

## **PART II - TALK 2**

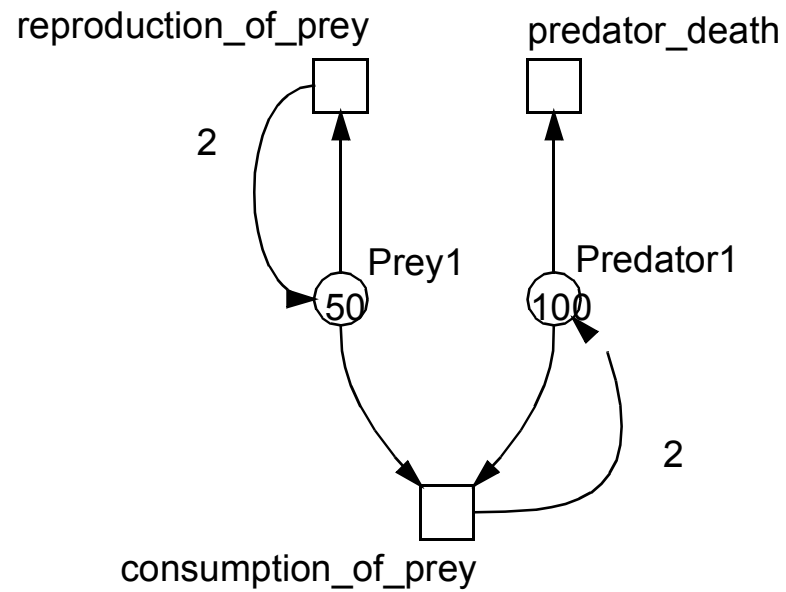
# **AND THEN THERE WAS COLOUR - COLOURED PETRI NET -**

