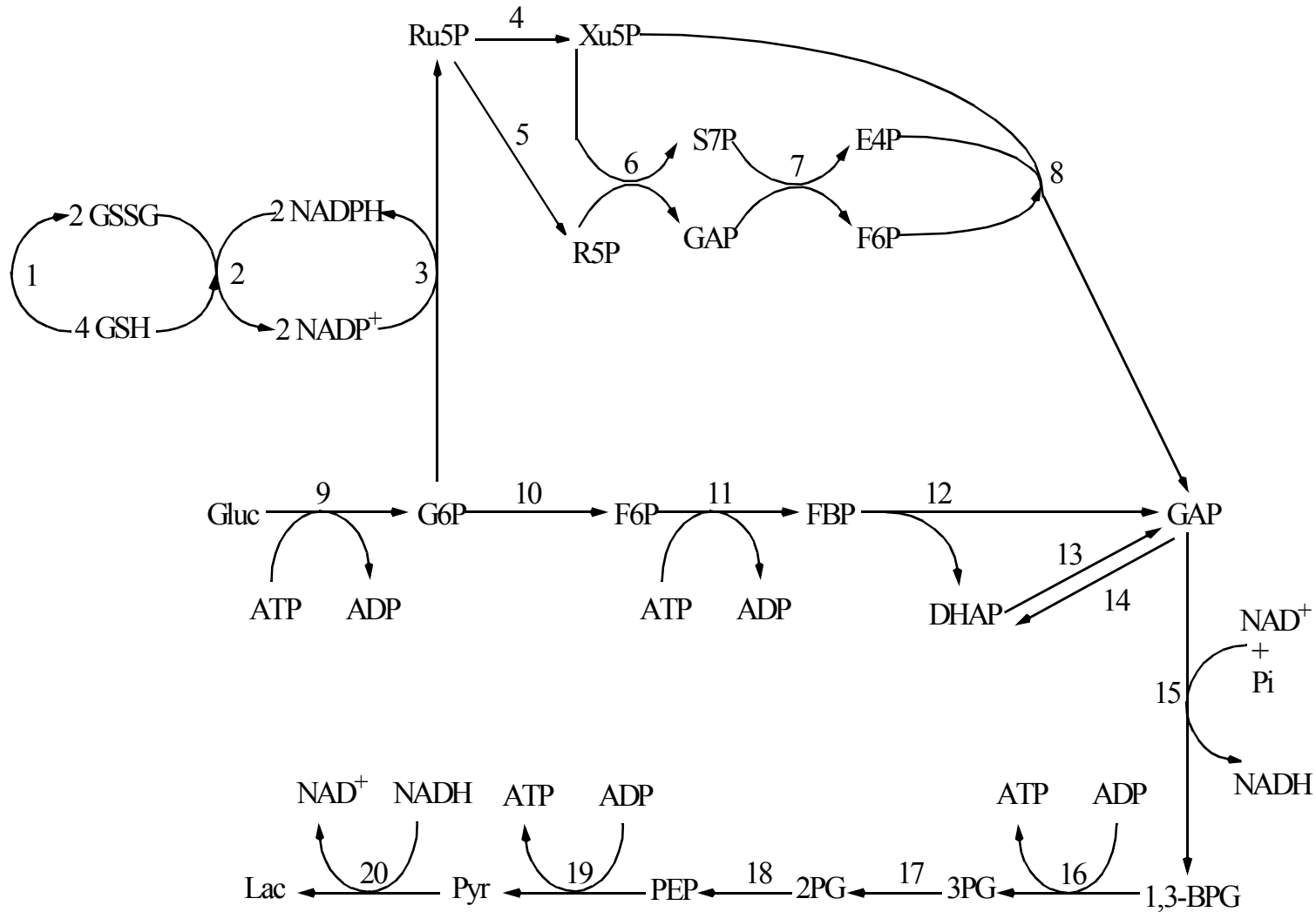
- > *molecules, moles, . . .*
- > *concentration levels, gene expression levels, . . .*
e.g., high/low = present/not present, or any finite integer number



BIO PETRI NETS - SOME EXAMPLES

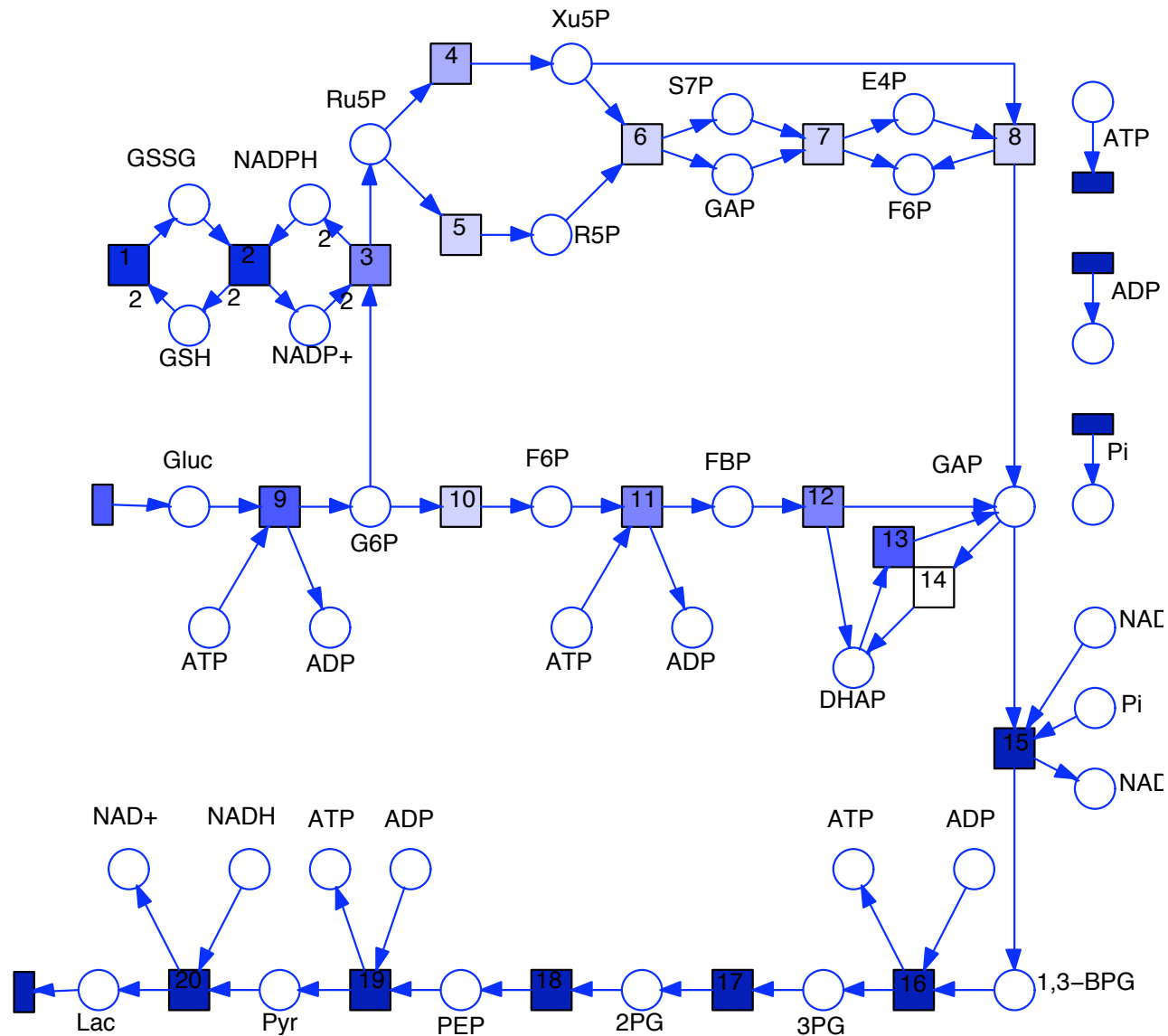
Ex1 - Glycolysis and Pentose Phosphate Pathway

[Reddy 1993]

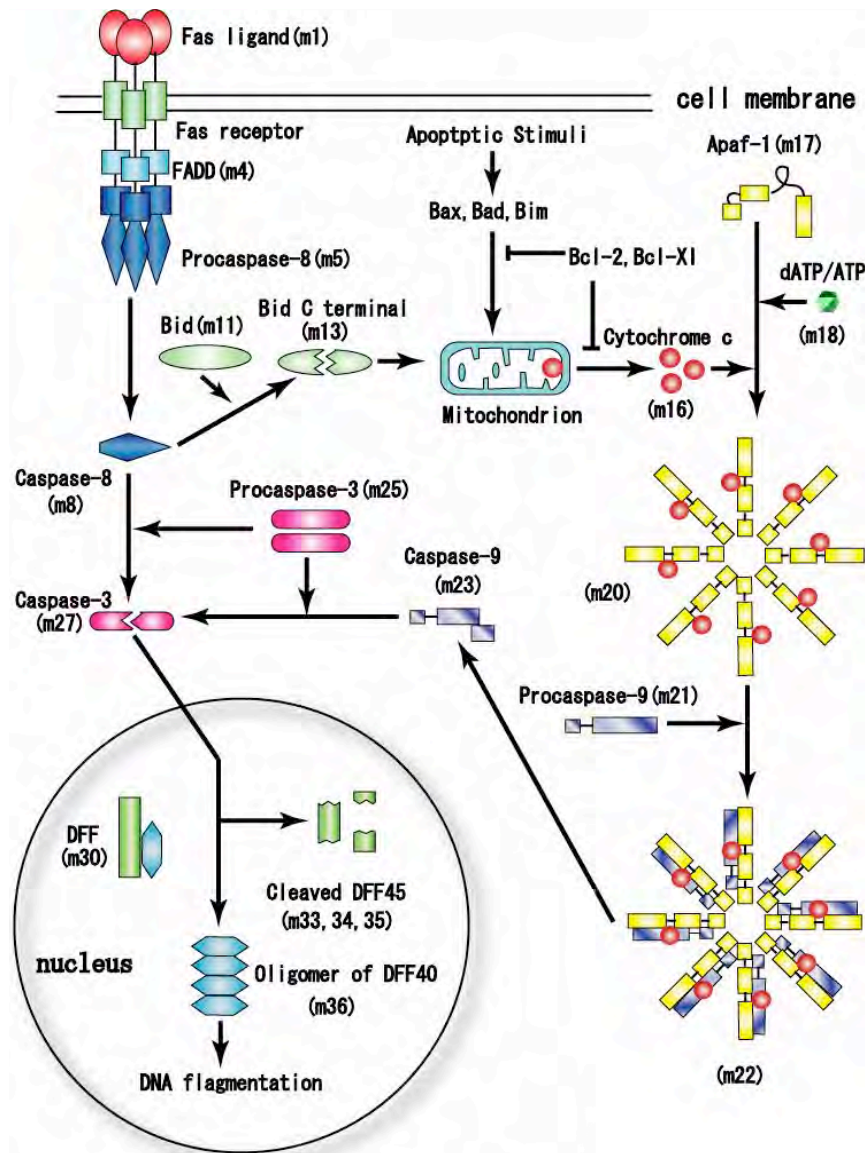


Ex1 - Glycolysis and Pentose Phosphate Pathway

[Reddy 1993]
[Heiner 1998]

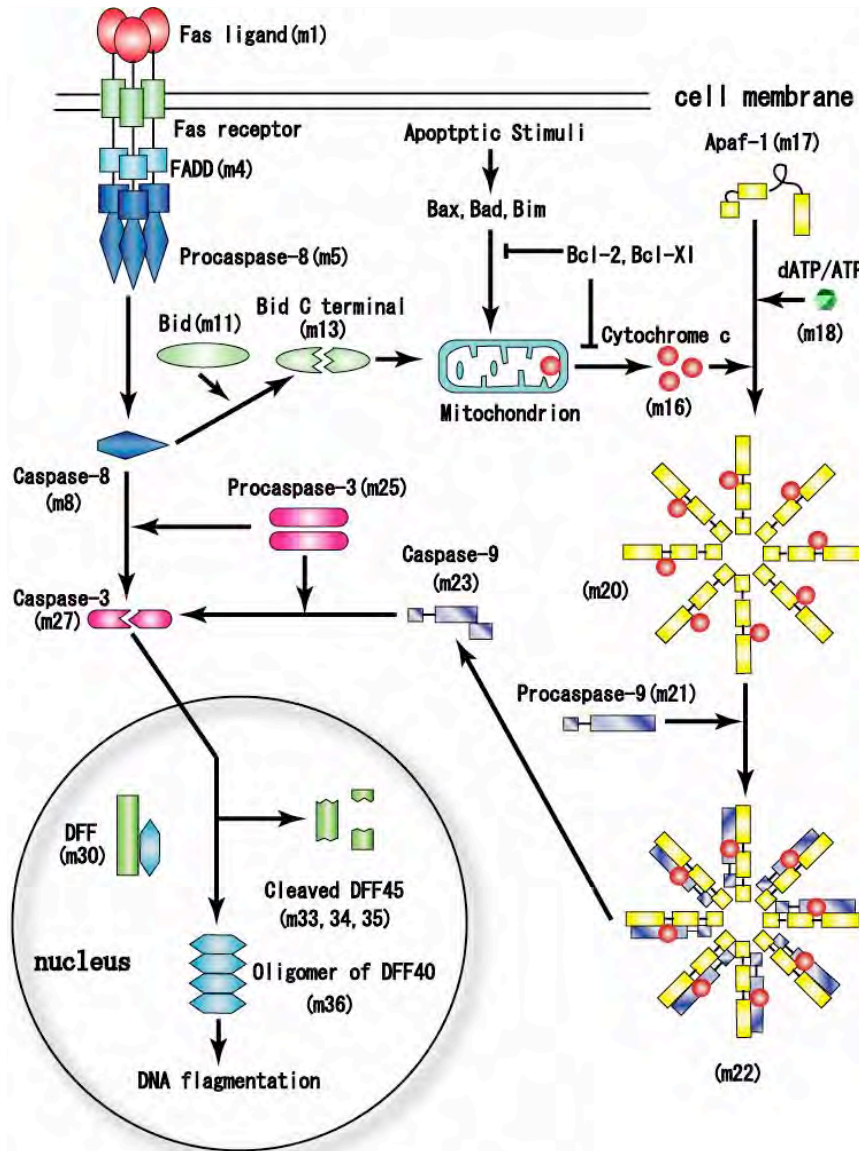


Ex2: APOPTOSIS IN MAMMALIAN CELLS

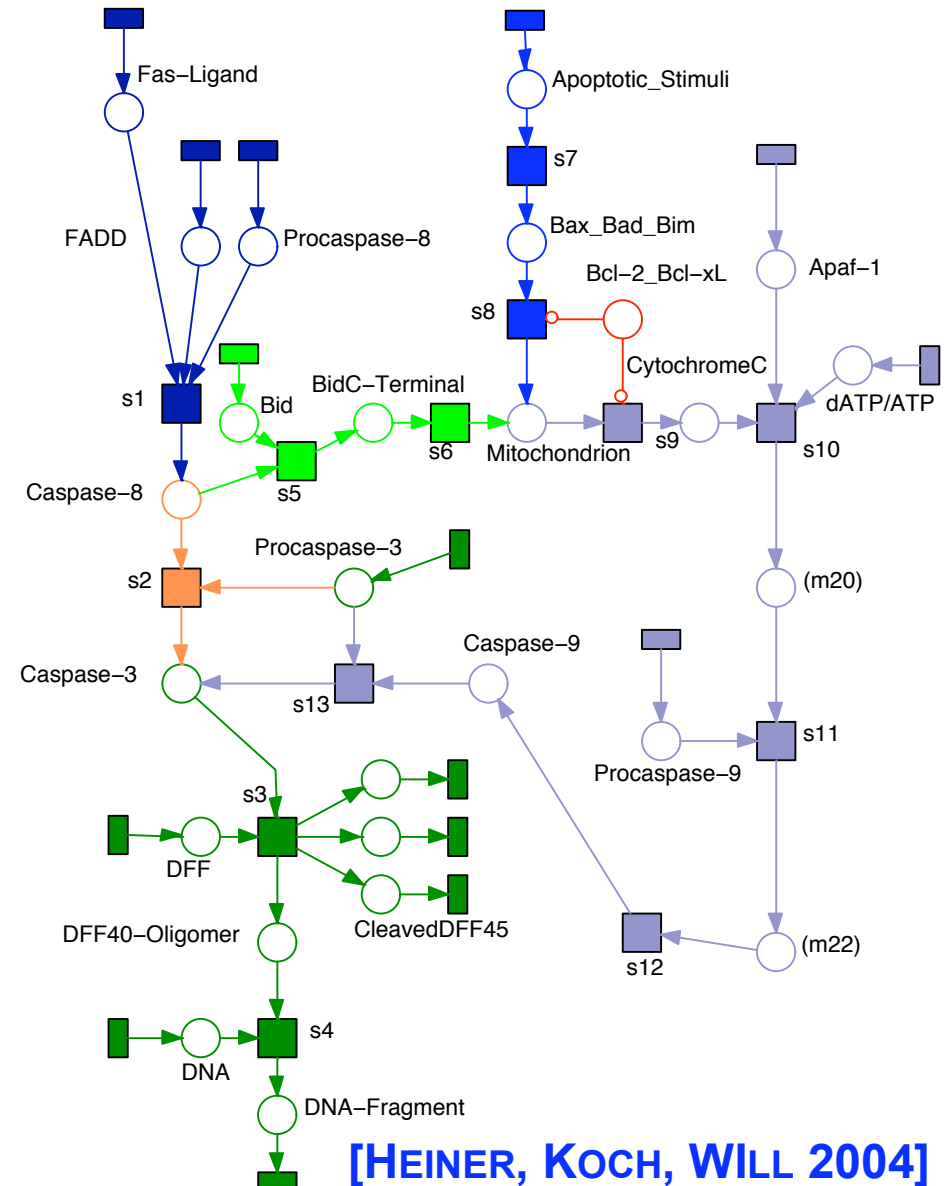


[GON 2003]

Ex2: APOPTOSIS IN MAMMALIAN CELLS



[GON 2003]



[HEINER, KOCH, WILL 2004]

