

# Generalized Hybrid Petri Nets

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# Motivations

- Some biological models require to be represented in hybrid way (Cells/Molecular interactions in one model).
- Continuous deterministic simulation does not consider the fluctuation of molecules, specially when there is a low number of them.
- Stochastic Simulation is computational expensive (fast reactions, large number of molecules).

# CPN and GSPN

- Continuous Petri Nets:
  - Continuous places
  - Continuous transitions
- Generalized Stochastic Petri Nets
  - Discrete places
  - Stochastic transitions
  - Immediate transitions
  - Deterministic transitions
  - Scheduled transitions

# Features of GHPN

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# Elements



Discrete



Continuous

## Places



stochastic



continuous



immediate



deterministic

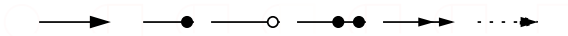
&lt;1&gt;



scheduled

[\_SimStart,1,\_SimEnd]

## Transitions



standard

read

inhibitor

equal

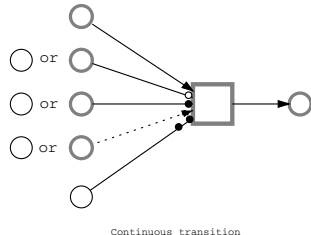
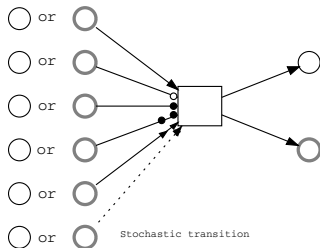
reset

modifier

## Edges



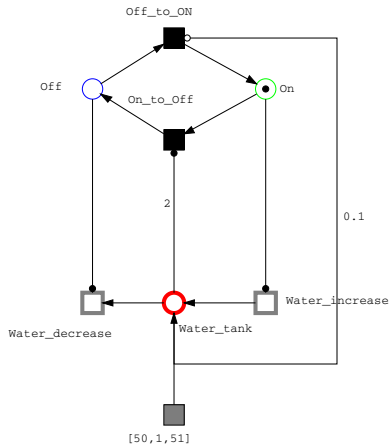
# Connectivity



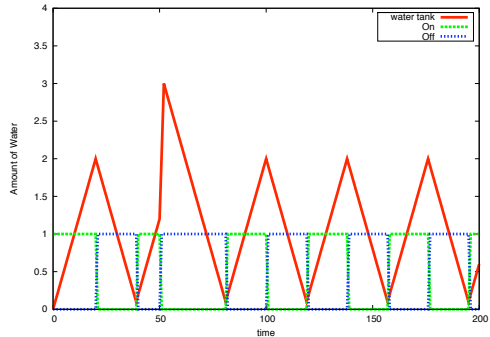
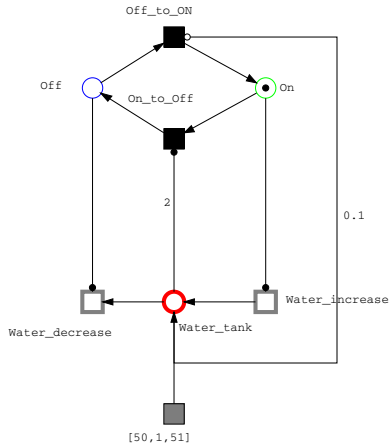
# Examples

- Water Tank
- T7 Phage
- Goutsias Model

# The Water Tank Model



# The Water Tank Model



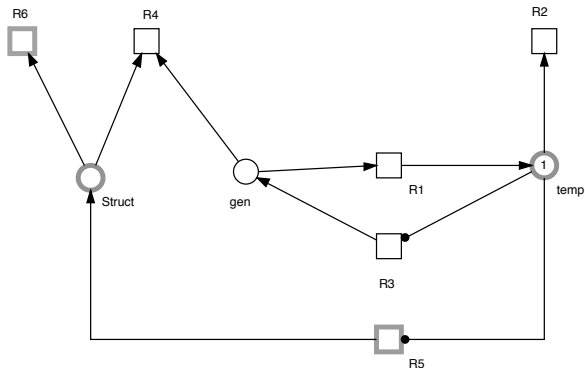
# T7 Phage

No.	Reaction	Propensity	Rate
R1	$gen \rightarrow temp$	$c_1 \cdot gen$	$c_1 = 0.0025$
R2	$temp \rightarrow \phi$	$c_2 \cdot temp$	$c_2 = 0.25$
R3	$temp \rightarrow temp + gen$	$c_3 \cdot temp$	$c_3 = 1.0$
R4	$gen + struct \rightarrow \text{"virus"}$	$c_4 \cdot gen \cdot struct$	$c_4 = 7.5 \times 10E - 6$
R5	$temp \rightarrow temp + struct$	$c_5 \cdot temp$	$c_5 = 1000$
R6	$struct \rightarrow \phi$	$c_6 \cdot struct$	$c_6 = 1.99$