**Monika Heiner**

**Brunel University, on sabbatical leave from  
Brandenburg University of Technology Cottbus**

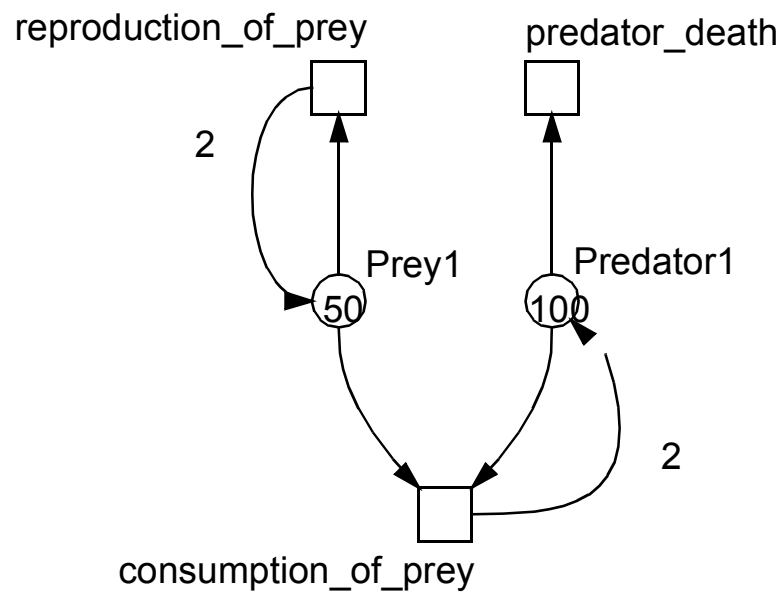
# Ex1: PREY - PREDATOR

sub-system1

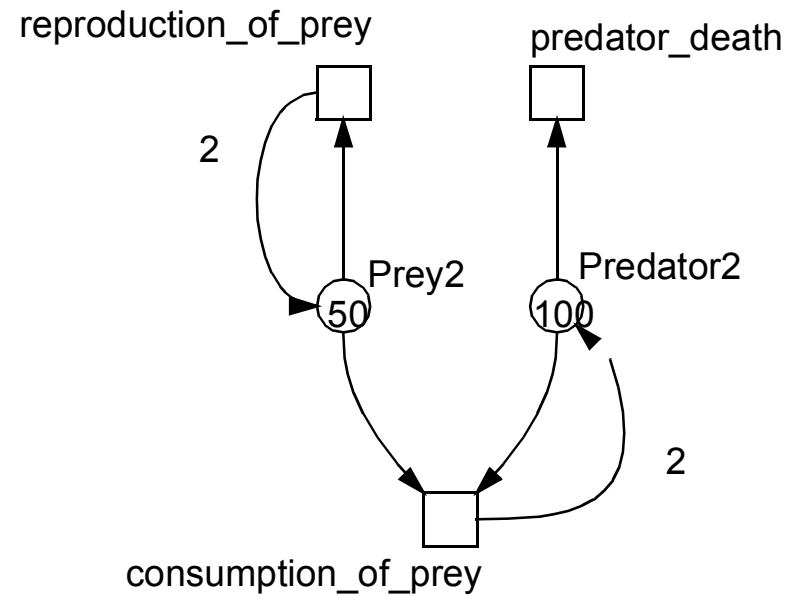


# Ex1: PREY - PREDATOR

sub-system1

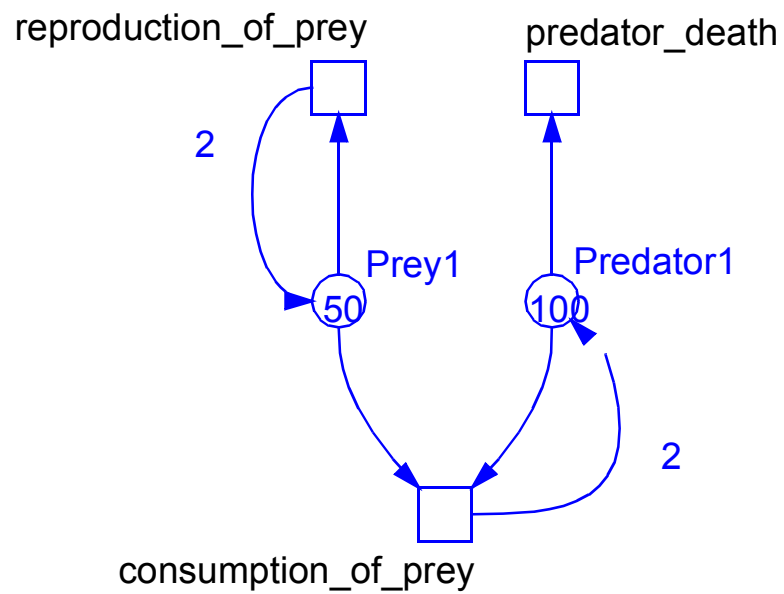


sub-system2

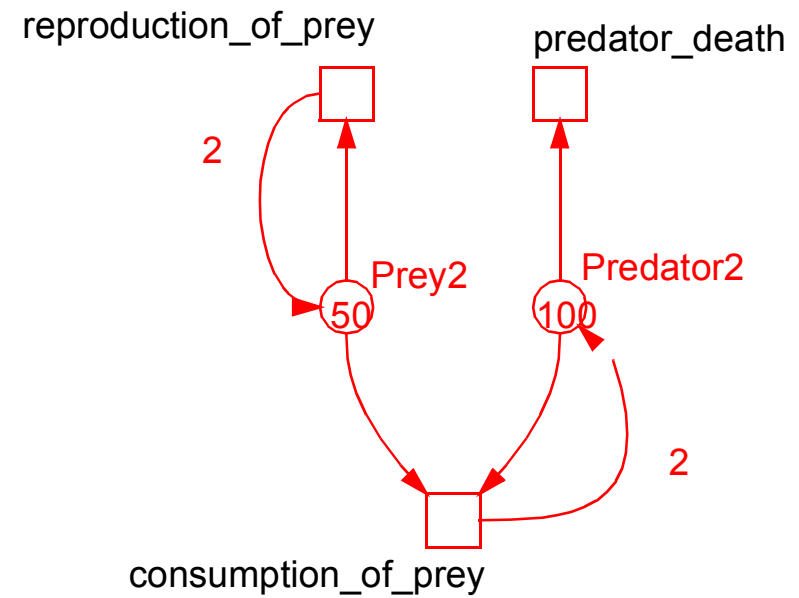


# Ex1: PREY - PREDATOR

sub-system1



sub-system2



## EX1: PREY - PREDATOR

### ❑ definitions

**colourset** CS = 1-2;

**var** x : CS;

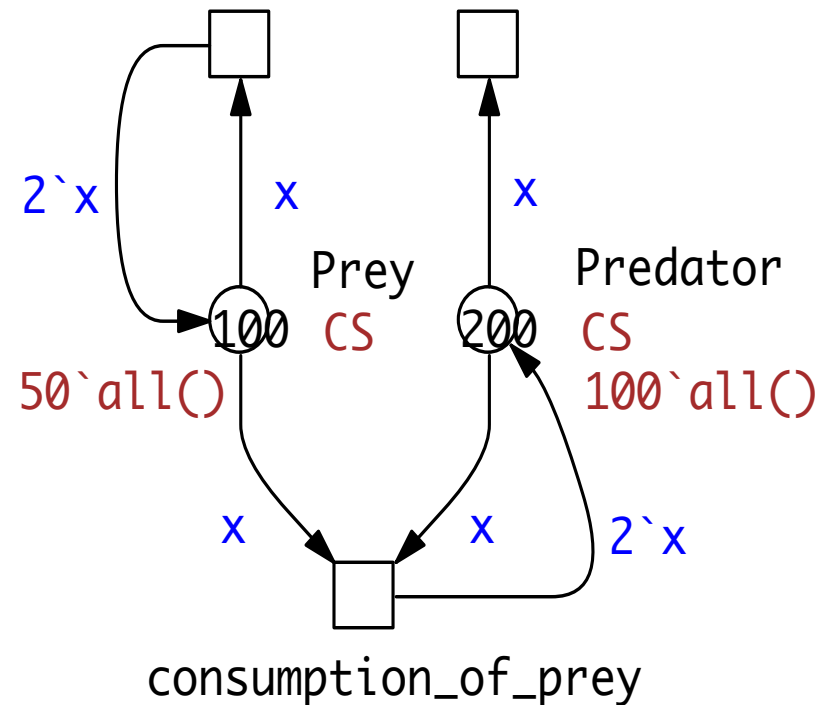
### ❑ better:

**const** SIZE = 2;

**colourset** CS = 1-SIZE;

**var** x : CS;

reproduction\_of\_preypredator\_death



### ❑ definitions

**colourset** CS = 1-2;

**var** x : CS;

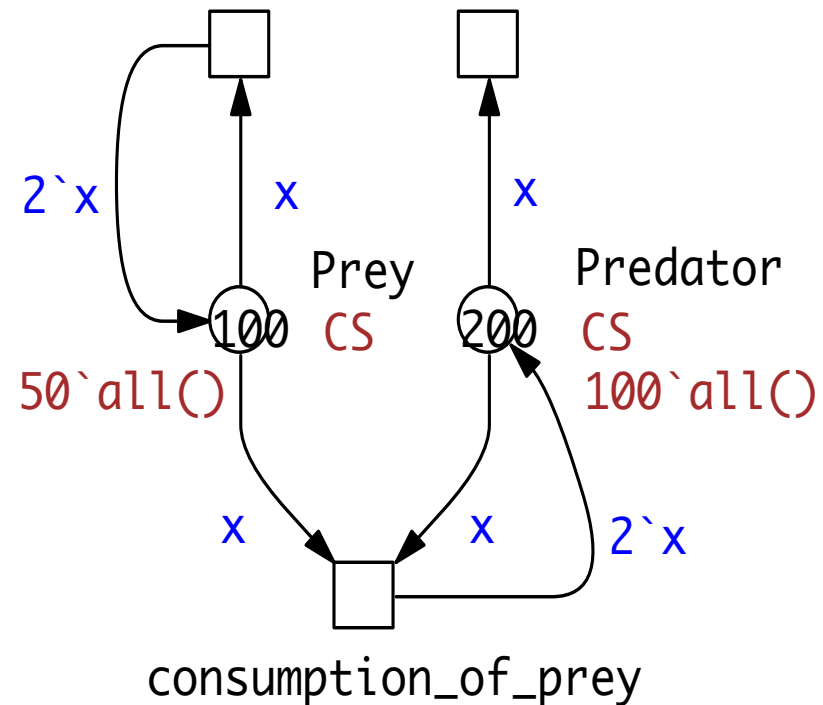
### ❑ better:

**const** SIZE = 2;

**colourset** CS = 1-SIZE;

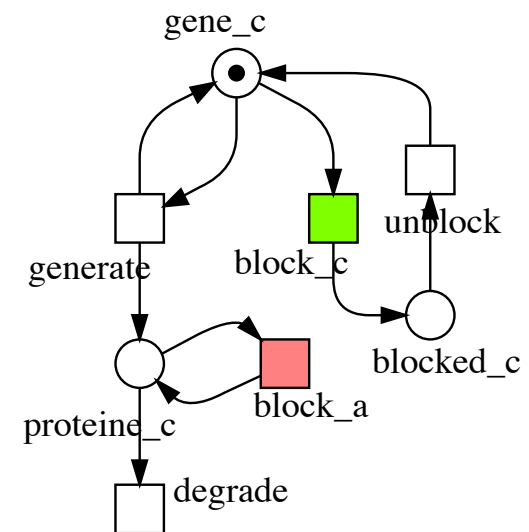
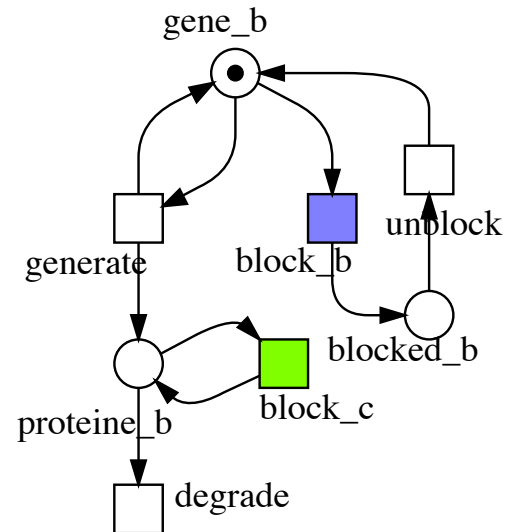
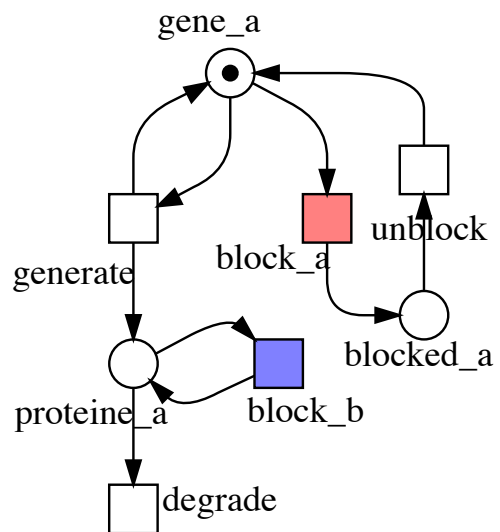
**var** x : CS;