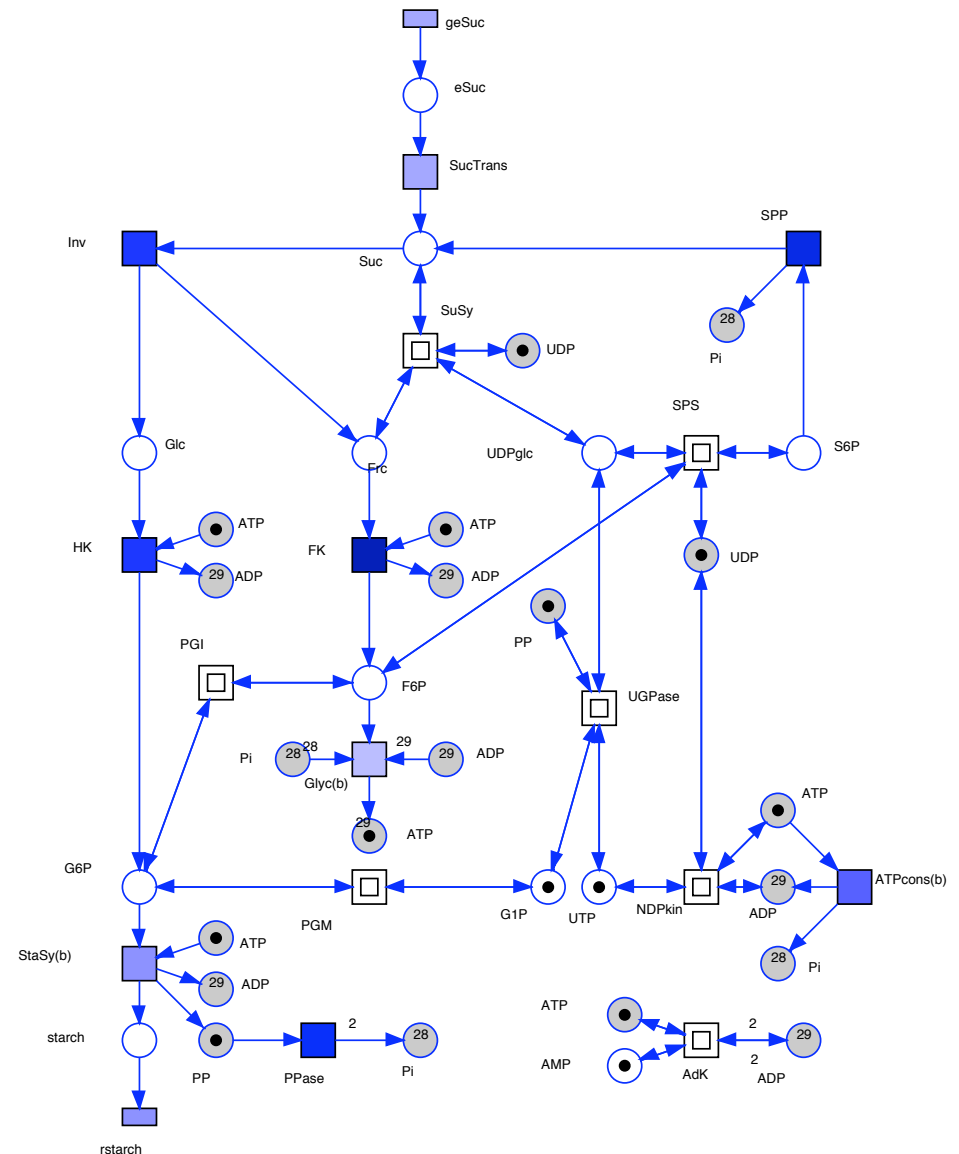
Ex3 - Carbon Metabolism in Potato Tuber

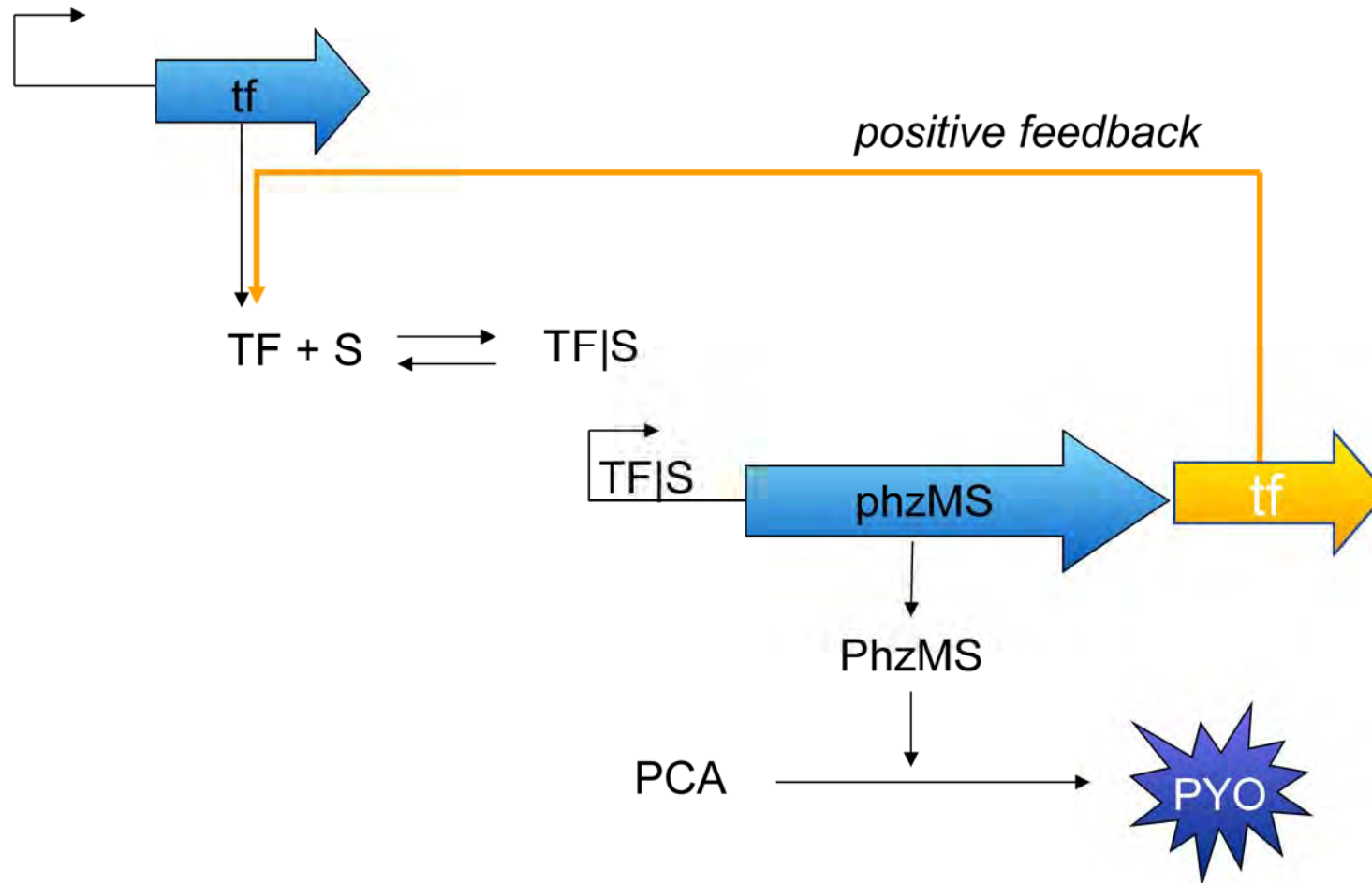
PN & Systems Biology



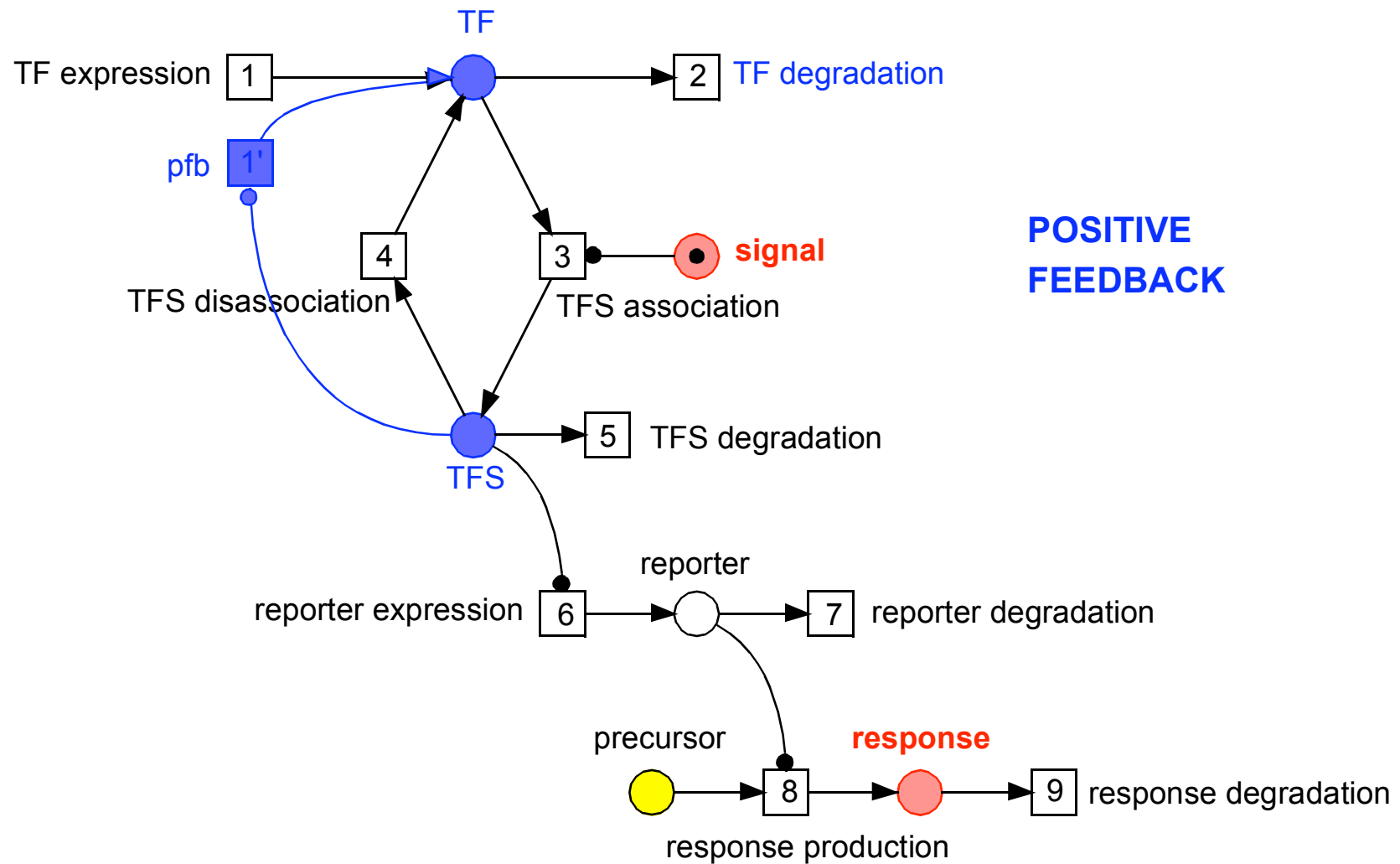
[KOCH, JUNKER, HEINER 2005]

PN & Systems Biology



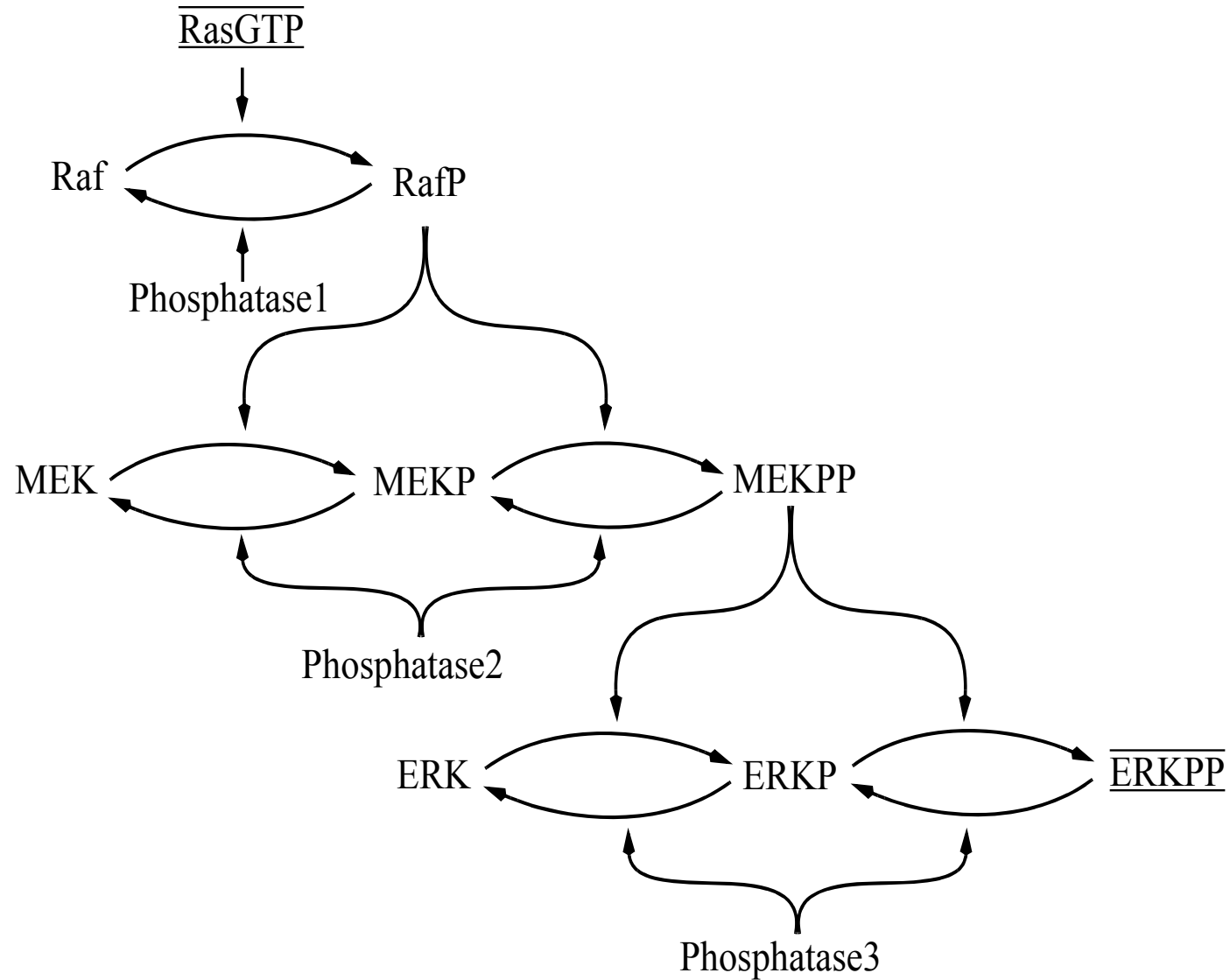


[GILBERT, HEINER, ROSSER, FULTON, GU, TRYBILO 2008]

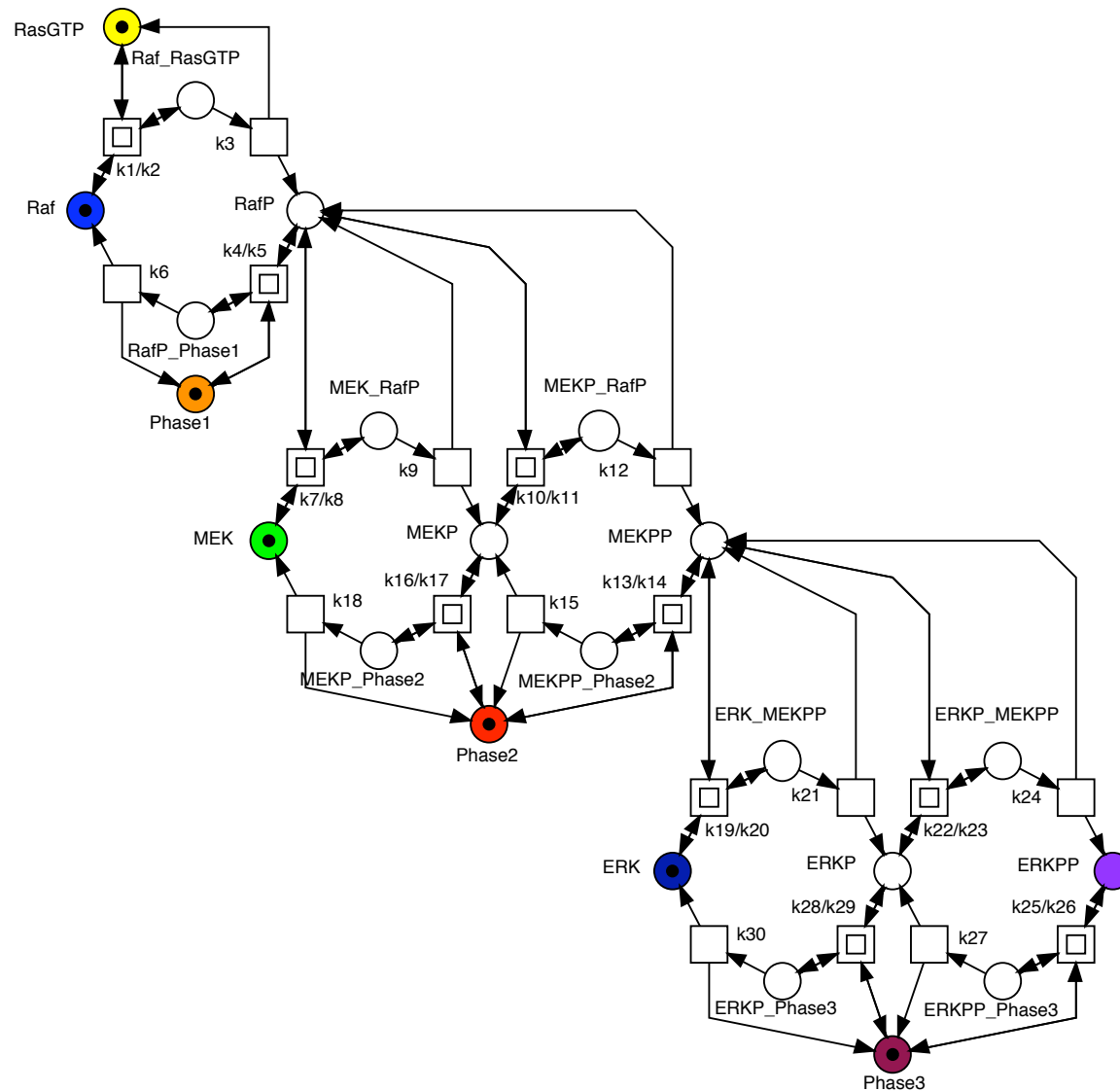


[GILBERT, HEINER, ROSSER, FULTON, GU, TRYBILO 2008]

EX5 - SIGNALLING CASCADE



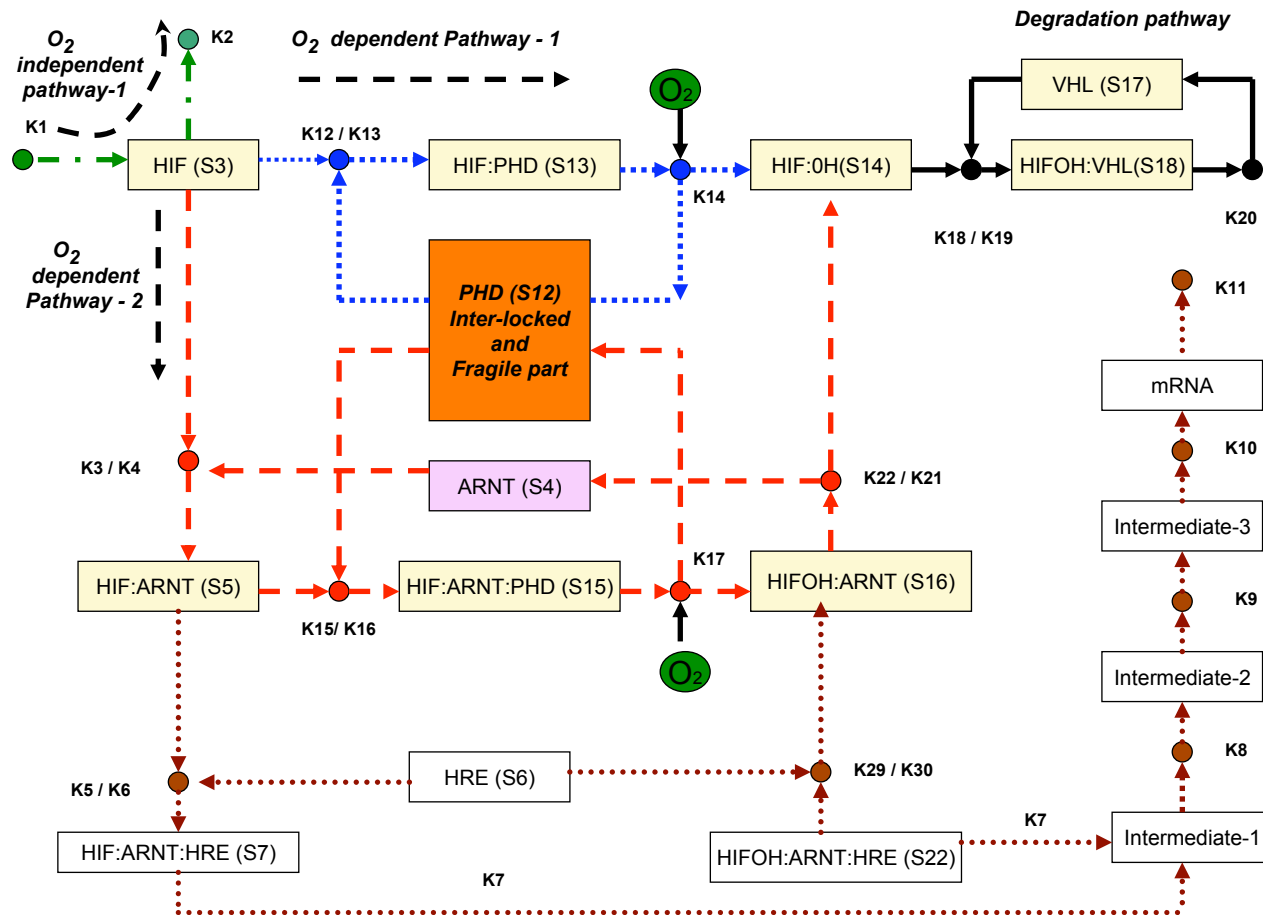
EX5 - SIGNALLING CASCADE



[GILBERT,
HEINER,
LEHRACK 2007]