Srivastava et al 2002

# T7 Phage (GHPN)

- $R_5$  and  $R_6$  are represented as continuous reactions
- $R_1, R_2, R_3,$  and  $R_4$  are represented as continuous reactions



0.025

0.25

1

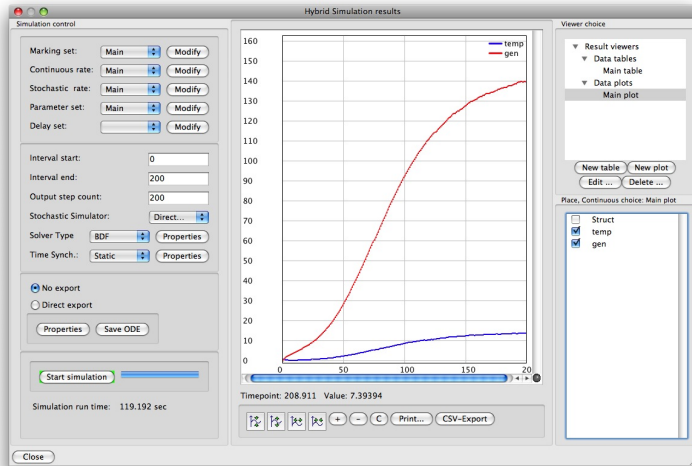
7.5e-06

1000

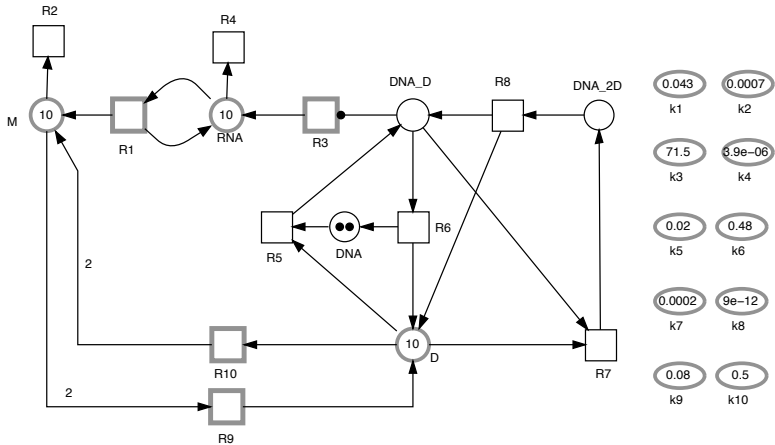
1.99



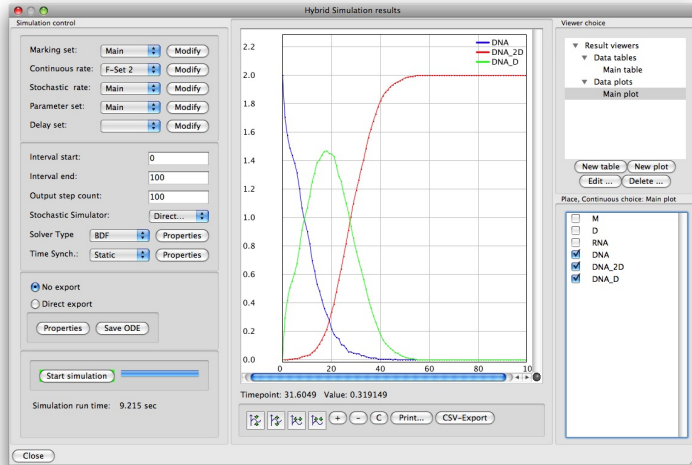
# T7 Phage Simulation Results



# Goutsias Model (GHPN)



# Goutsias Model (Simulation Results)



# Simulation Time

	Continuous	Stochastic	hybrid (static)	hybrid (dynamic)
Goutsias	0.01	0.972	0.014	0.138
T7 Phage	0.007	12.36	0.210	0.107

# Try It Now

- Get your copy at:  
<http://www-dssz.informatik.tu-cottbus.de/DSSZ/Software/Snoopy>
- The implementation is freely available as part of Snoopy
- GHPN enjoys all of Snoopy features

# Thank You