reproduction\_of\_prey predator\_death

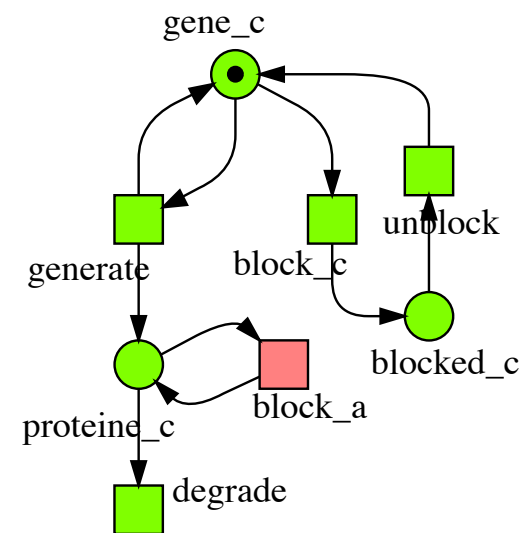
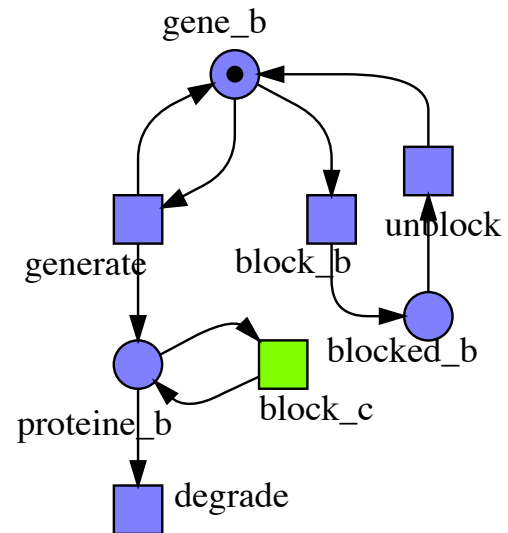
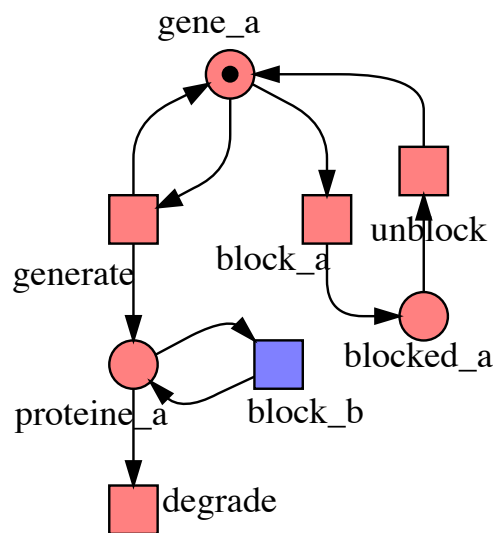


### ❑ changing SIZE adapts the model to various scenarios

## Ex2: REPRESSILATOR



## Ex2: REPRESSILATOR



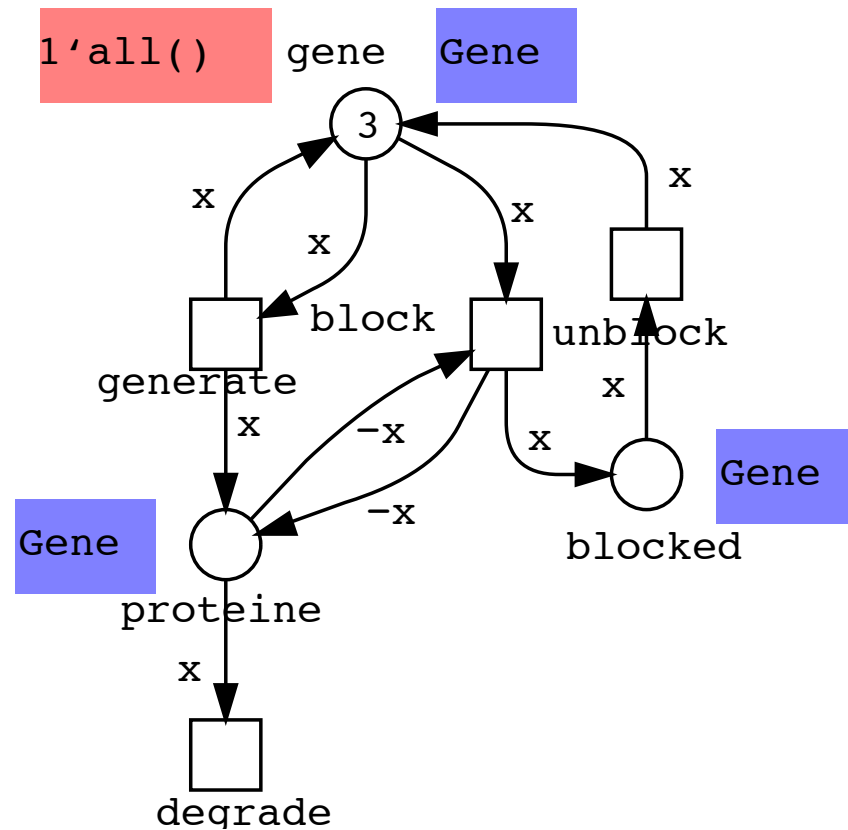


## EX2: REPRESSILATOR

### □ definitions

*colorset* Gene = enum a-c;

*var* x : Gene;



## EX2: REPRESSILATOR

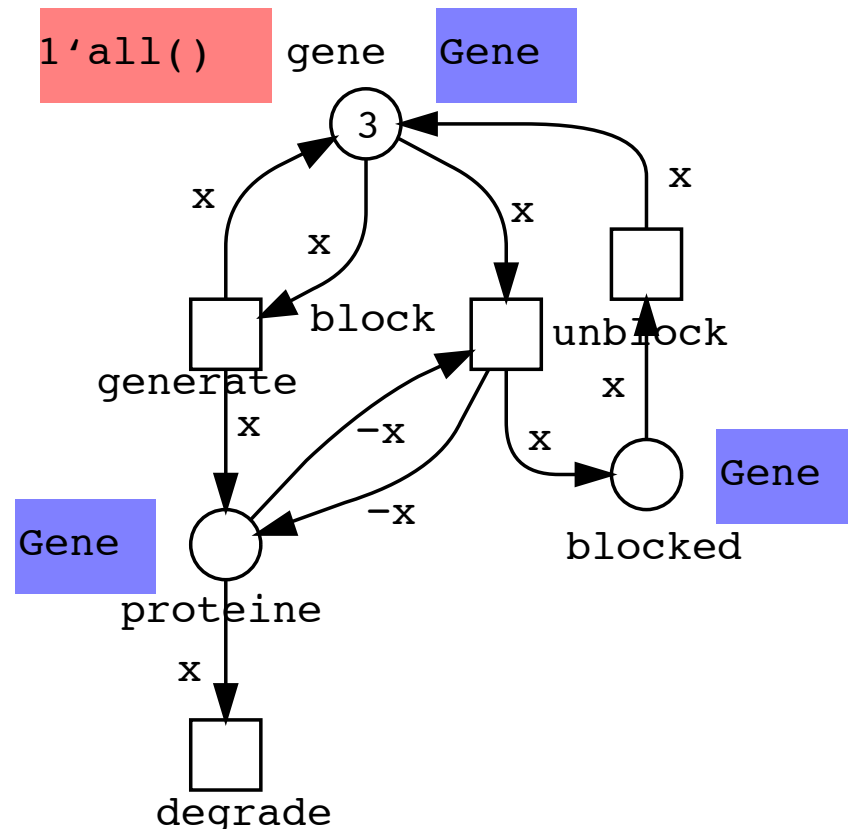
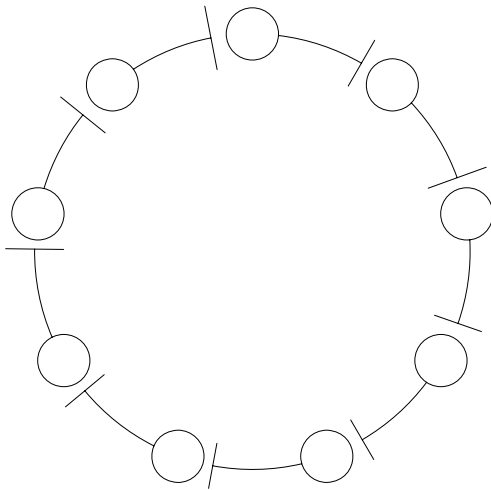
### ❑ definitions