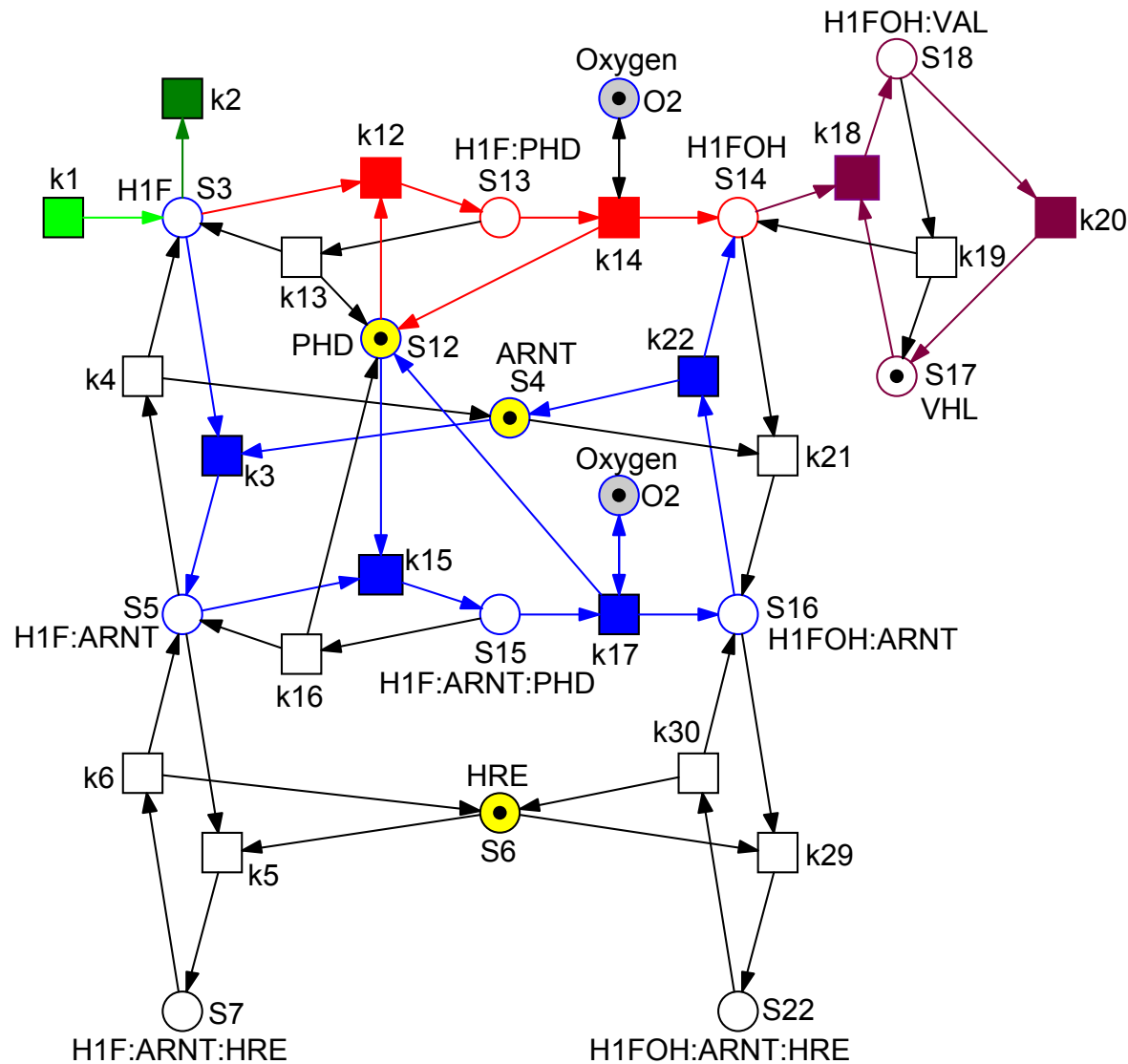
[HEINER,
GILBERT,
DONALDSON 2008]

Ex6 - HYPOXIA



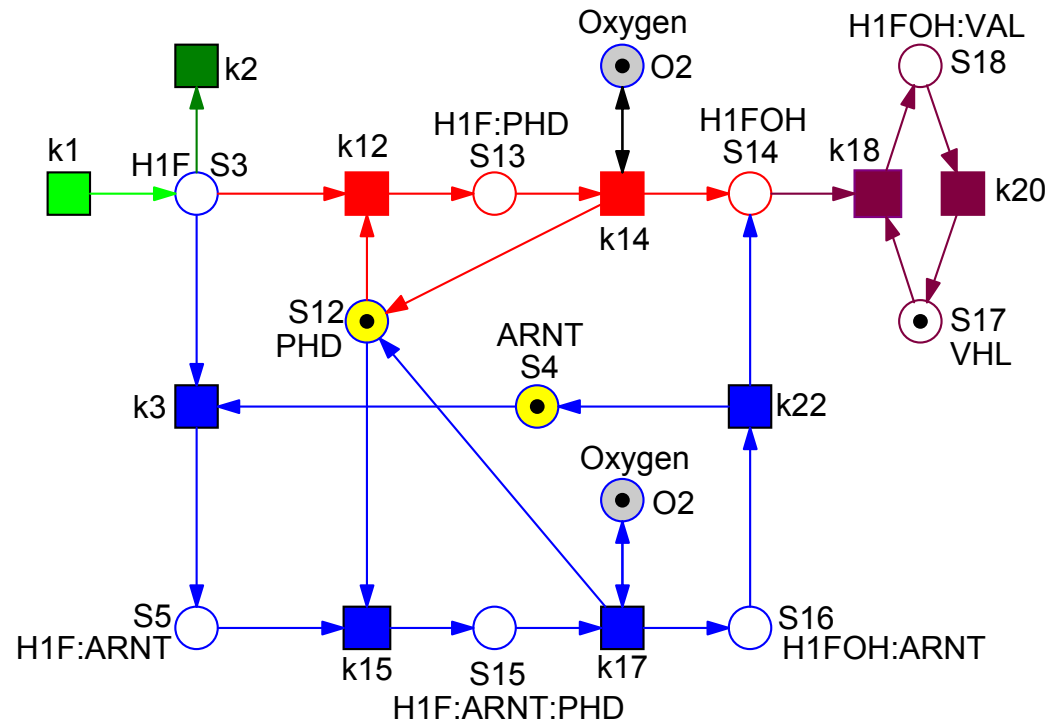
[YU ET AL. 2007]

Ex6 - HYPOXIA

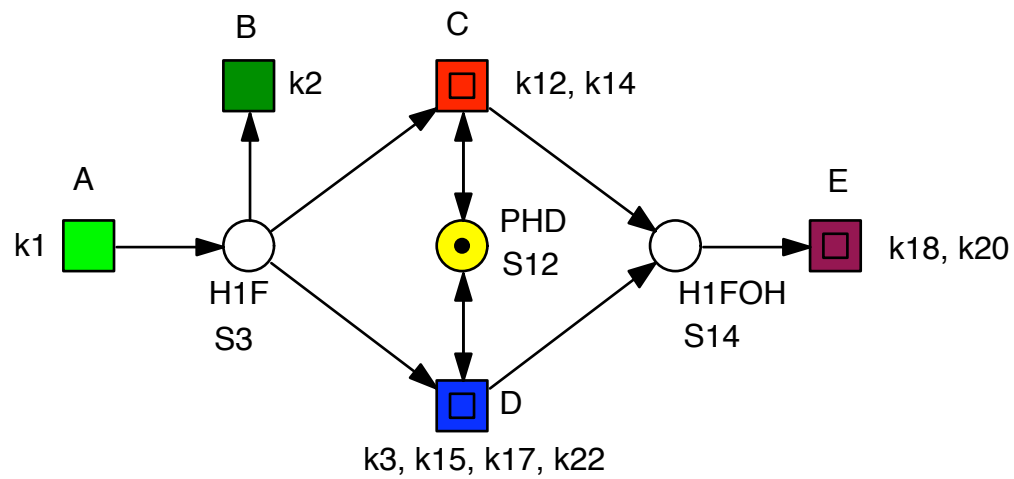


[HEINER,
SRIRAM 2010]

Ex6 - HYPOXIA

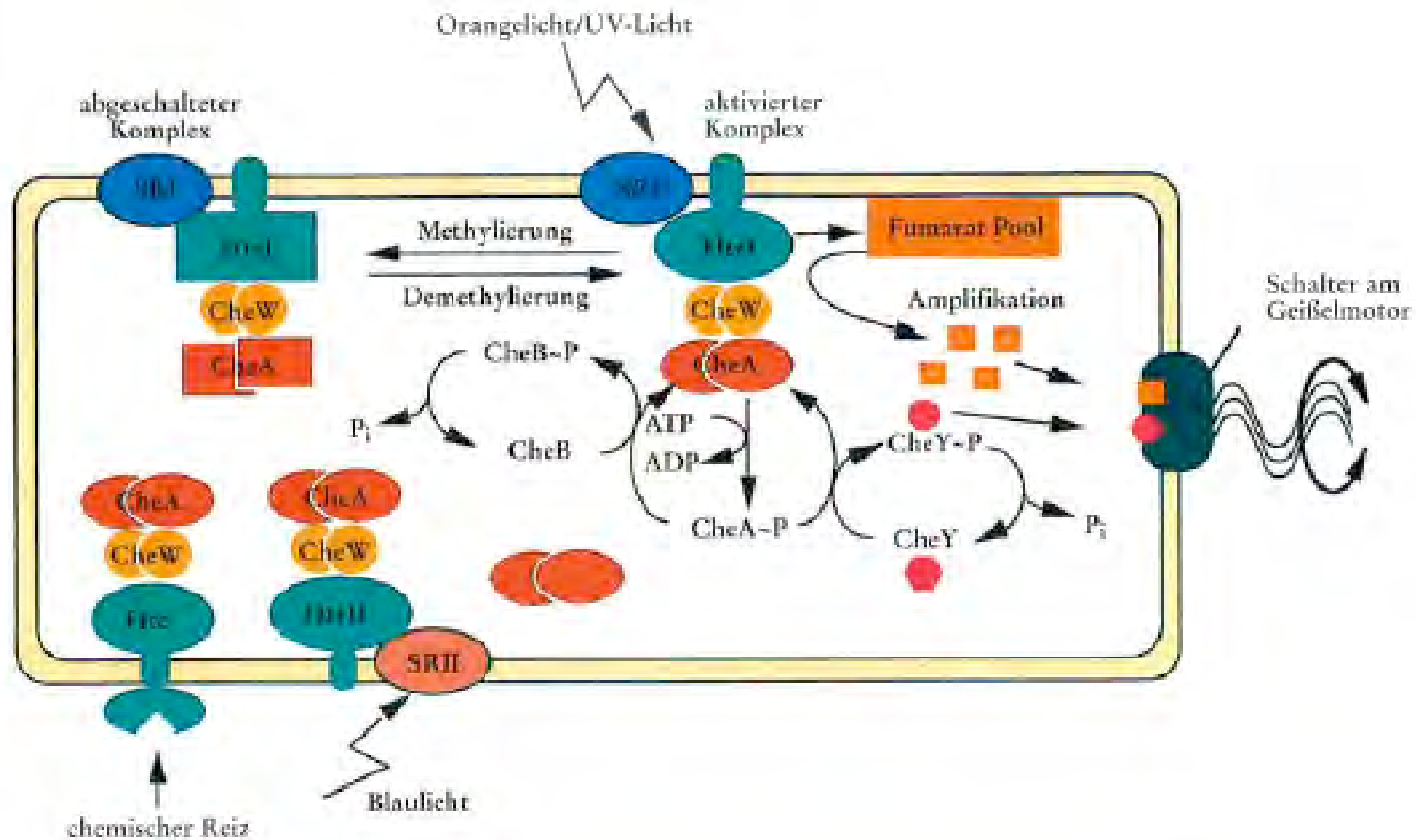


[HEINER,
SRIRAM 2010]



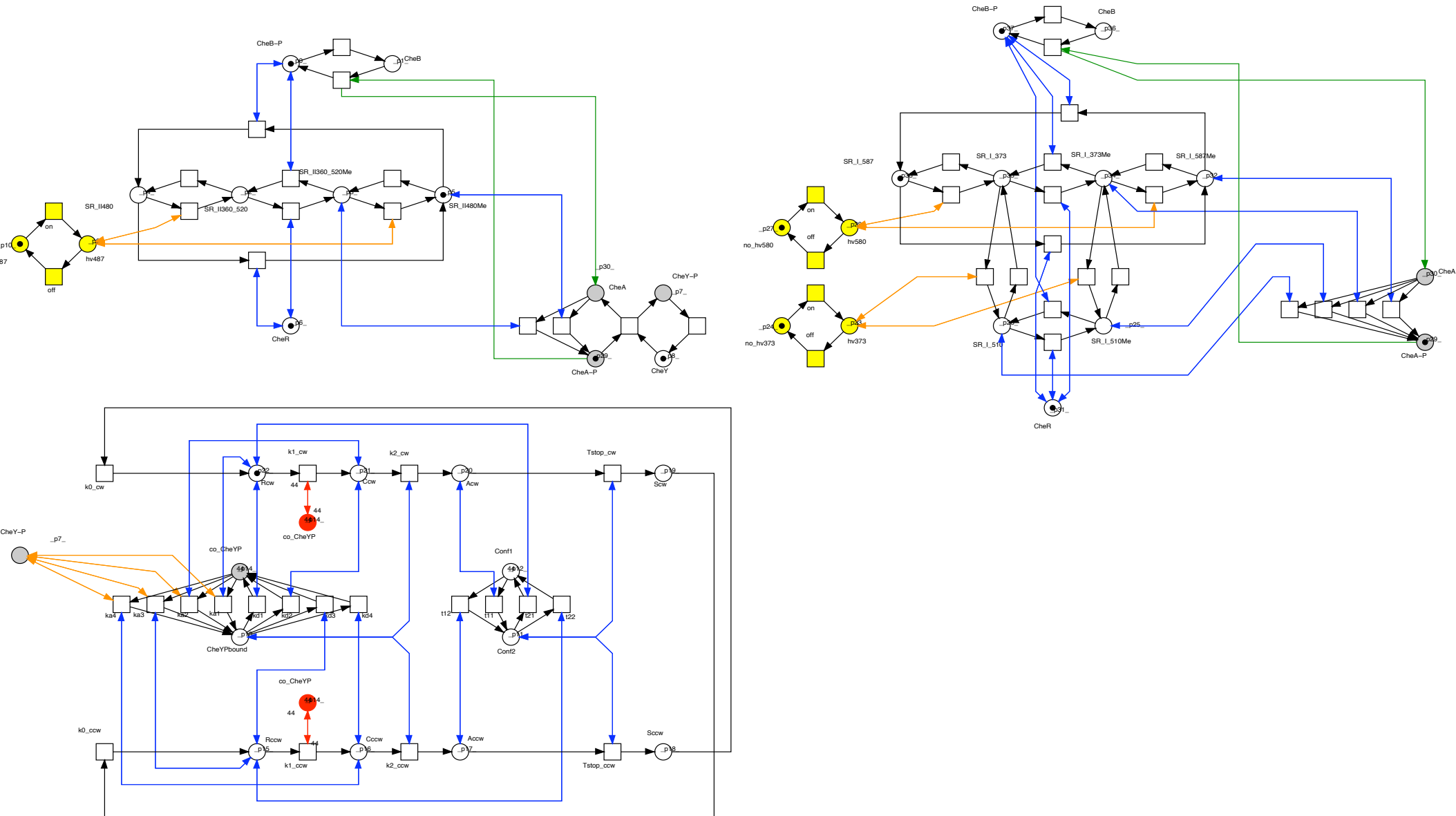
[HEINER,
SRIRAM 2010]

EX7 - SWITCH CYCLE HALOBACTERIUM SALINARUM



[MARWAN, OESTERHELT 1999]

Ex7 - SWITCH CYCLE HALOBACTERIUM SALINARUM



QUALITATIVE ANALYSES

❑ How many tokens can reside at most in a given place ?

-> $(0, 1, k, \infty)$

-> **BOUNDEDNESS**

❑ How many tokens can reside at most in a given place ?

-> (0, 1, *k*, oo)

-> *BOUNDEDNESS*

❑ How often can a transition fire ?