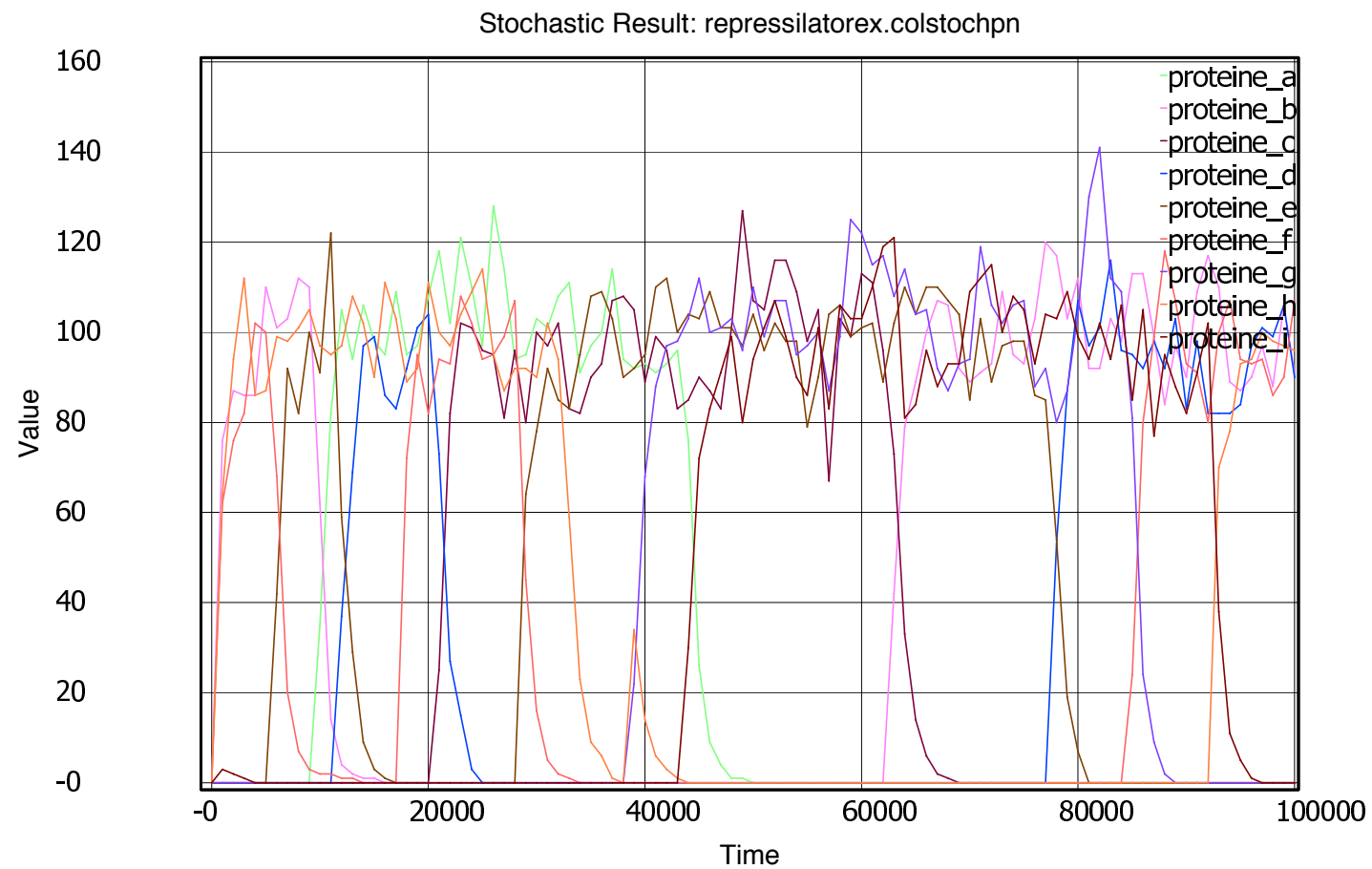
*colorset* Gene = enum a-c;

*var* x : Gene;

### ❑ model scaling

*colorset* Gene = enum a-i;

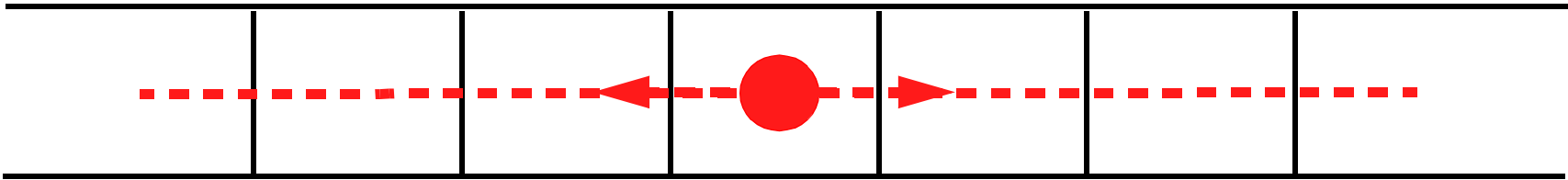




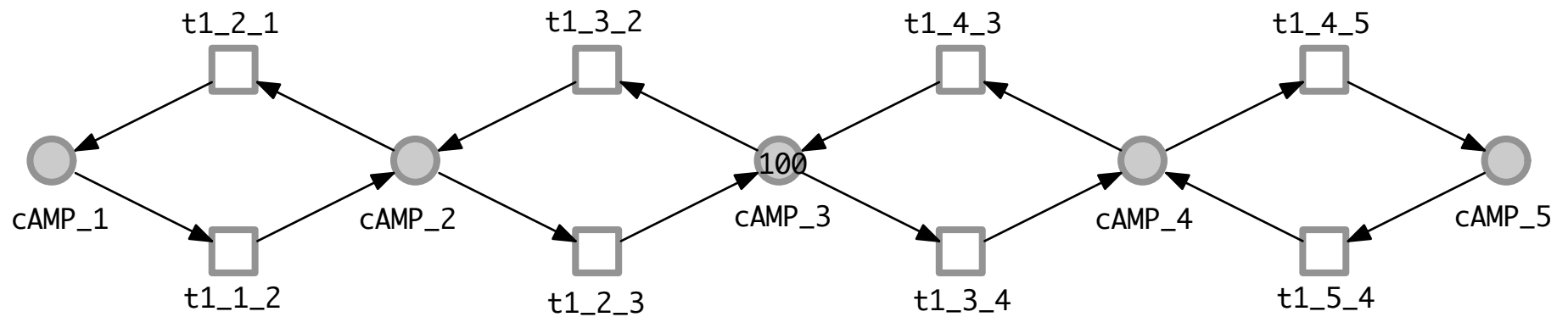
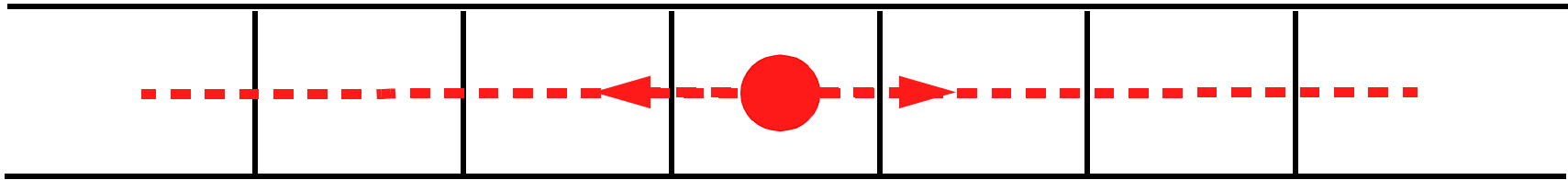
## Ex3: DIFFUSION - 1D