-> (0-times, n-times, *oo-times*)

-> *LIVENESS*

❑ **How many tokens can reside at most in a given place ?**

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❑ **How often can a system state be reached ?**

-> *never*

-> *UNREACHABLE* -> *SAFETY PROPERTIES*

-> *n-times*

-> *REPRODUCIBLE*

-> *oo-times*

-> *REVERSIBILITY*

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❑ **Are there behaviourally invariant net structures ?**

-> *token conservation*

-> *P - INVARIANTS*

-> *token distribution reproduction*

-> *T - INVARIANTS*

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❑ **... and many more -> temporal logics** -> *CTL / LTL - CSL / PLTL*

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❑ ... and many more -> temporal logics

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GENERAL
BEHAVIOURAL
PROPERTIES

SPECIAL
BEHAVIOURAL
PROPERTIES

❑ **static analyses**

-> **no state space construction**

❑ **dynamic analyses**

-> **total/ partial state space construction**

- ❑ **static analyses** **-> no state space construction**
 - > *structural properties (graph theory, combinatorics), e.g. DTP*
 - > *P / T - invariants (linear algebra)*

- ❑ **dynamic analyses** **-> total/ partial state space construction**

- ❑ **static analyses** -> no state space construction
 - > *structural properties (graph theory)*
 - > *P / T - invariants (linear algebra)*

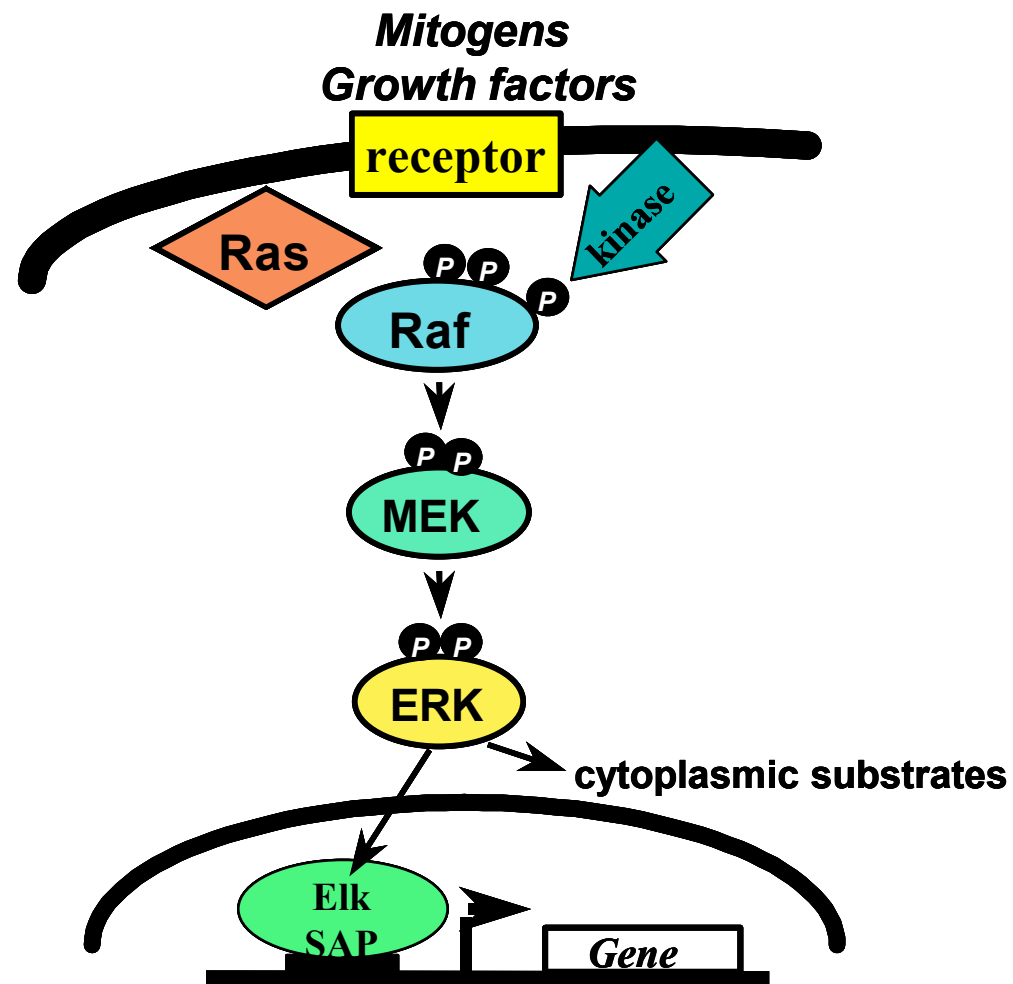
- ❑ **dynamic analyses** -> total/ partial state space construction
 - > analysis of **general** behavioural system properties,
e.g. boundedness, liveness, reversibility, . . .

 - > model checking of **special** behavioural system properties,
e.g. reachability of a given (sub-) system state (with constraints),
reproducibility of a given (sub-) system state (with constraints)

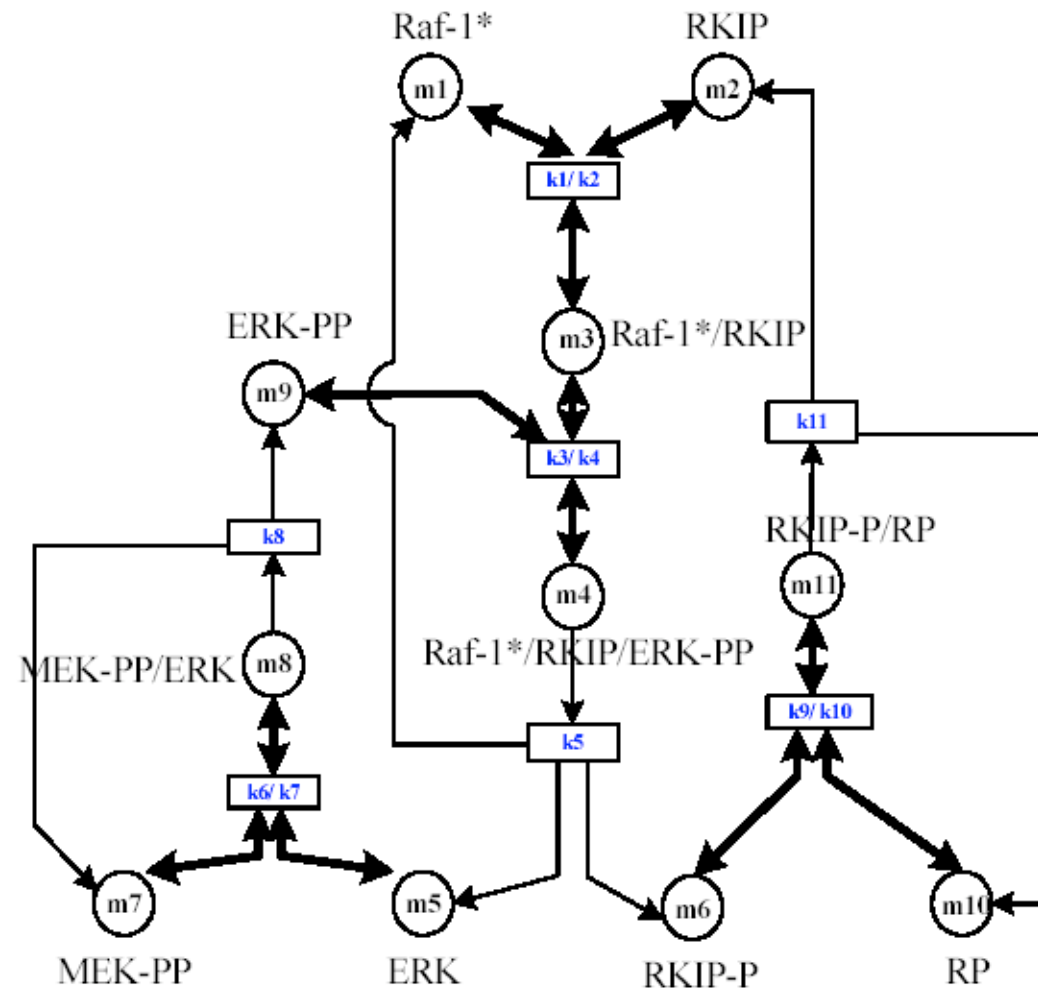
 - expressed in temporal logics (CTL / LTL),
-> **very flexible, powerful query language**

A CASE STUDY

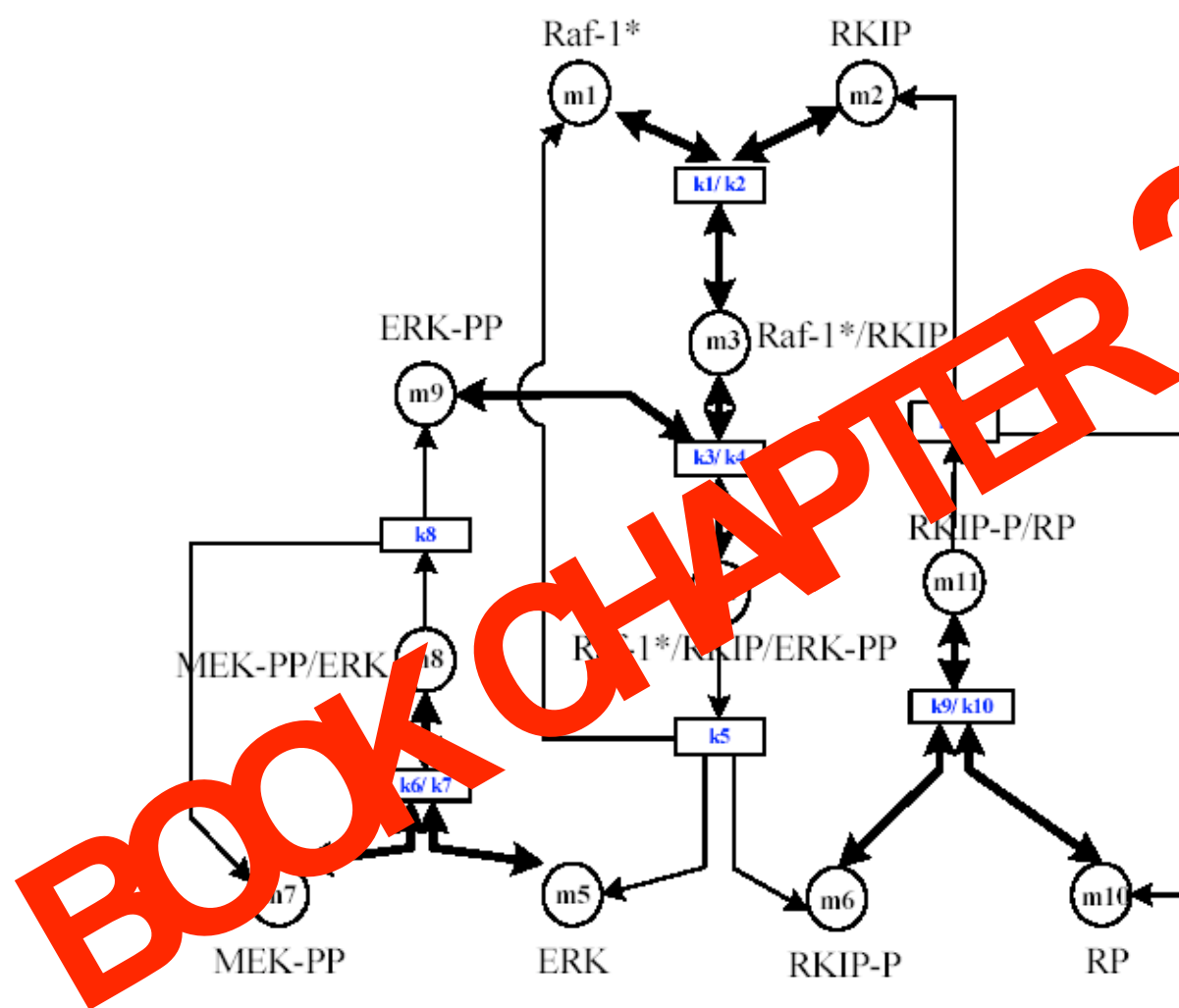
...one pathway...



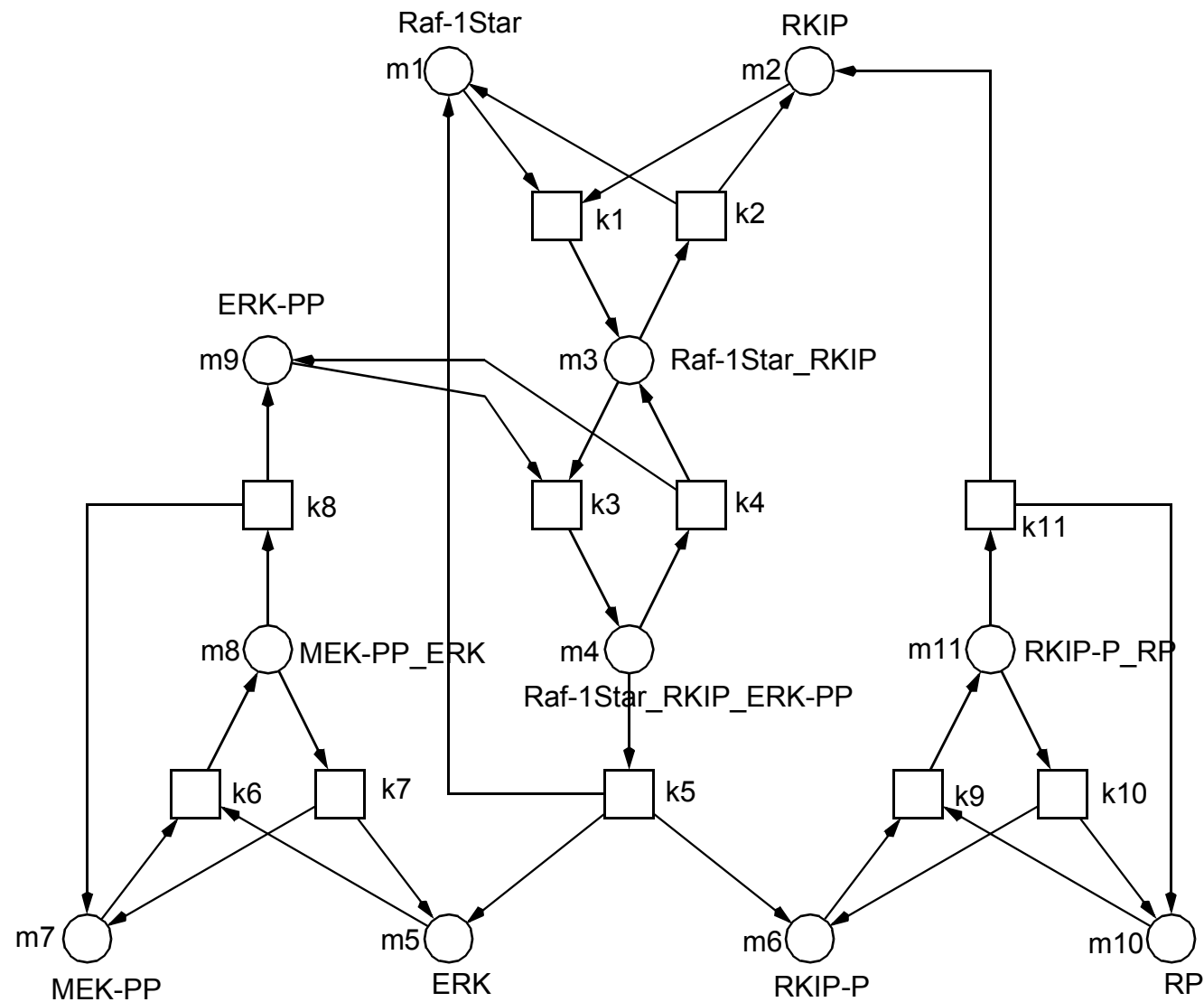
THE RKIP PATHWAY



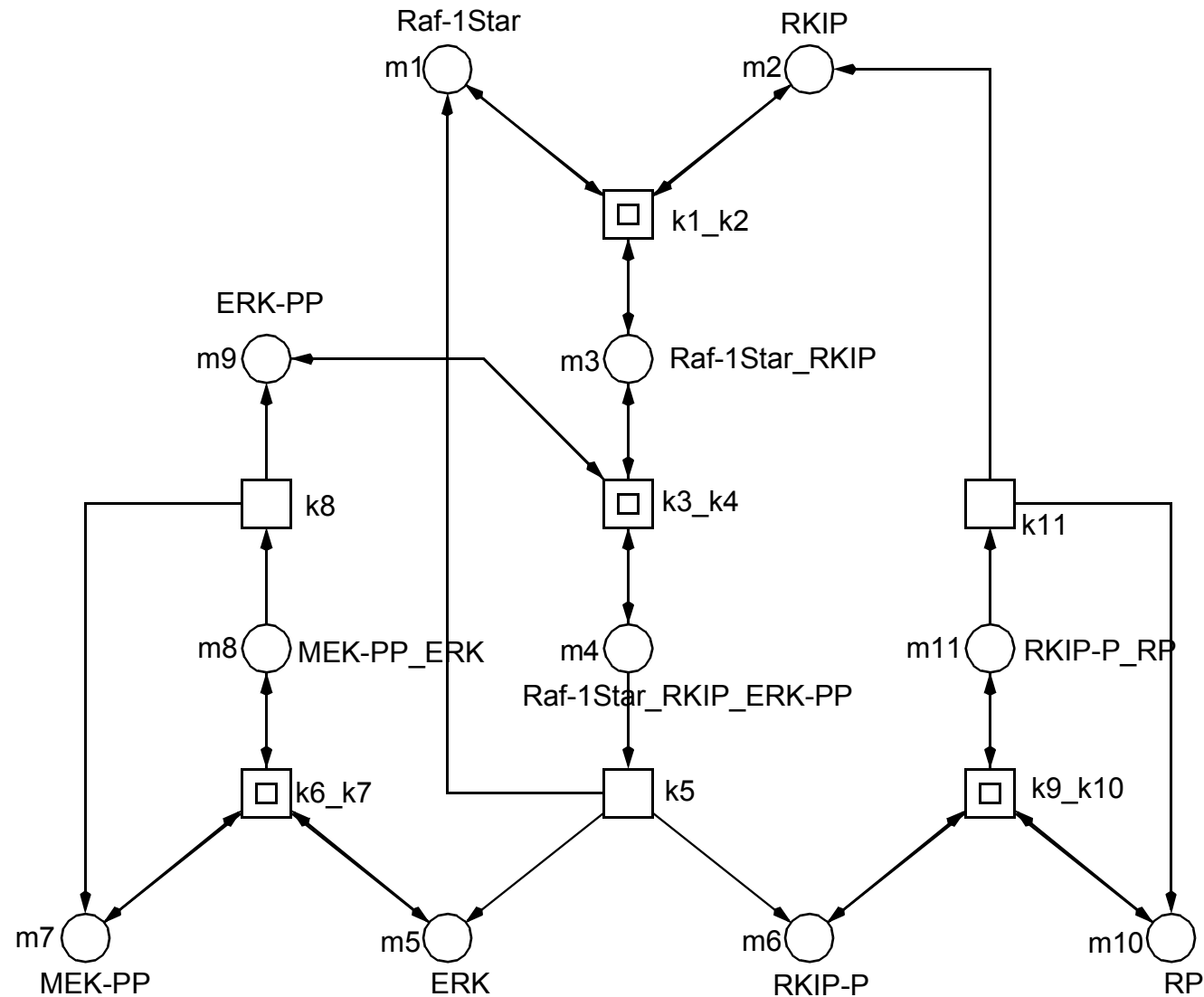
**[Cho et al.,
CMSB 2003]**



[Cho et al.,
CMSB 2003]

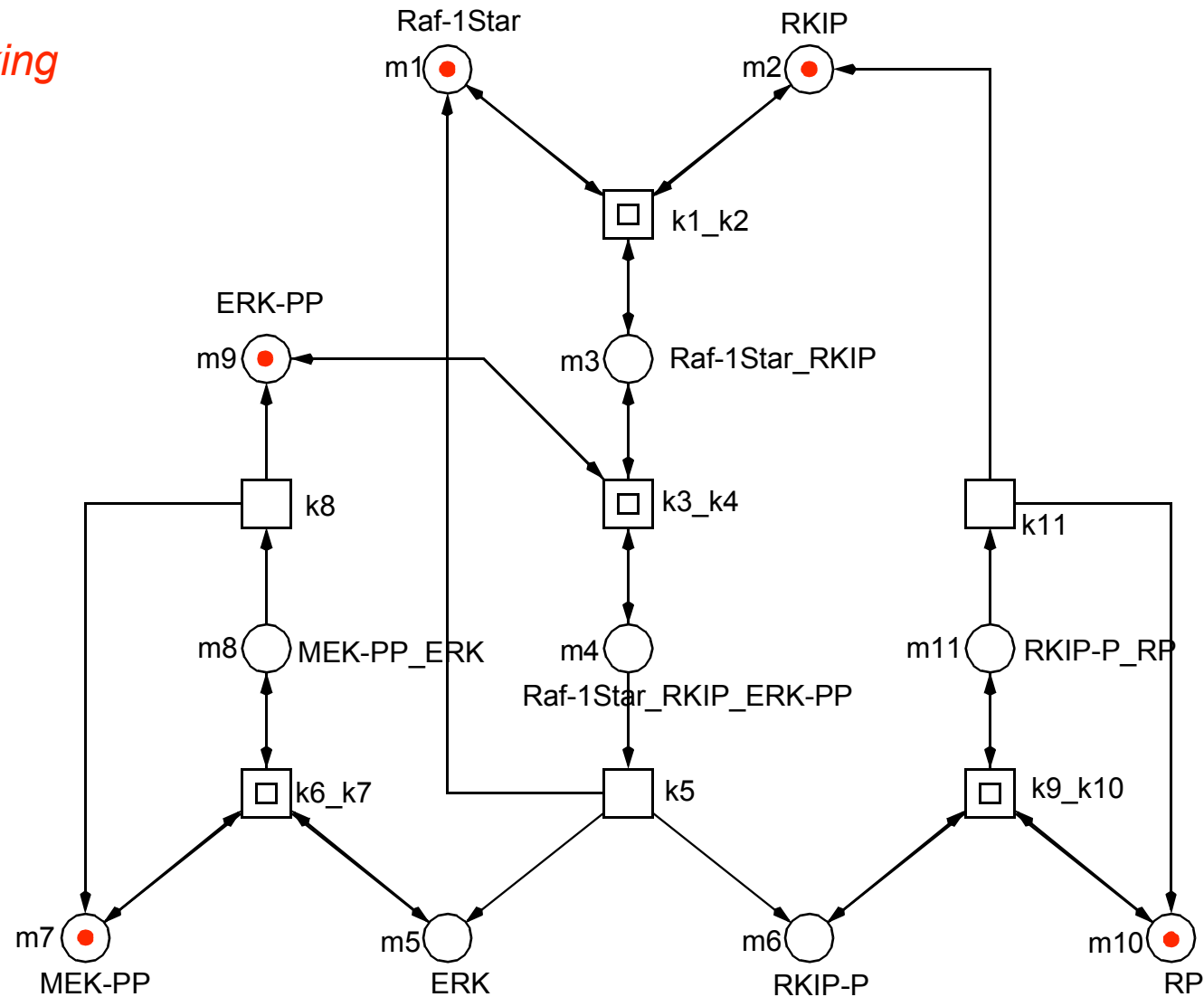


THE RKIP PATHWAY, HIERARCHICAL PETRI NET



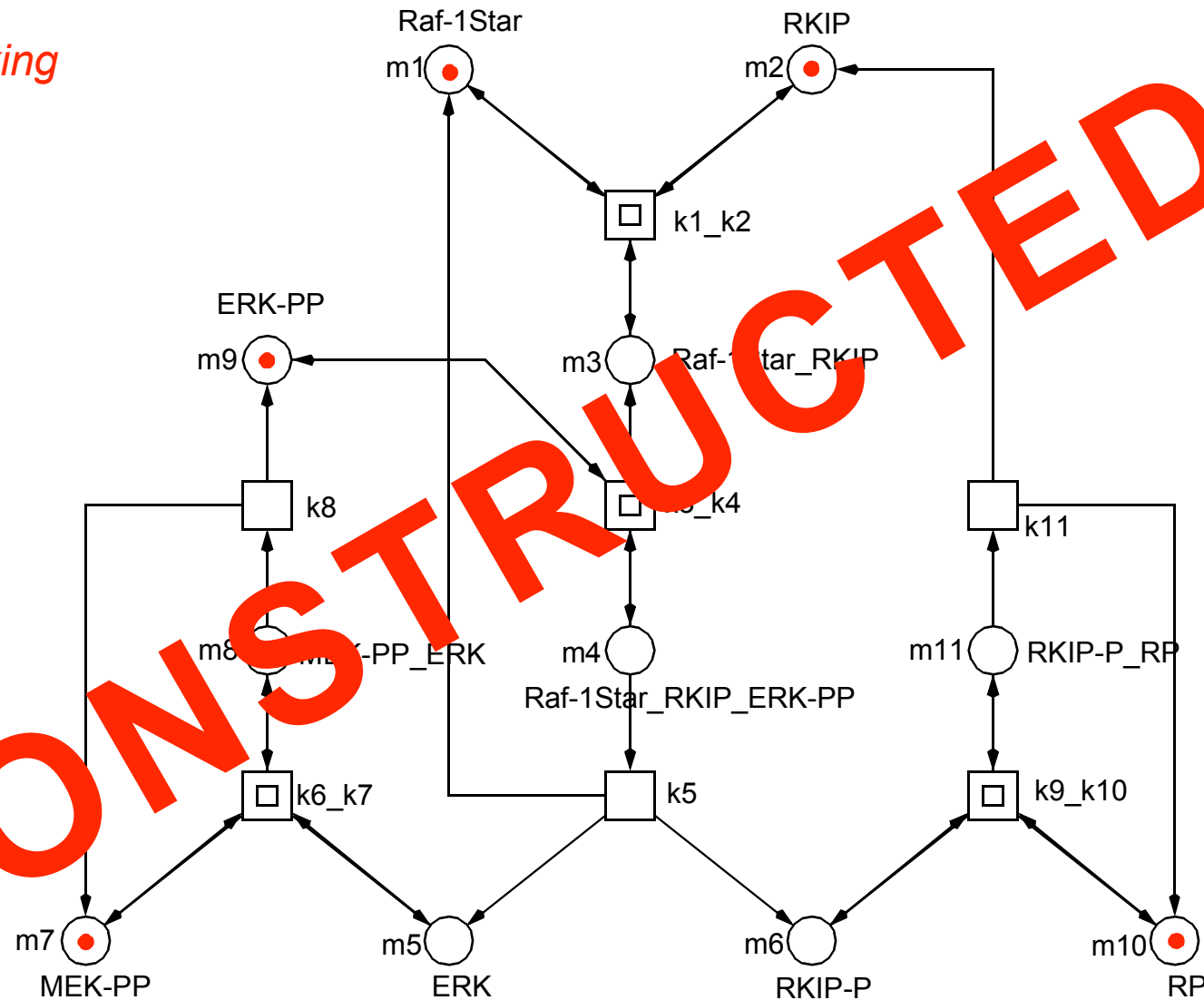
THE RKIP PATHWAY, HIERARCHICAL PETRI NET

initial marking

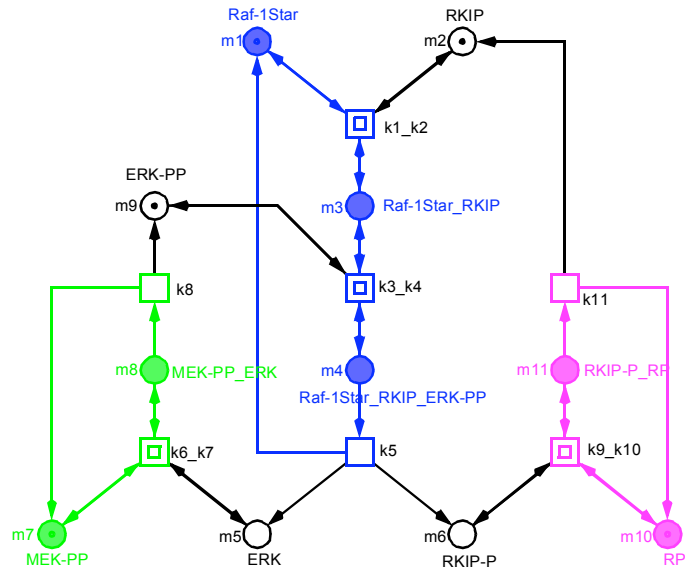


THE RKIP PATHWAY, HIERARCHICAL PETRI NET

initial marking



THE RKIP PATHWAY, P-INVARIANTS



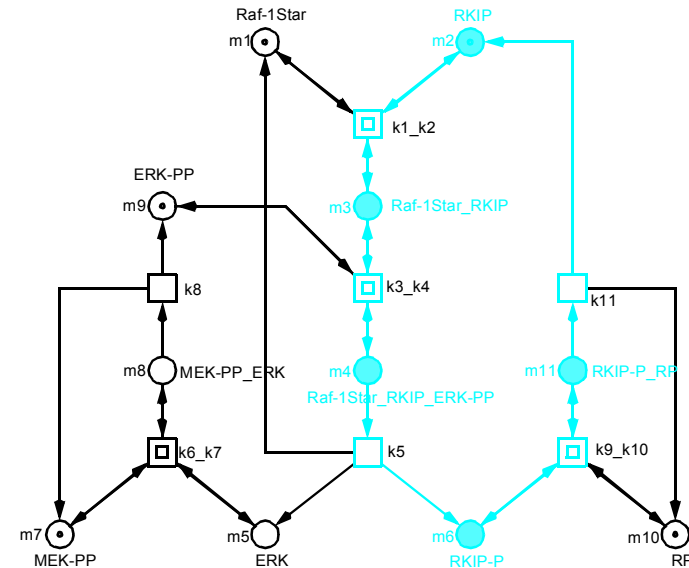
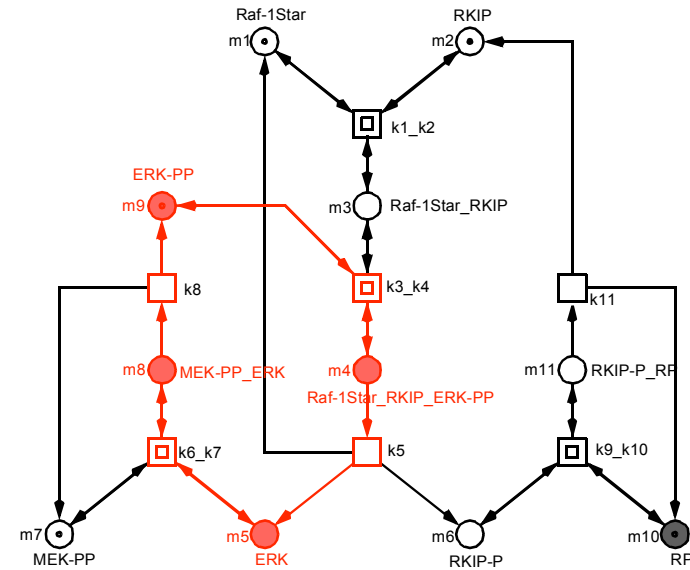
P-INV1: MEK

P-INV2: RAF-1STAR

P-INV3: RP

P-INV4: ERK

P-INV5: RKIP

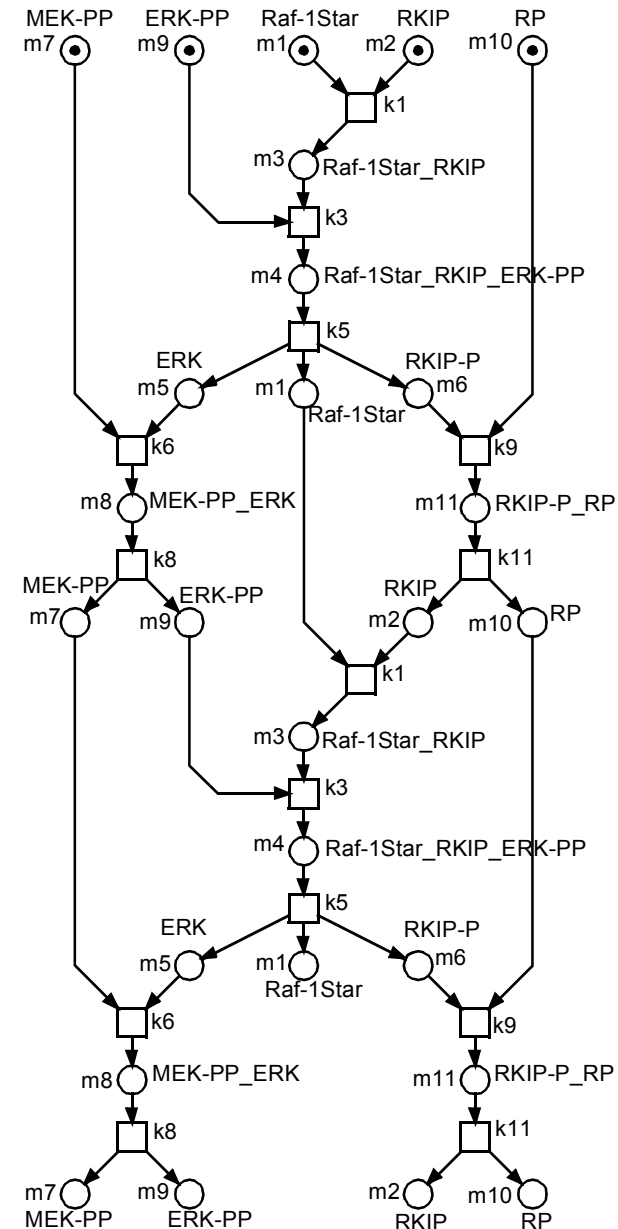


- ❑ **each P-invariant gets at least one token**
 - > *P-invariants are structural deadlocks and traps*
- ❑ **in signal transduction**
 - > *exactly 1 token, corresponding to species conservation*
 - > *token in least active state*
- ❑ **all (non-trivial) T-invariants get realizable**
 - > *to make the net live*
- ❑ **minimal marking**
 - > *minimization of the state space*

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-> UNIQUE INITIAL MARKING <-

- ❑ realizability check under the constructed marking
- ❑ T-invariant's unfolding to describe its behaviour
 - > *partial order structure*
- ❑ labelled condition / event net
 - > *events (boxes)*
 - *transition occurrences*
 - > *conditions (circles)*
 - *involved compounds*
- ❑ occurrence net
 - > *acyclic*
 - > *no backward branching conditions*
 - > *infinite*



❑ property 1

Is a given (sub-) marking (system state) reachable ?

$EF (ERK * RP);$

❑ property 2

Liveness of transition k8 ?

$AG EF (MEK-PP_ERK);$

❑ property 3

Is it possible to produce ERK-PP neither creating nor using MEK-PP ?

$E (! MEK-PP \ U ERK-PP);$

❑ property 4

Is there cyclic behaviour w.r.t. the presence / absence of RKIP ?

$EG ((RKIP \rightarrow EF (! RKIP)) * (! RKIP \rightarrow EF (RKIP)));$

-> static analysis

- ## ❑ CPI & CTI

- reachability graph

-> **dynamic analysis**

- **model checking**

-> requires professional understanding

- monika.heiner@informatik.tu-cottbus.de

- ❑ **structural decisions of behavioural properties** -> **static analysis**
 - > *CPI* -> *BND*
 - > *ES & DTP* -> *LIVE*

- ❑ **CPI & CTI**
 - > *all minimal T-invariant / P-invariants enjoy biological interpretation*
 - > *non-trivial T-invariant -> partial order description of the essential behaviour*

- ❑ **reachability graph** -> **dynamic analysis**
 - > *finite* -> *BND*
 - > *the only SCC contains all transitions* -> *LIVE*
 - > *one Strongly Connected Component (SCC)* -> *REV*

- ❑ **model checking** -> **requires professional understanding**
 - > *all expected properties are valid*

-> VALIDATED QUALITATIVE MODEL

❑ validation criterion 1

- > *all expected structural properties hold*
- > *all expected general behavioural properties hold*

❑ validation criterion 2

- > *CTI*
- > *no minimal T-invariant without biological interpretation*
- > *no known biological behaviour without corresponding T-invariant*

❑ validation criterion 3

- > *CPI*
- > *no minimal P-invariant without biological interpretation (?)*

❑ validation criterion 4

- > *all expected special behavioural properties hold*
- > *temporal-logic properties -> TRUE*

**NOW WE ARE READY
FOR SOPHISTICATED
QUANTITATIVE ANALYSES !**

STOCHASTIC PETRI NETS - SPN (*xSPN*) -

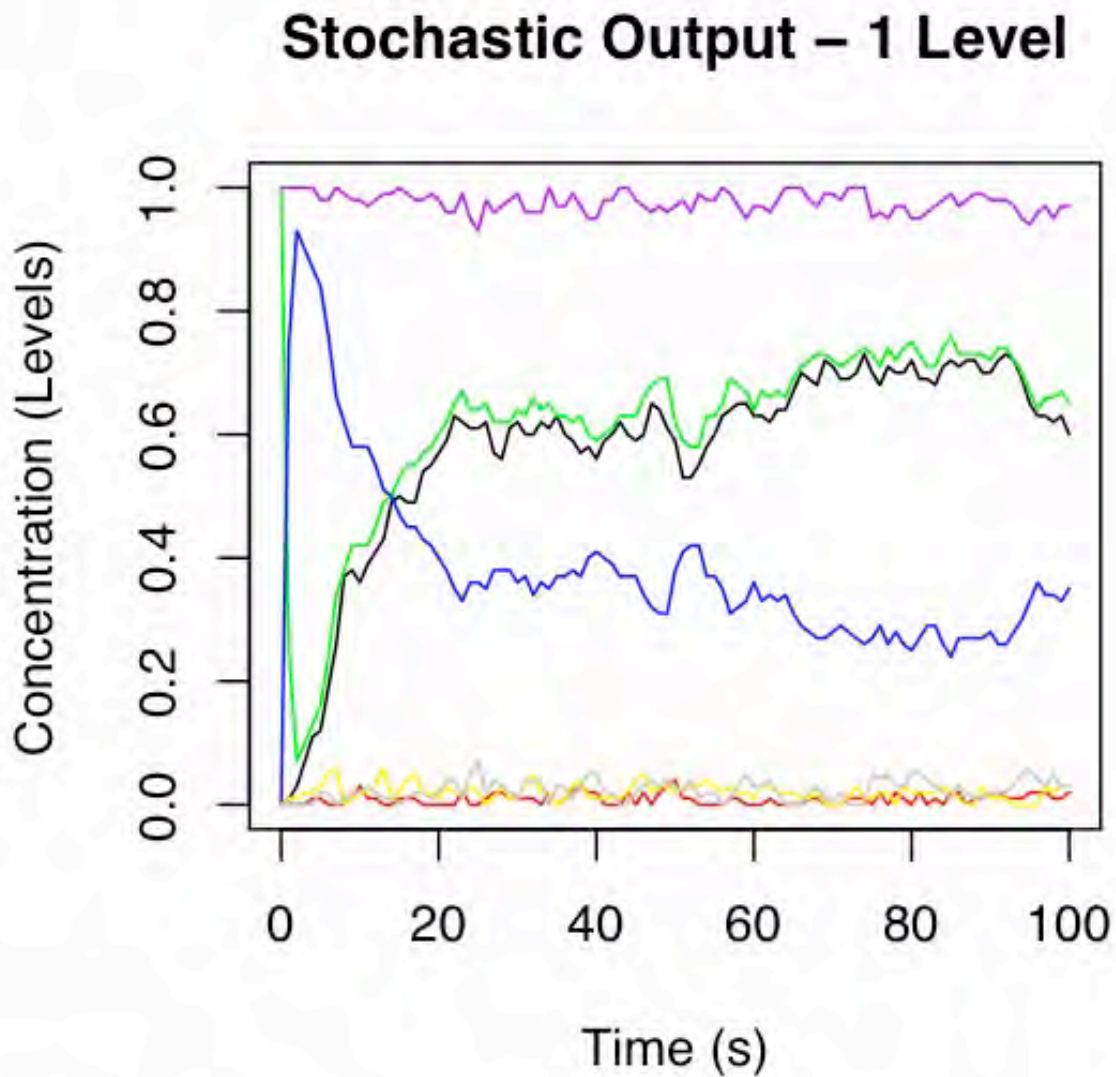
- ❑ **transitions get a stochastic waiting time**
 - > *exponential distribution with parameter λ*
- ❑ **state-dependent λ defined by rate function**
 - > *any arithmetic function including
the transition's pre-places as integer variables and
user-defined real-valued parameters*
 - > *modifier arcs*
 - > *popular kinetics:
mass-action semantics, level semantics*
- ❑ **semantics: Continuous Time Markov Chain (CTMC)**
 - > *reachability graph + state transition rates*
- ❑ **analysis**
 - > *standard Markov analysis techniques: transient, steady state*
 - > *stochastic simulation algorithms (SSA), e.g. Gillespie's SSA*