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PN & BioModel Engineering



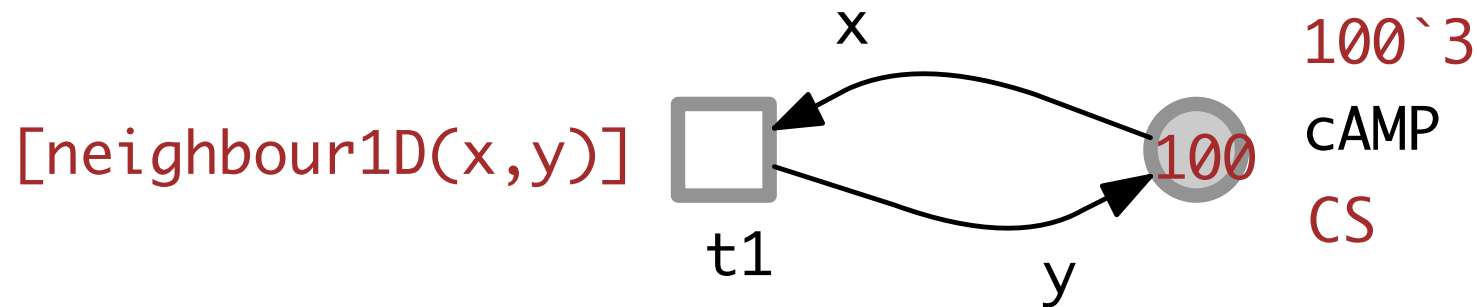
## Ex3: DIFFUSION - 1D



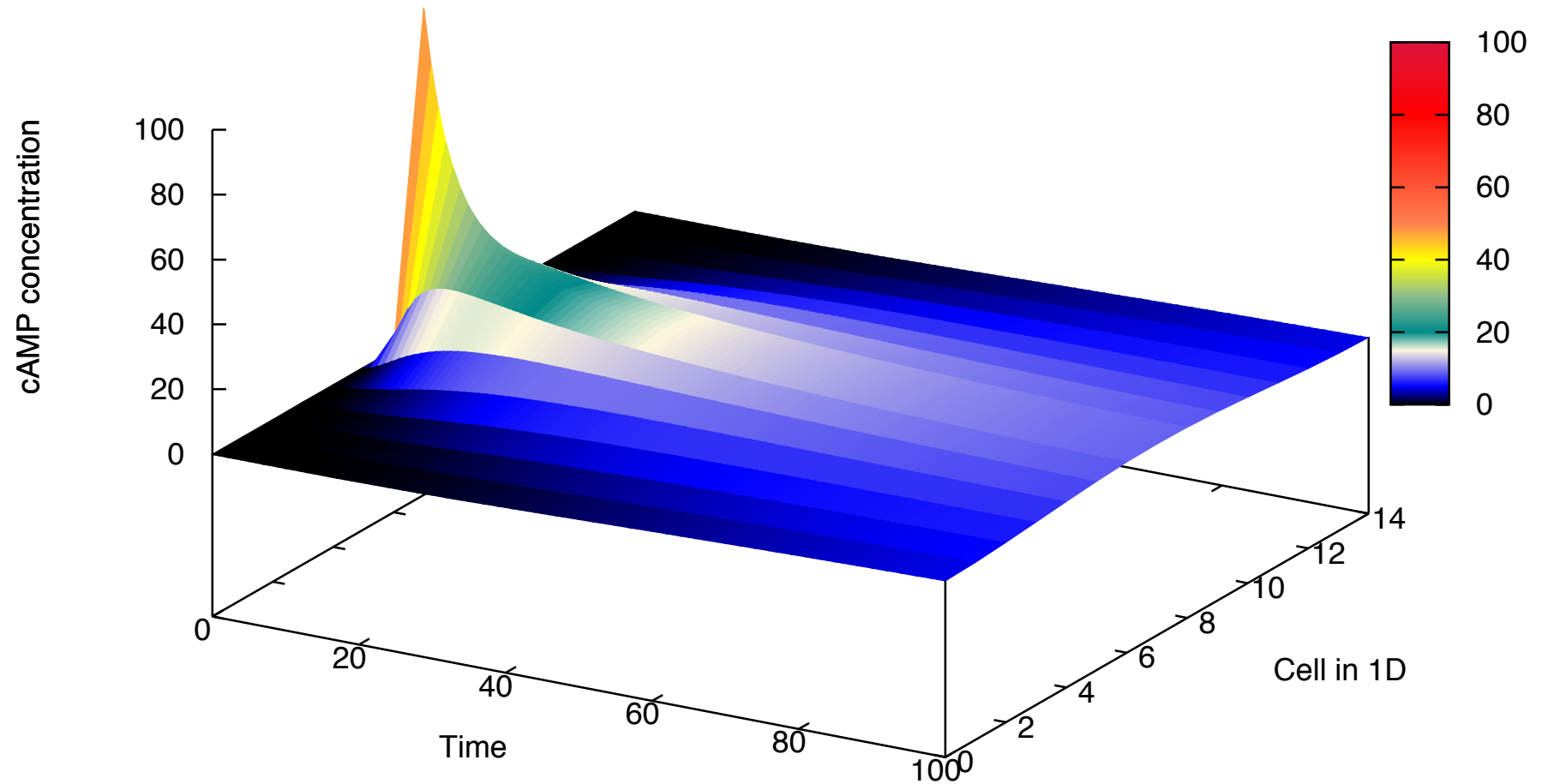
### ❑ definitions

```
const D1 = 5;           // grid size  
colorset CS = 1-D1;    // grid positions  
var x,y : CS;
```

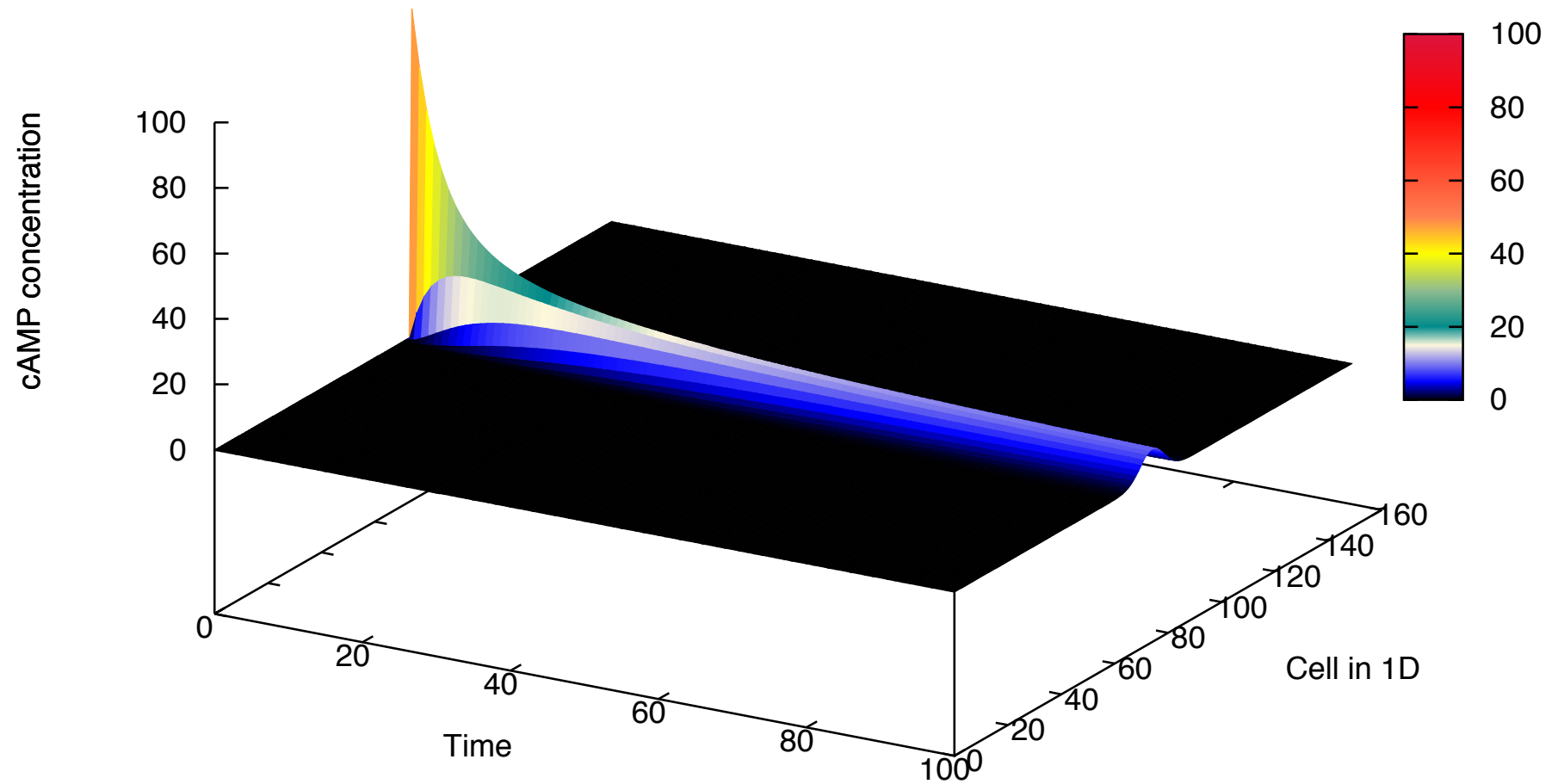
```
function neighbour1D (CS x,a) bool:  
  // a is neighbour of x  
  ( a=x-1 | a=x+1 ) & (1<=a) & (a<=D1);
```



## Ex3: DIFFUSION - 1D

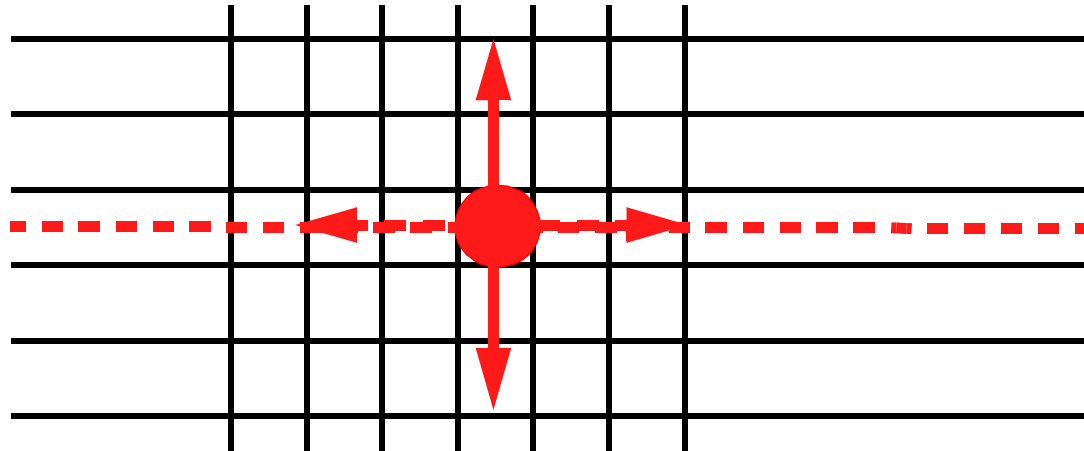


## Ex3: DIFFUSION - 1D

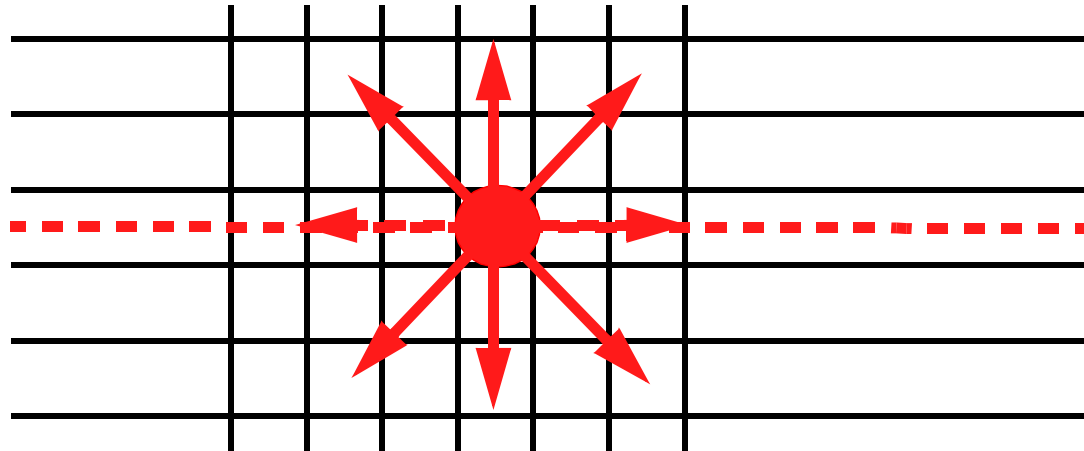




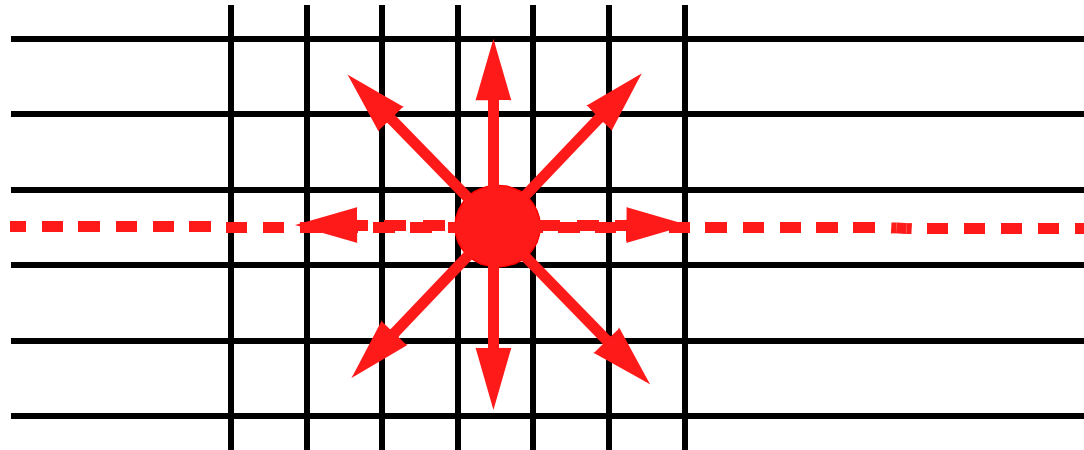
### ❑ SCHEME



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### ❑ definitions

```
const D1 = 5;           // grid size first dimension
const D2 = 5;           // grid size second dimension
colorset CD1 = 1-D1;    // row index
colorset CD2 = 1-D2;    // column index
colorset Grid2D = CD1 x CD2; // 2D grid

var x, a : CD1;
var y, b : CD2;
```