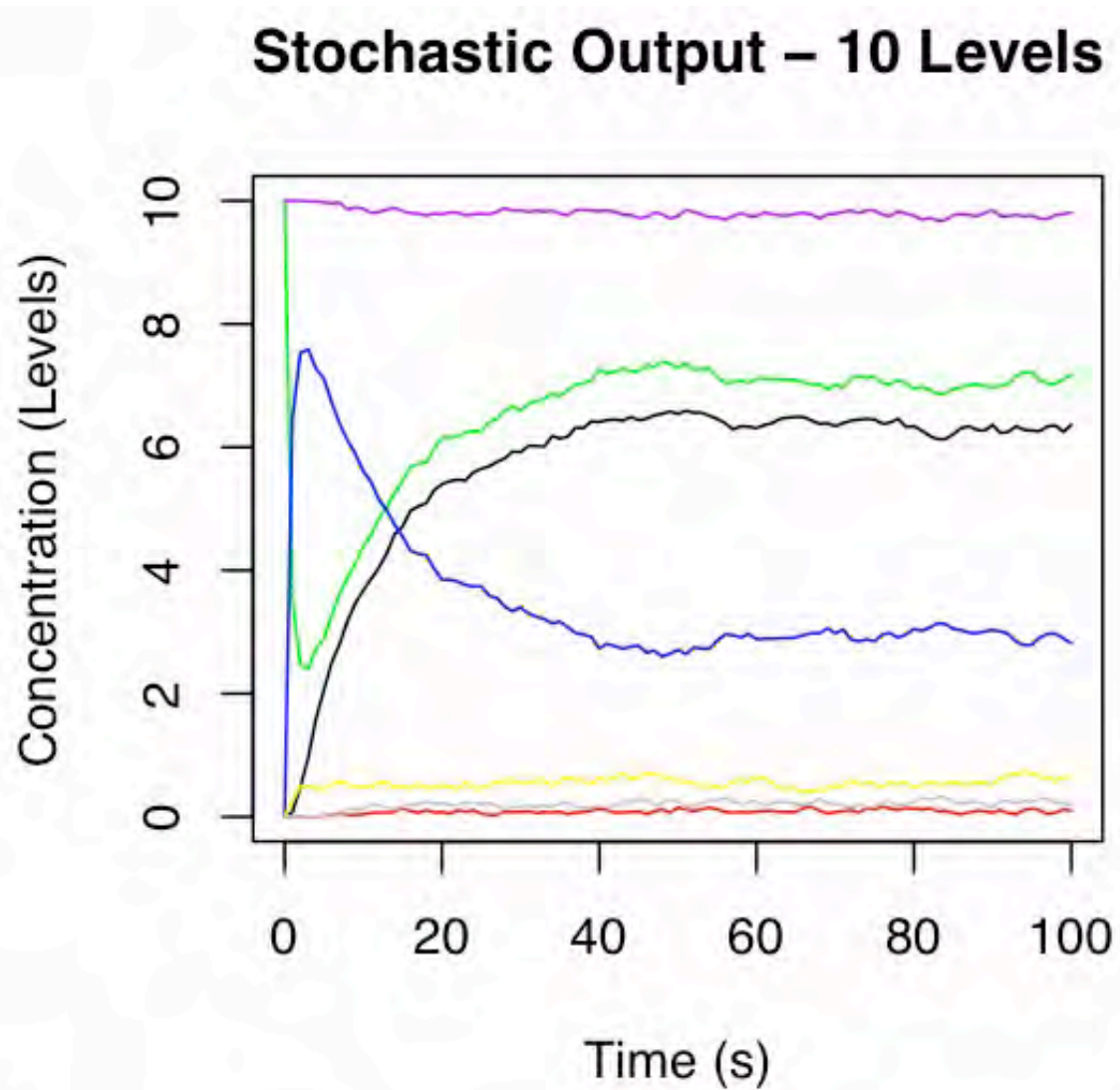
- *molecules semantics*

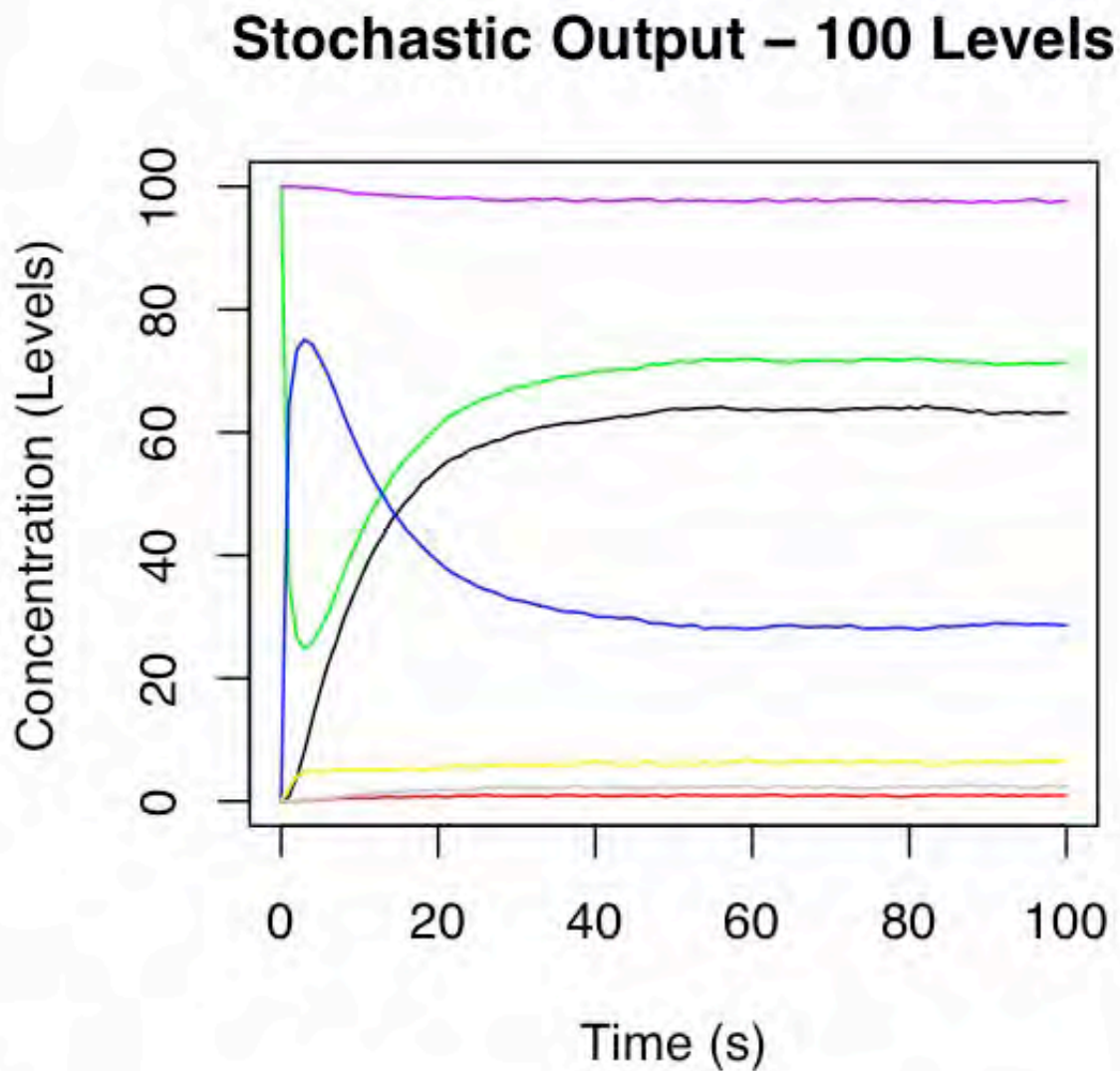
$$h_t := c_t \cdot \prod_{p \in \bullet t} \binom{m(p)}{f(p, t)}$$

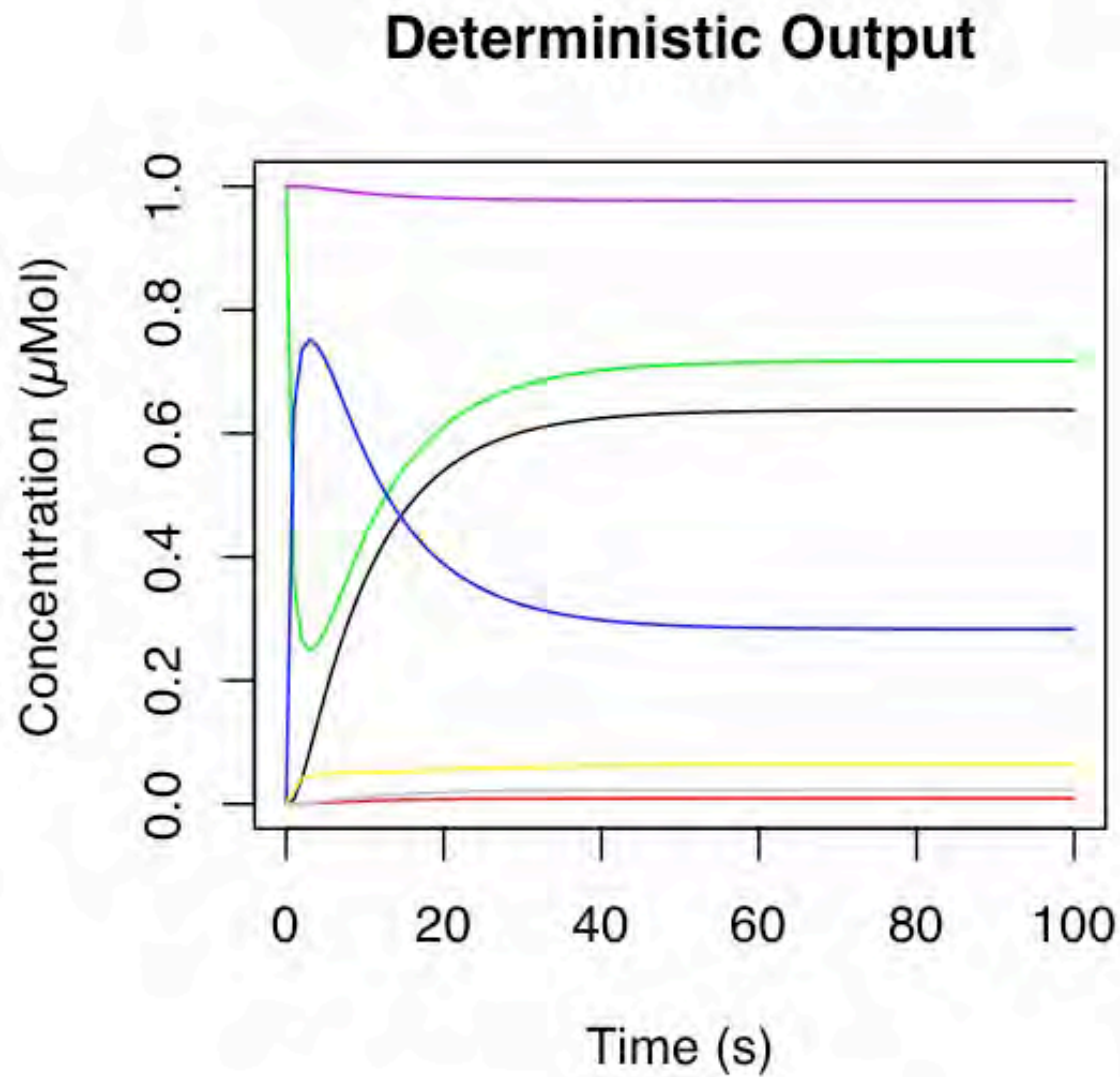
- *concentration levels semantics*

$$h_t := k_t \cdot N \cdot \prod_{p \in \bullet t} \left(\frac{m(p)}{N} \right)$$



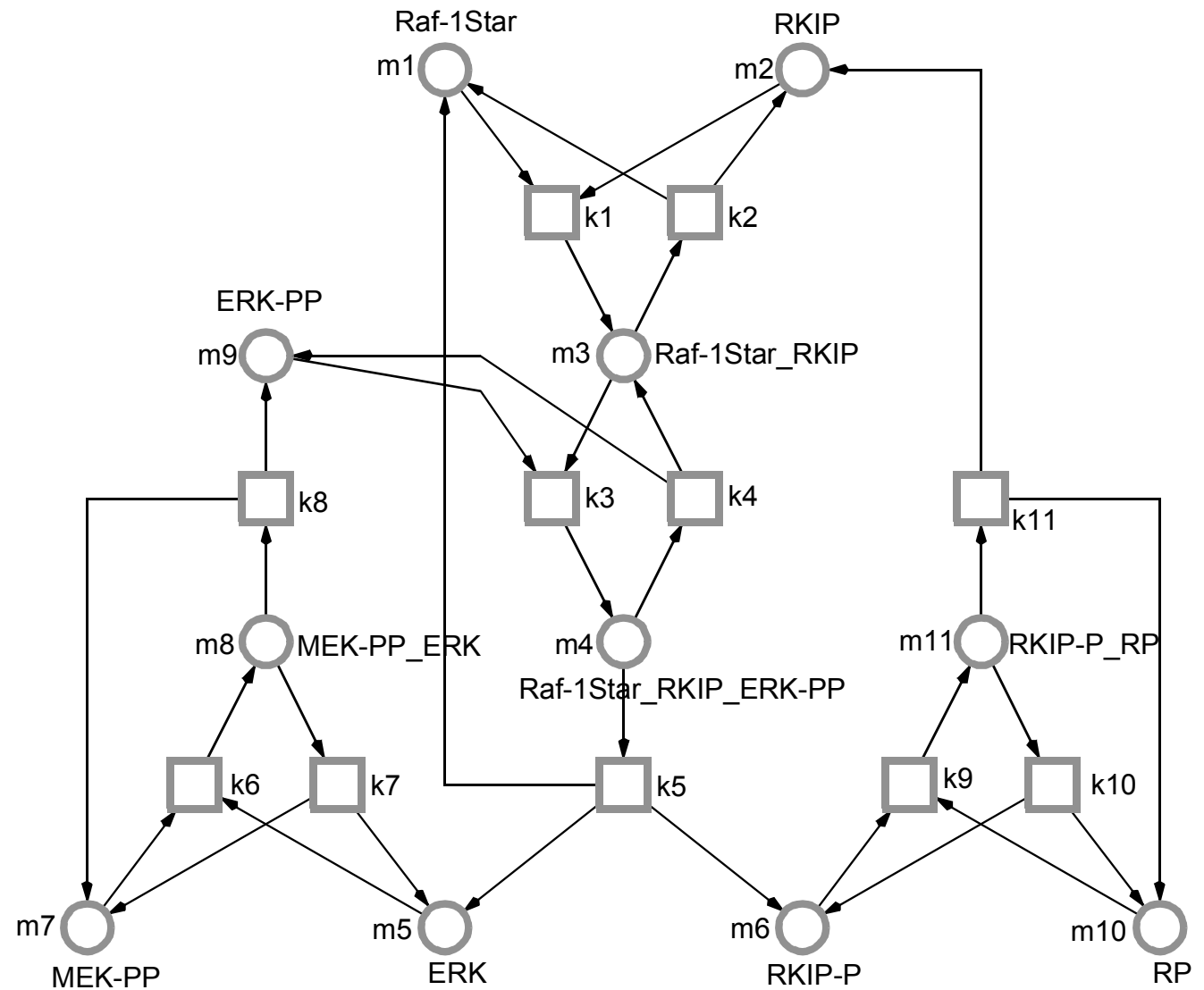






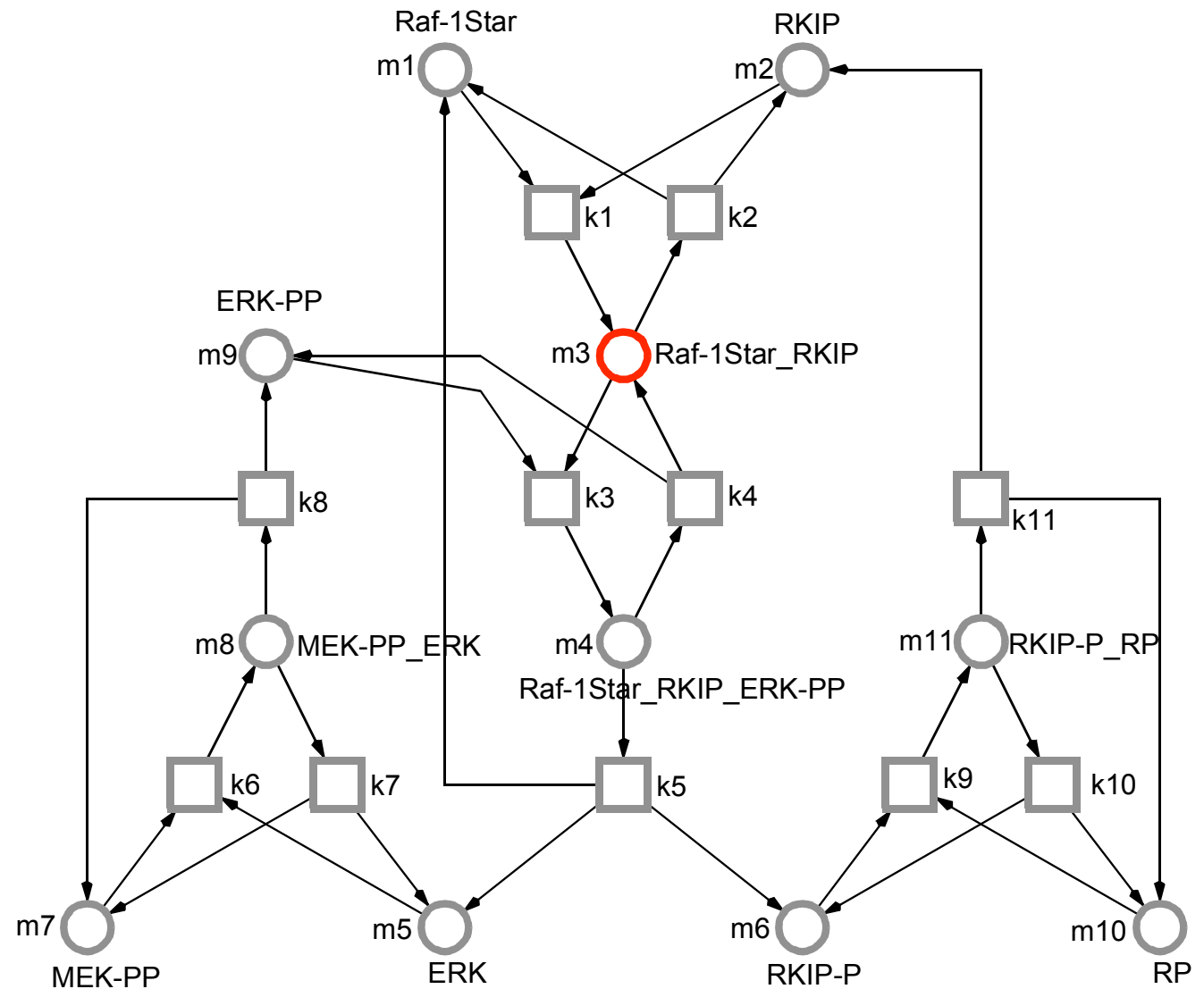
CONTINUOUS PETRI NETS - CPN -

- ❑ **transitions fire continuously**
- ❑ **rate functions**
 - > *any arithmetic function including the transition's pre-places as real-valued variables and user-defined real-valued parameters*
- ❑ **real-valued tokens**
 - > *concentrations*
- ❑ **semantics: set of Ordinary Differential Equations (ODEs)**
 - > *uniquely defined, but not vice versa*
 - > *typically non-linear*
- ❑ **simulation (numerical integration)**
 - > *stiff/unstiff solvers*