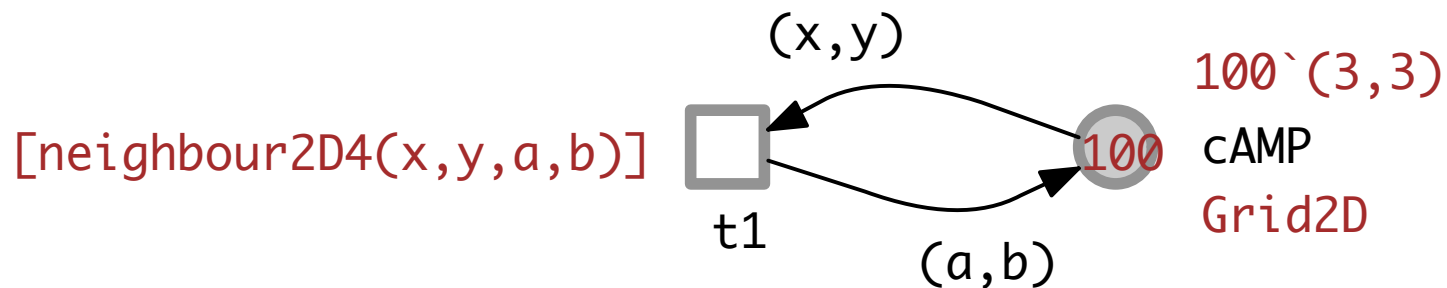
### ❑ four neighbours

**function** neighbour2D4 (CD1 x, CD2 y, CD1 a, CD2 b) **bool**:

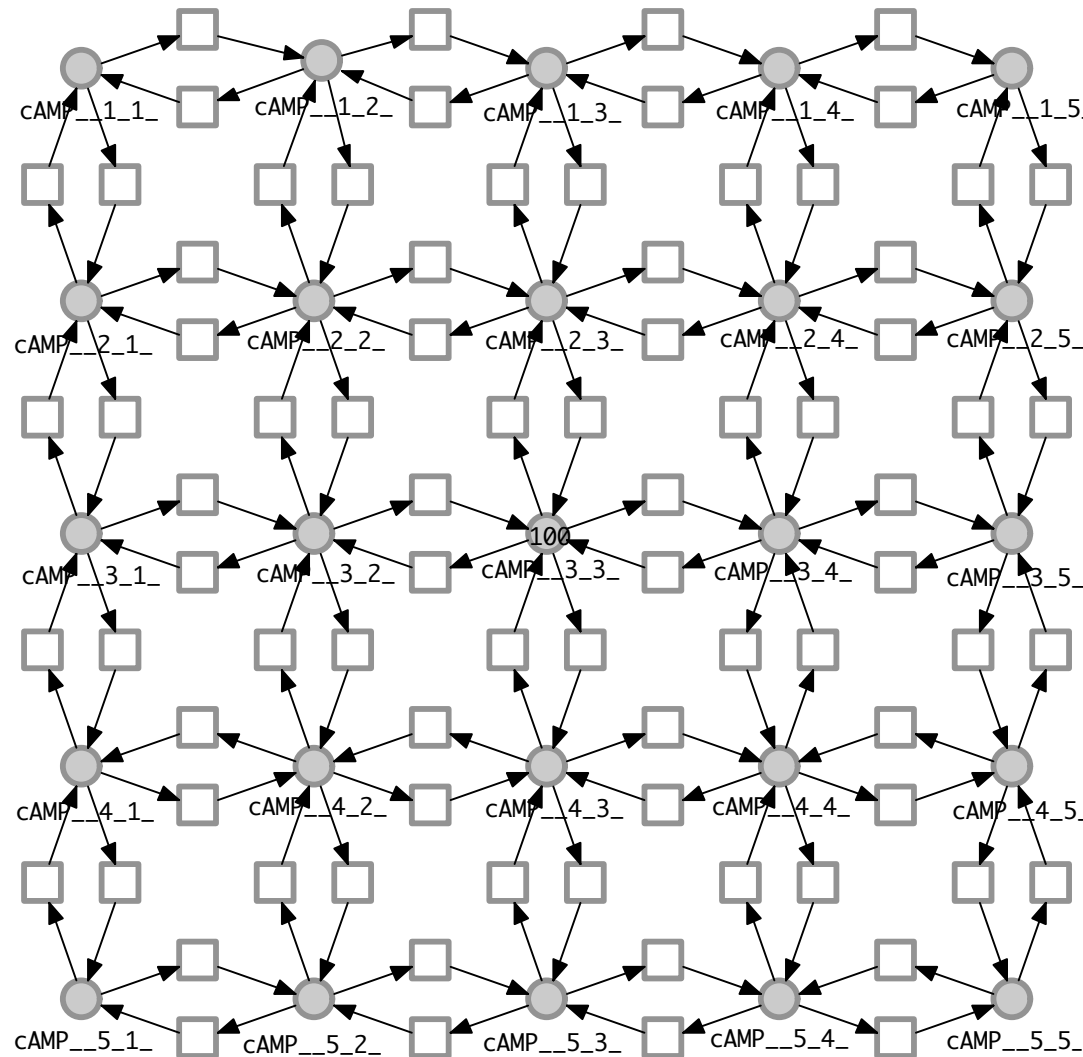
*// (a,b) is one of the up to four neighbours of (x,y)*

$(a=x \ \& \ b=y-1) \mid (a=x \ \& \ b=y+1)$

$\mid (b=y \ \& \ a=x-1) \mid (b=y \ \& \ a=x+1);$



## Ex3: DIFFUSION - 2D4 NEIGHBOURHOOD



### ❑ eight neighbours

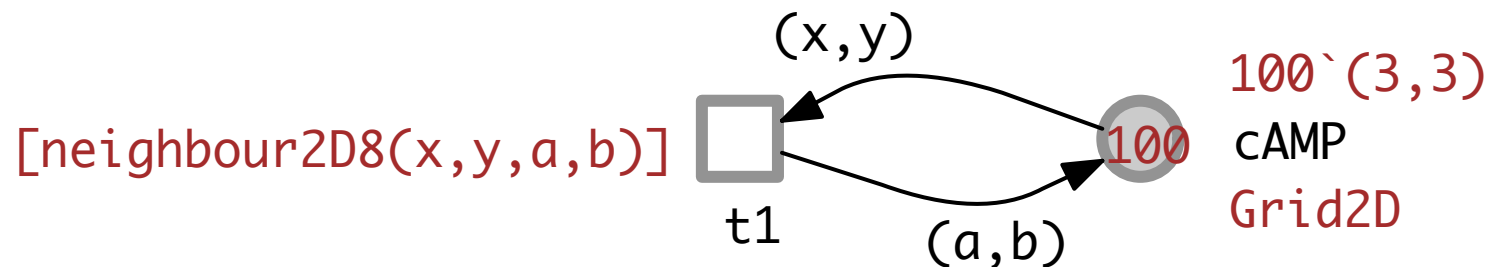
**function** neighbour2D8 (CD1 x, CD2 y, CD1 a, CD2 b) **bool**:

*// (a,b) is one of the up to eight neighbours of (x,y)*

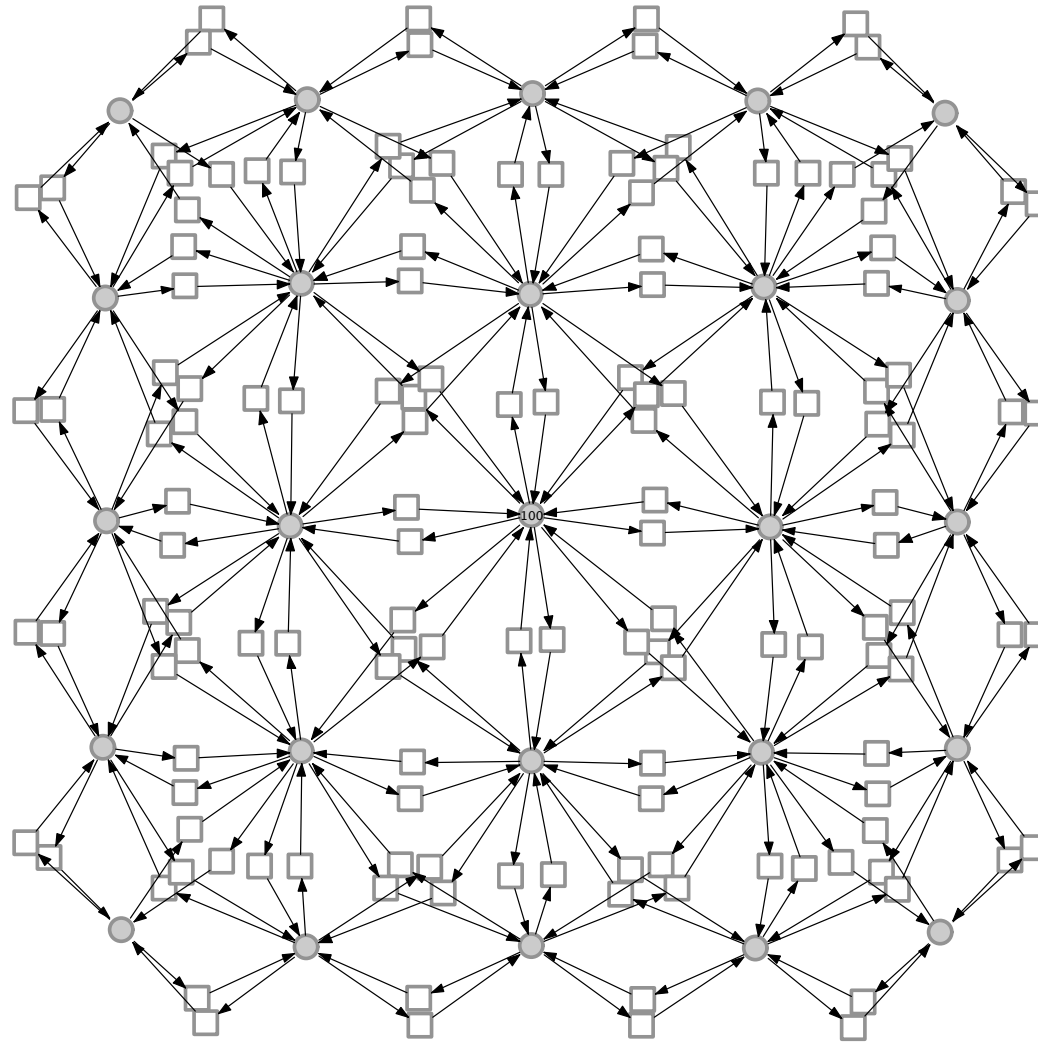
$(a=x \mid a=x+1 \mid a=x-1) \ \& \ (b=y \mid b=y+1 \mid b=y-1)$