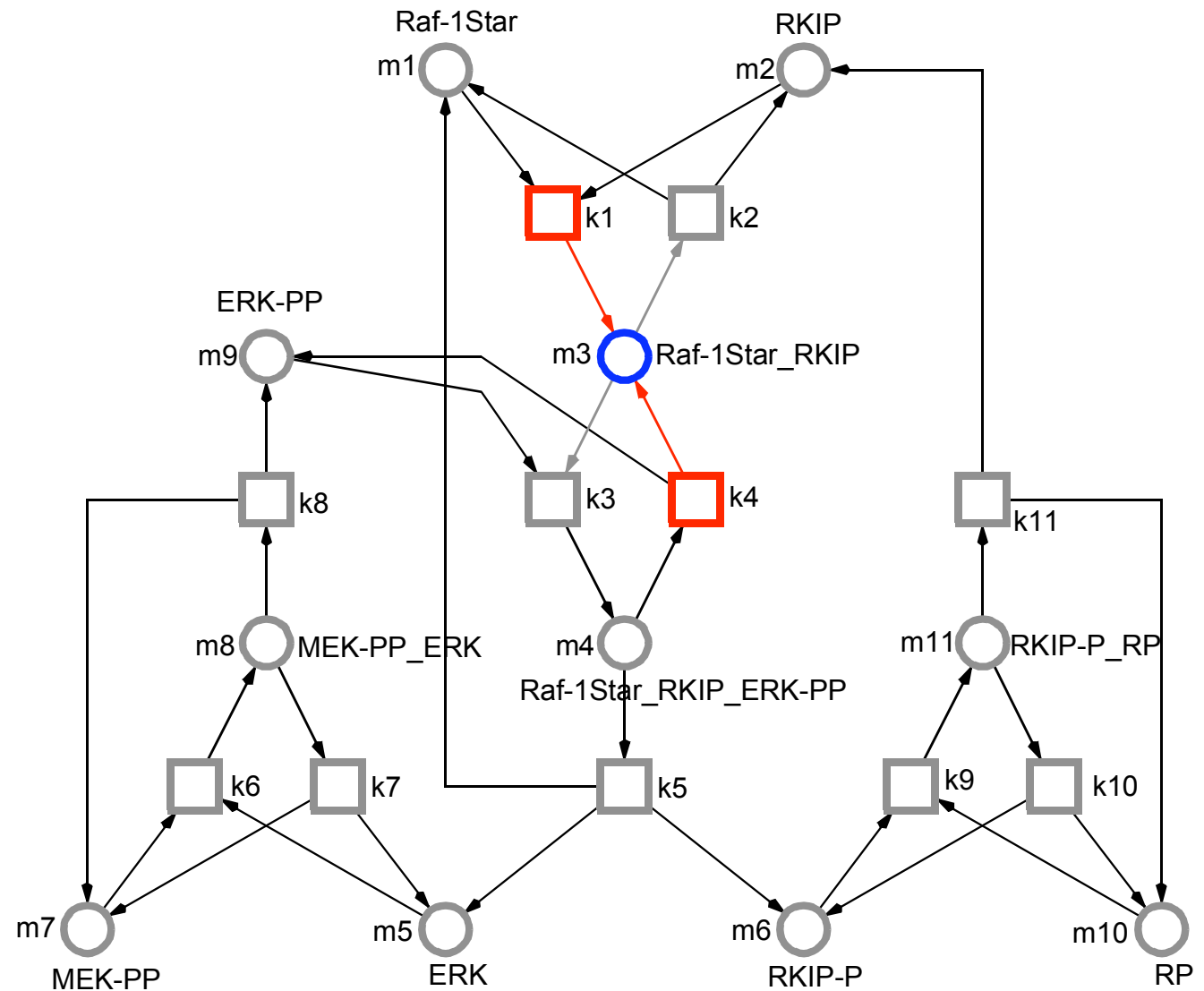
CONTINUOUS PETRI NET DEFINES ODEs

$$\frac{dm_3}{dt} =$$



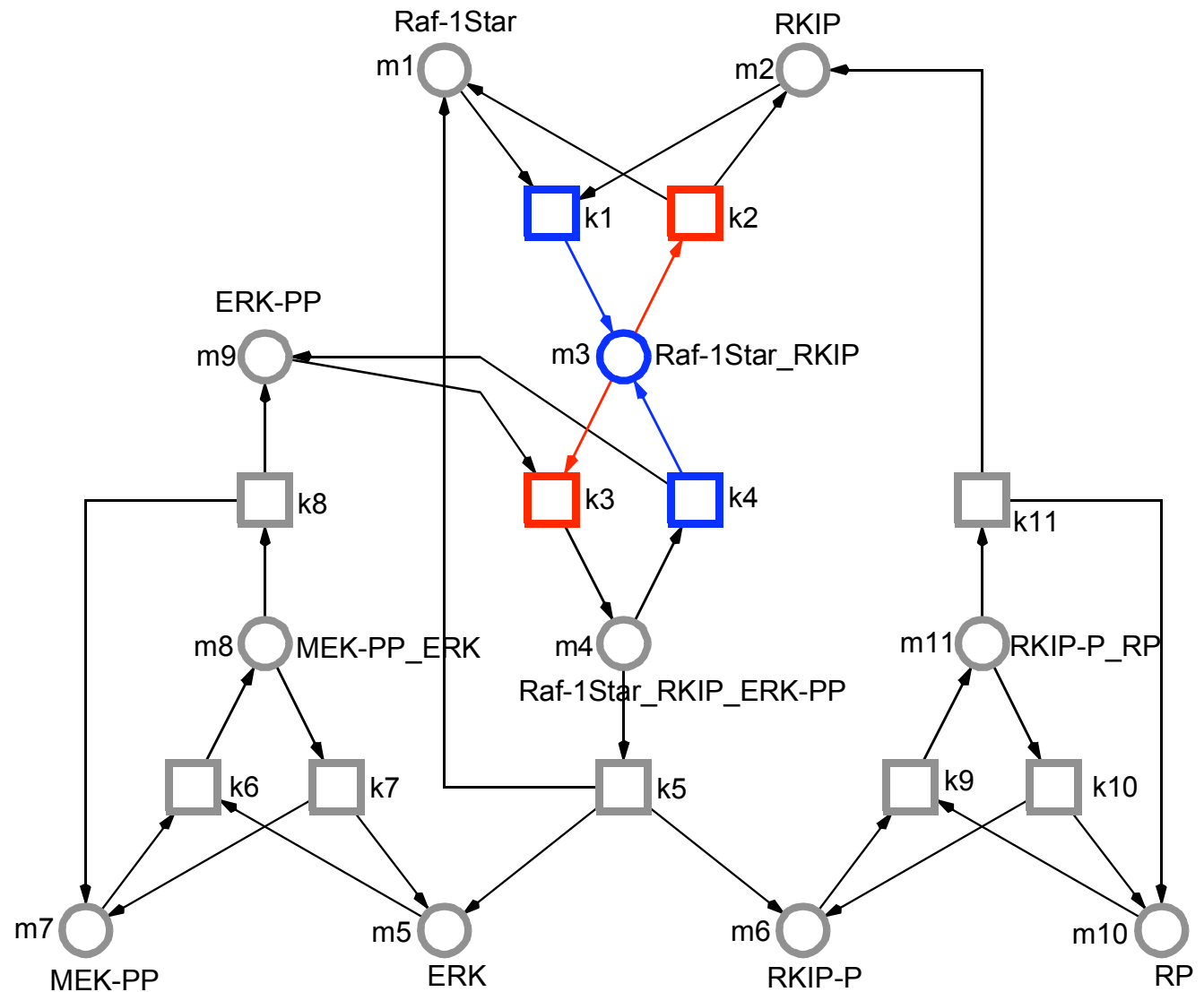
CONTINUOUS PETRI NET DEFINES ODEs

$$\frac{dm_3}{dt} = +r_1 + r_4$$



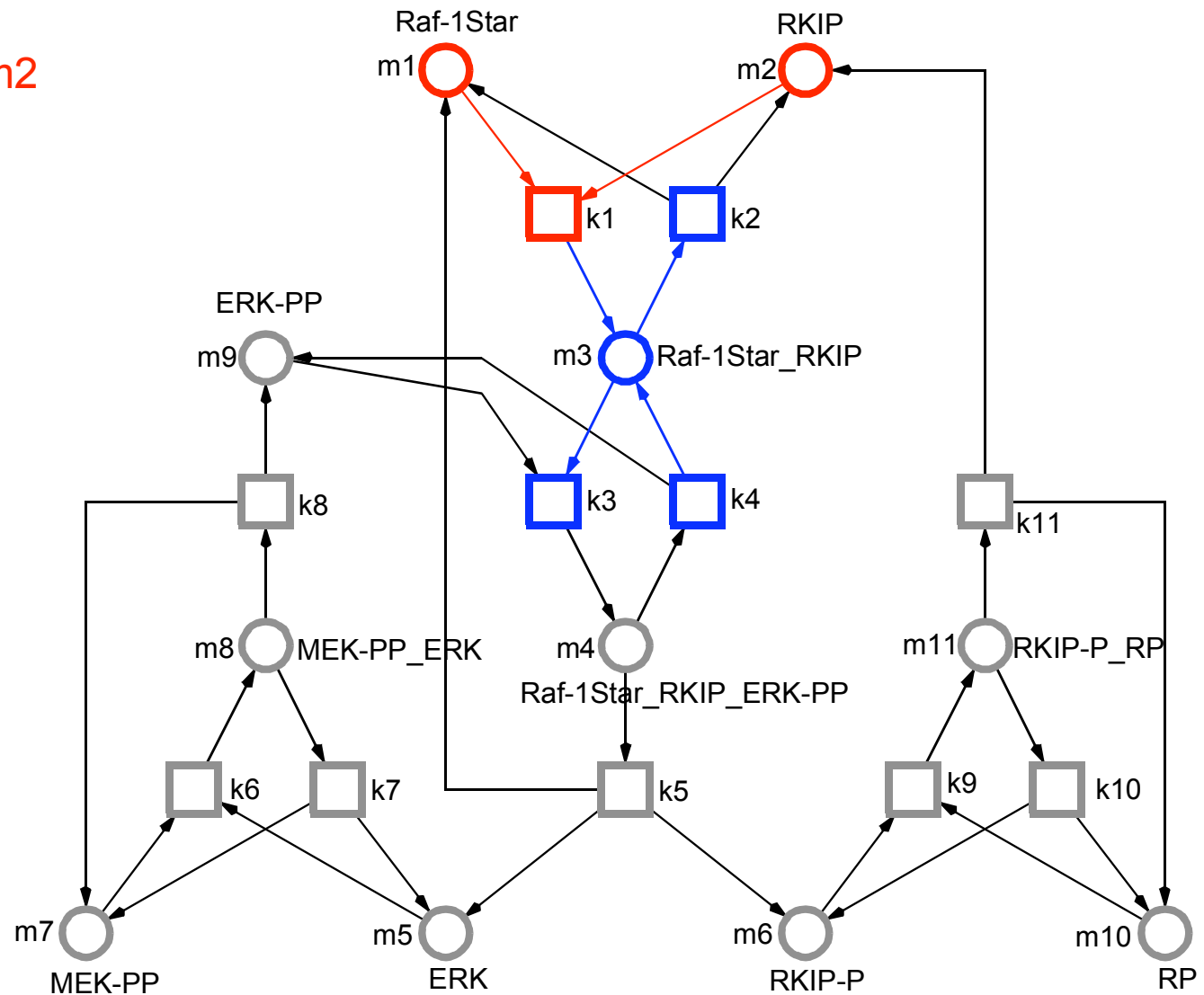
CONTINUOUS PETRI NET DEFINES ODEs

$$\frac{dm_3}{dt} = +r_1$$
$$+r_4$$
$$-r_2$$
$$-r_3$$

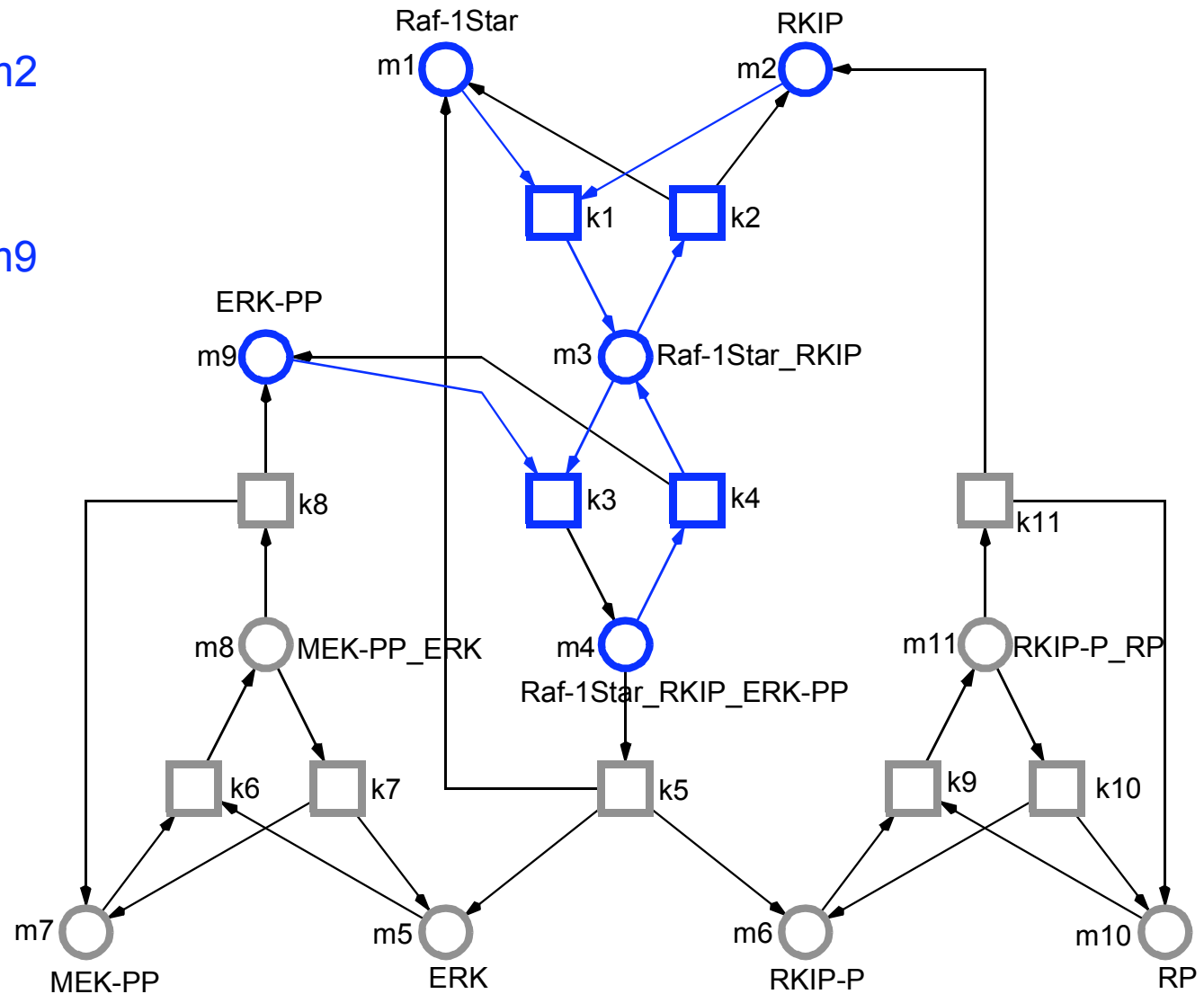


CONTINUOUS PETRI NET DEFINES ODES

$$\frac{dm_3}{dt} = +k_1 * m_1 * m_2 + r_4 - r_2 - r_3$$



$$\begin{aligned} \frac{dm_3}{dt} = & + k_1 * m_1 * m_2 \\ & + k_4 * m_4 \\ & - k_2 * m_3 \\ & - k_3 * m_3 * m_9 \end{aligned}$$



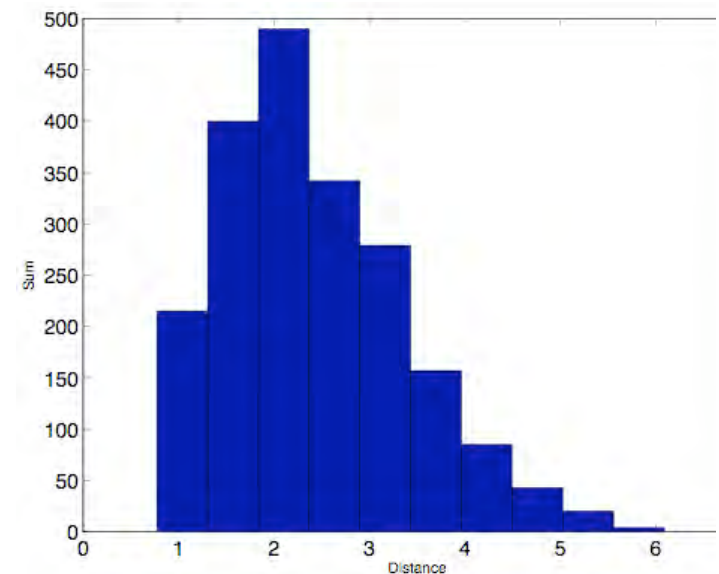
**THE QUALITATIVE MODEL
BECOMES
THE STRUCTURED DESCRIPTION
OF THE QUANTITATIVE MODEL !**

Species	S1	S2	S3	S4	S5	S6	S7	S8	S9	S10	S11	S12	S13
Raf-1*	1	0	0	1	1	1	1	1	0	0	1	1	1
RKIP	1	0	0	0	0	0	0	1	0	0	1	0	0
Raf-1*_RKIP	0	1	0	0	0	0	0	0	1	1	0	0	0
Raf-1*_RKIP_ERK-PP	0	0	1	0	0	0	0	0	0	0	0	0	0
ERK	0	0	0	1	0	0	1	1	1	0	0	0	0
RKIP-P	0	0	0	1	1	0	0	0	0	0	0	0	1
MEK-PP	1	1	1	1	0	0	1	1	1	0	0	1	1
MEK-PP_ERK	0	0	0	0	1	1	0	0	0	1	1	0	0
ERK-PP	1	1	0	0	0	0	0	0	0	0	0	1	1
RP	1	1	1	1	1	0	0	1	1	1	1	0	1
RKIP-P_RP	0	0	0	0	0	1	1	0	0	0	0	1	0

Cho et al

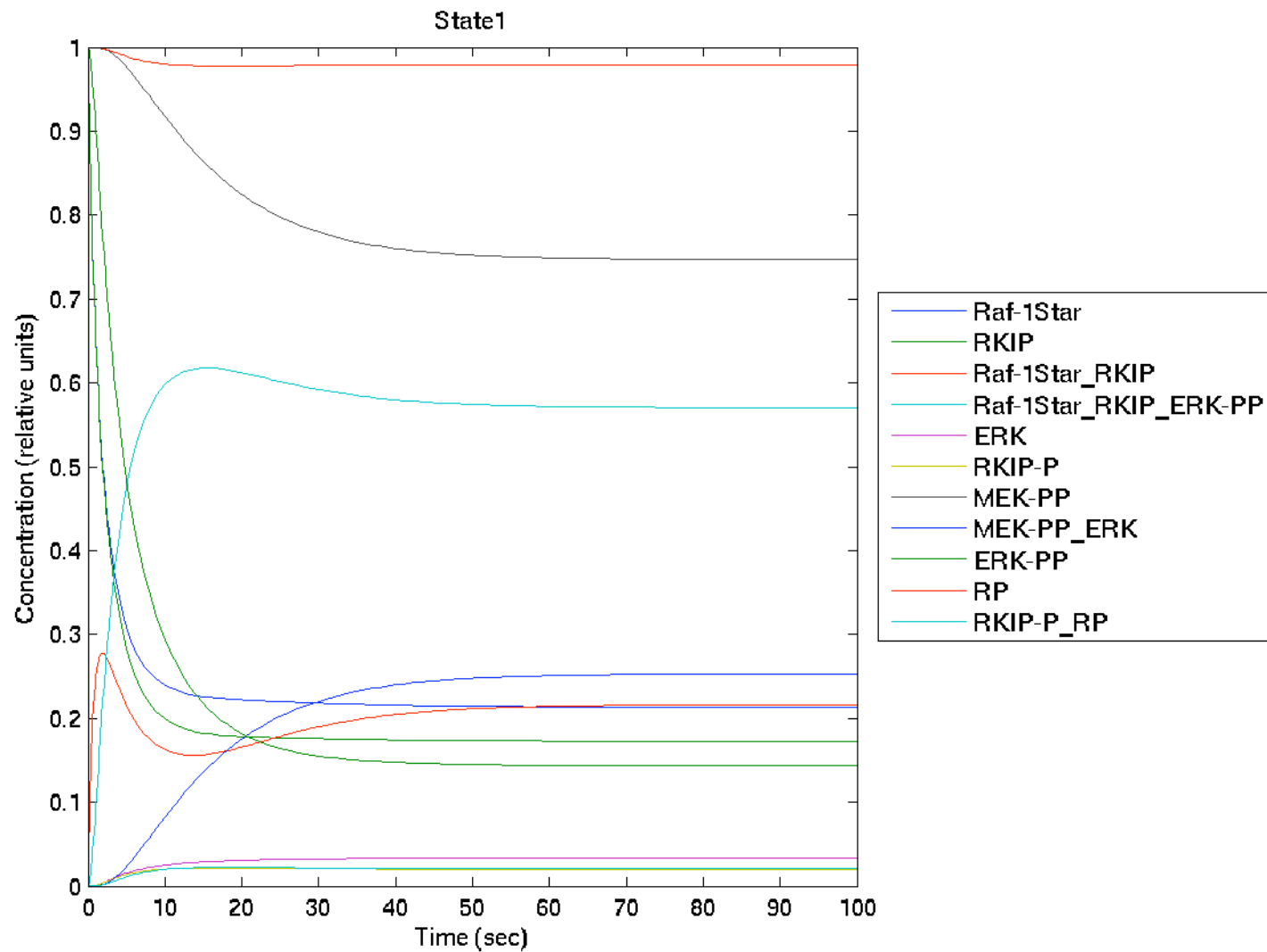
Biochemist

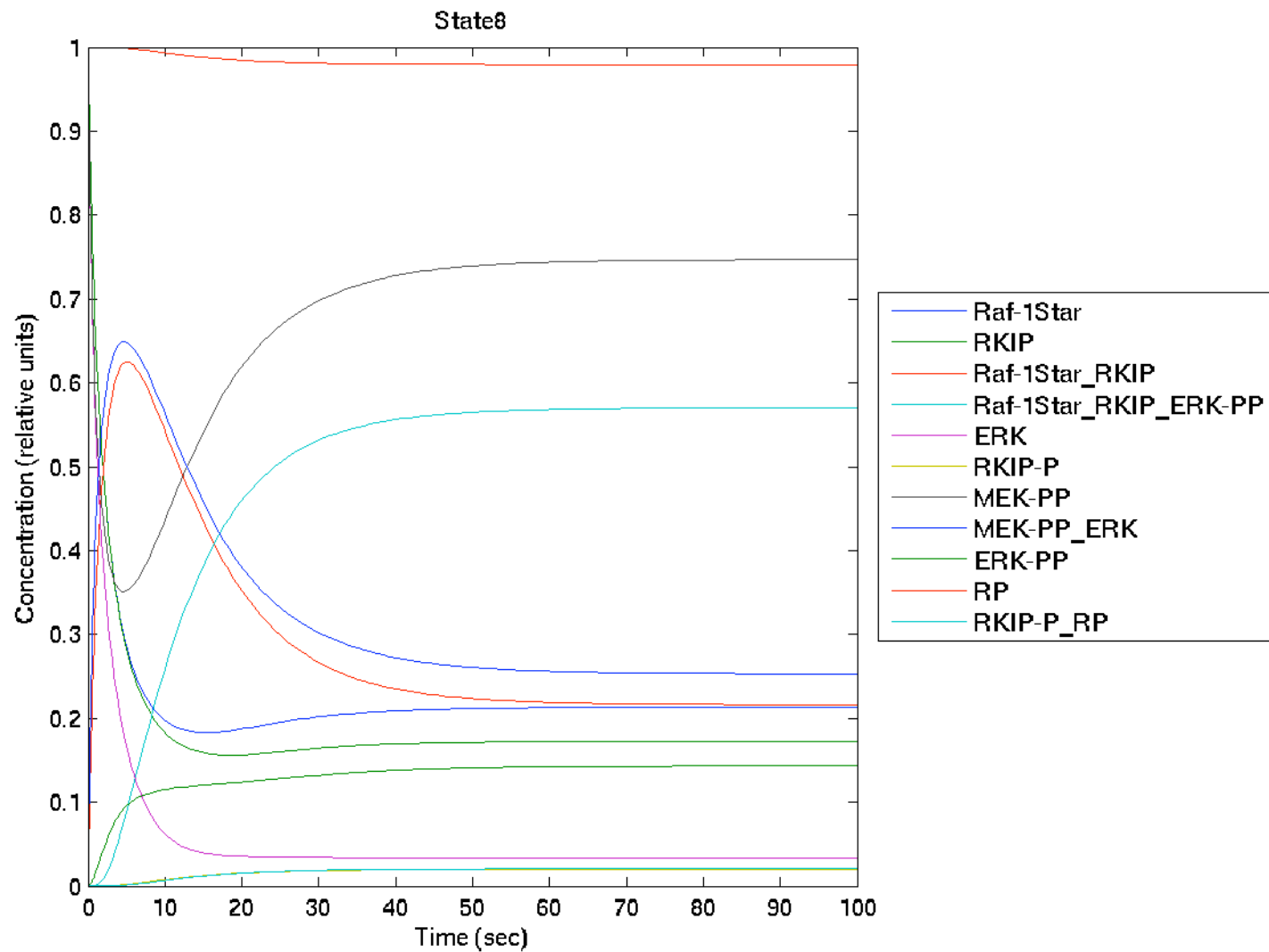
13 “good” state configurations

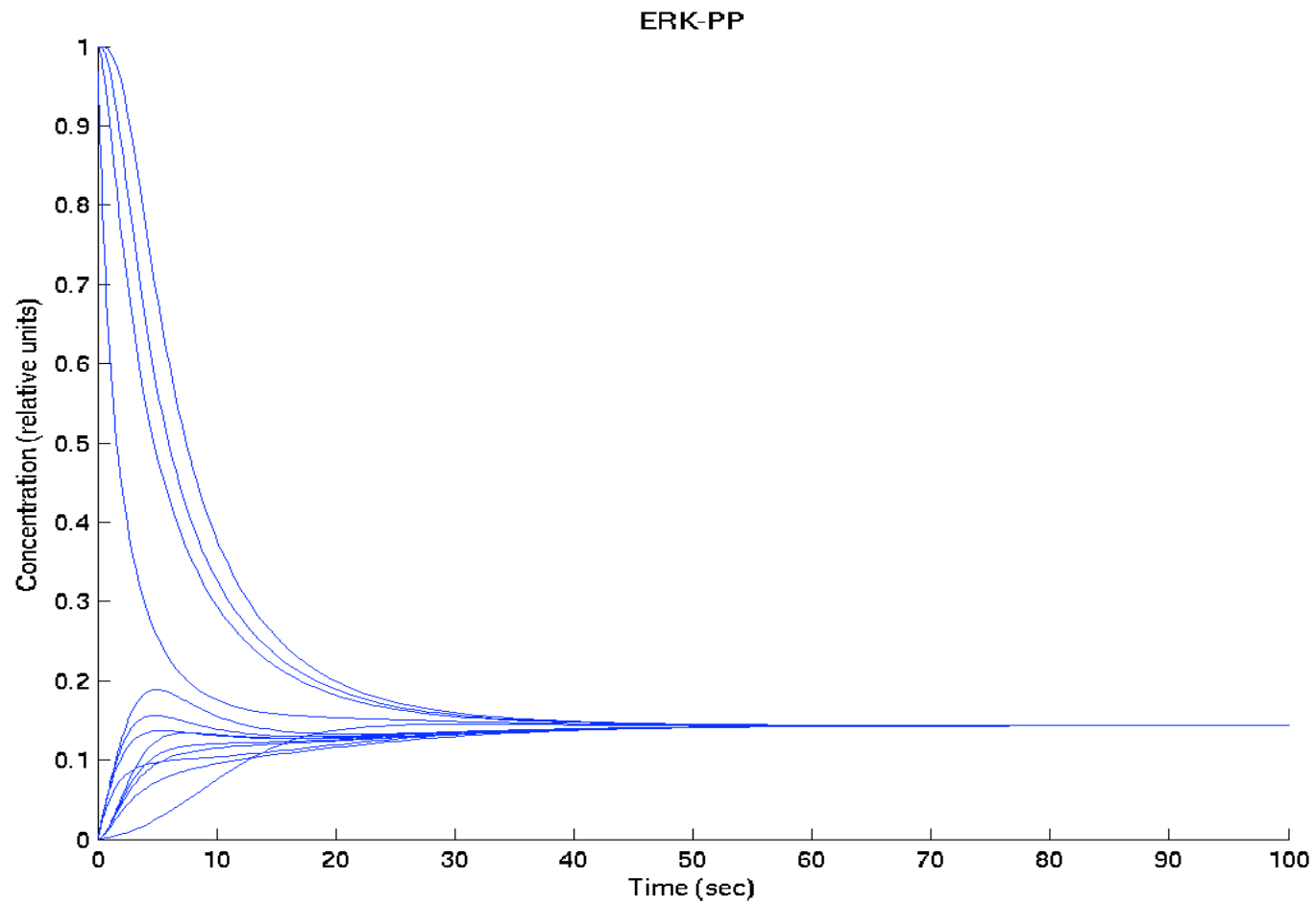


Distribution of 'bad' steady states as euclidean distances from the 'good' final steady state

the “bad” ones







SUMMARY

❑ representation of bionetworks by Petri nets

- > *partial order representation*
- > *formal semantics*
- > *unifying view*

-> *better comprehension*

-> *sound analysis techniques*

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❑ purposes

- > *animation*
- > *model validation against consistency criteria*
- > *qualitative / quantitative behaviour prediction*

- > *to experience the model*
- > *to increase confidence*
- > *experiment design,
new insights*

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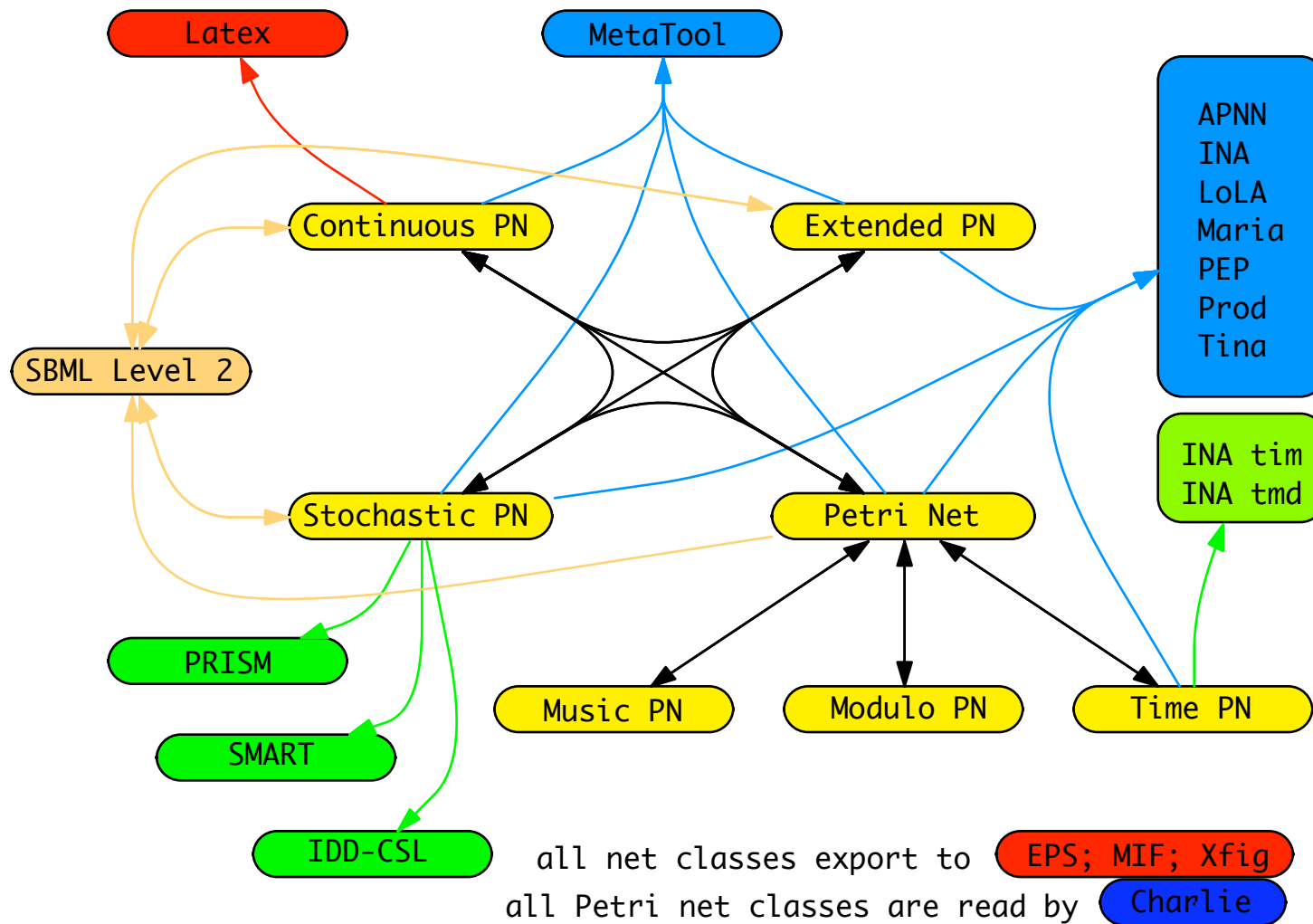
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- > *qualitative / quantitative behaviour prediction*

- > *to experience the model*
- > *to increase confidence*
- > *experiment design, new insights*

❑ step-wise model development

- > *qualitative model*
- > *discrete quantitative model*
- > *continuous quantitative model*

- > *discrete Petri nets*
- > *stochastic Petri nets*
- > *continuous Petri nets = ODEs*



❑ **Rainer Breitling**

*University Glasgow, Integrative and Systems Biology &
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❑ **David Gilbert**

*Brunel University London/Uxbridge,
School of Information Systems, Computing and Mathematics*

❑ **Wolfgang Marwan**

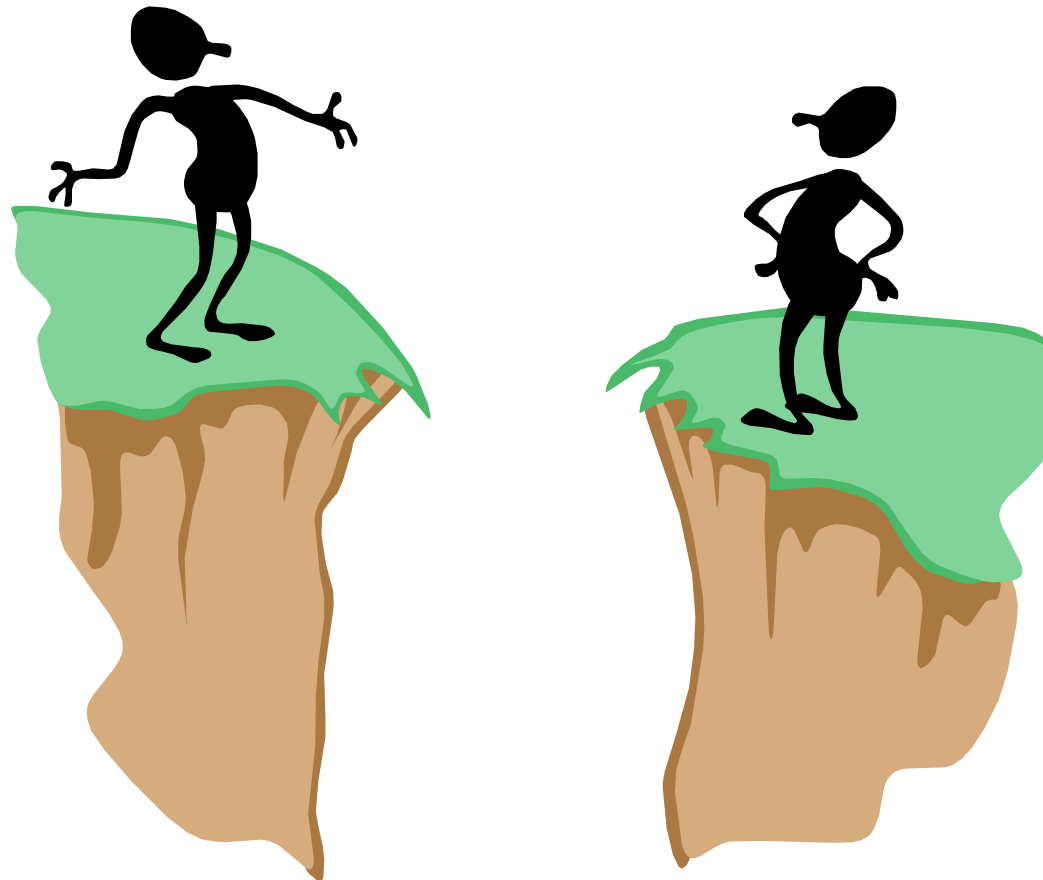
*Otto von Guericke University & Magdeburg Centre for Systems Biology &
Max Planck Institute for Dynamics of Complex Technical Systems*

❑ **Louchka Popova-Zeugmann**

Humboldt University Berlin, Computer Science Institute

- ❑ M Heiner; R Donaldson; D Gilbert:
Petri Nets for Systems Biology; MS Iyengar (ed.): Symbolic Systems Biology: Theory and Methods, Jones & Bartlett Publishers, LLC, 2010.
- ❑ D Gilbert, M Heiner, S Rosser, R Fulton, X Gu, M Trybilo:
A Case Study in Model-driven Synthetic Biology; IFIP WCC 2008, BICC 2008, Milano, Sept. 2008, Springer Boston, IFIP, Vol . 268, pp. 163-175, 2008.
- ❑ M Heiner, D Gilbert, R Donaldson:
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- ❑ D Gilbert, M Heiner, S Lehrack:
A Unifying Framework for Modelling and Analysing Biochemical Pathways Using Petri Nets; Proc. CMSB 2007, Edinburgh, Springer LNCS/LNBI 4695, pp. 200-216.

- ❑ M Heiner, C Rohr, M Schwarick, S Streif:
A Comparative Study of Stochastic Analysis Techniques; Proc. CMSB 2010, Trento, September 2010, ACM digital library 2010.
- ❑ C Rohr, W Marwan, M Heiner:
Snoopy - a unifying Petri net framework to investigate biomolecular networks;
Bioinformatics 2010 26(7): 974-975
- ❑ M Heiner, S Lehrack, D Gilbert, W Marwan:
Extended Stochastic Petri Nets for Model-based Design of Wet-lab Experiments;
Trans. on Comp. Systems Biology XI, Springer LNBI 5750, pp. 138-163, 2009.
- ❑ M Heiner, M Schwarick, A Tovchigrechko:
DSSZ-MC - A Tool for Symbolic Analysis of Extended Petri Nets; Proc. Petri Nets
2009, Paris, June 2009, Springer LNCS 5606, pp. 323-332.
- ❑ M Schwarick, M Heiner:
CSL model checking of biochemical networks with Interval Decision Diagrams; Proc.
CMSB 2009, Bologna, September 2009, Springer LNCS/LNBI 5688, pp. 296-312.



THANKS !

[HTTP://WWW-DSSZ.INFORMATIK.TU-COTTBUS.DE](http://www-dssz.informatik.tu-cottbus.de)