$\& \ (! (a=x \ \& \ b=y))$

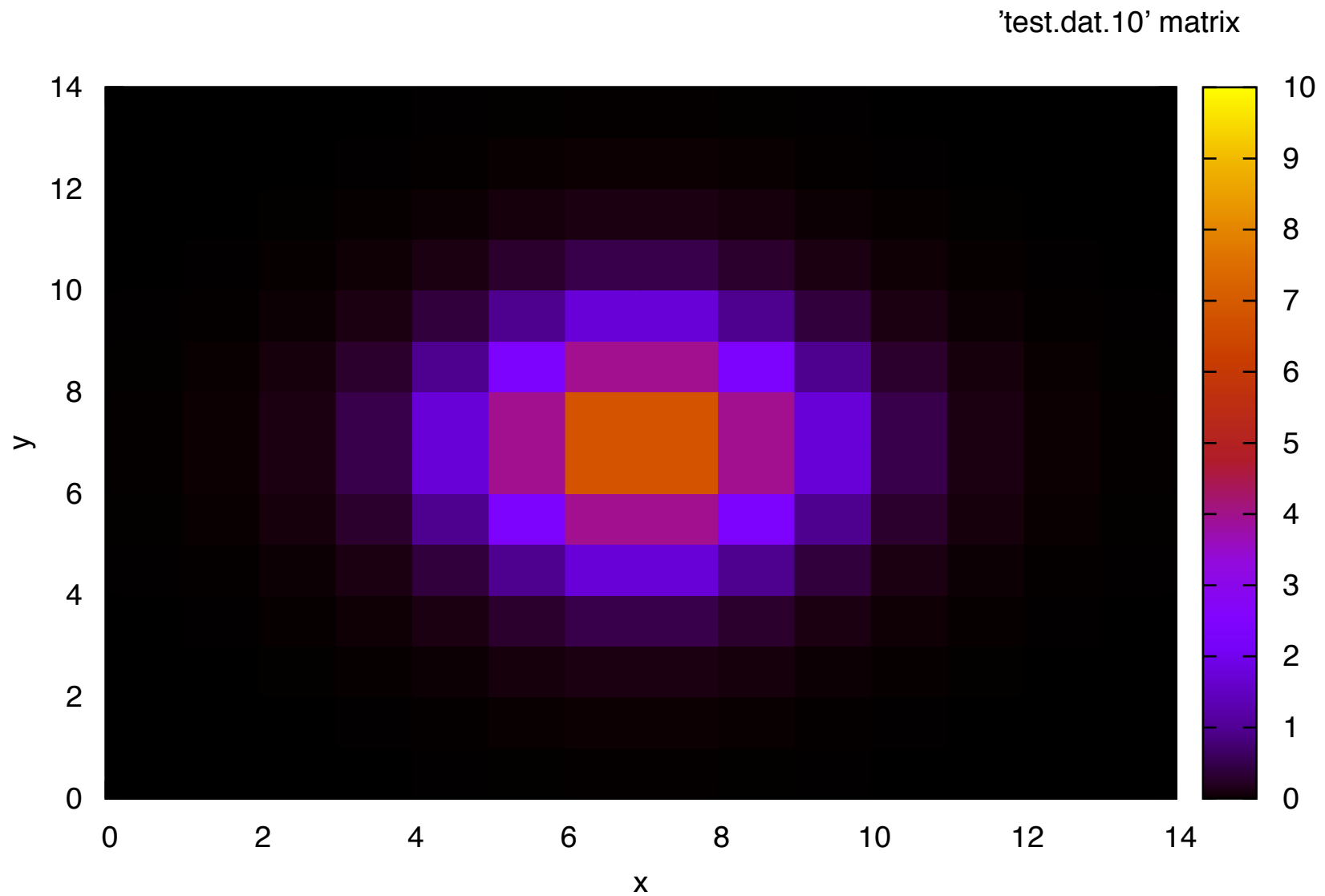
$\& \ (1 \leq a \ \& \ a \leq D1) \ \& \ (1 \leq b \ \& \ b \leq D2);$



## Ex3: DIFFUSION - 2D8 NEIGHBOURHOOD

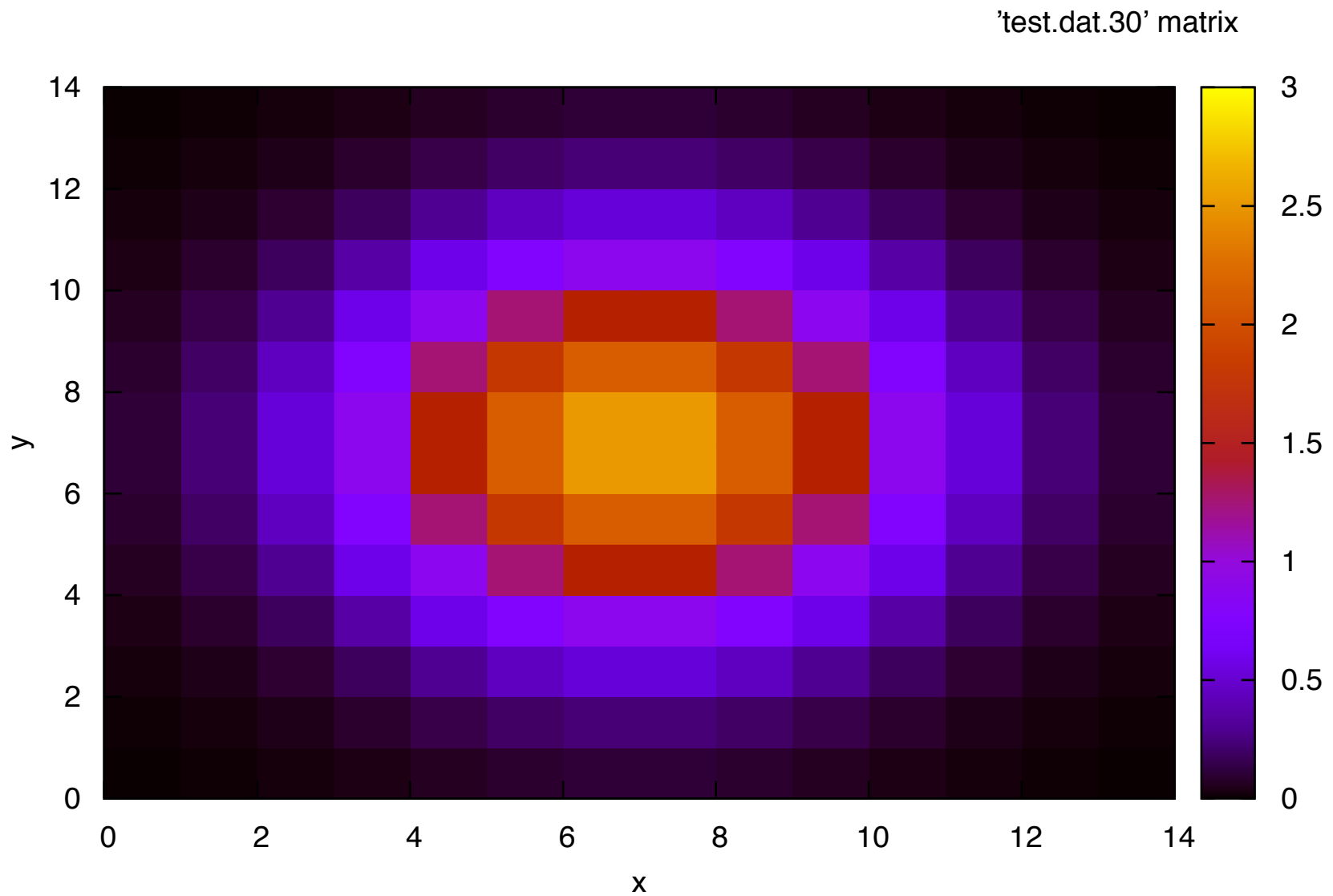


## Ex3: DIFFUSION - 2D8 NEIGHBOURHOOD

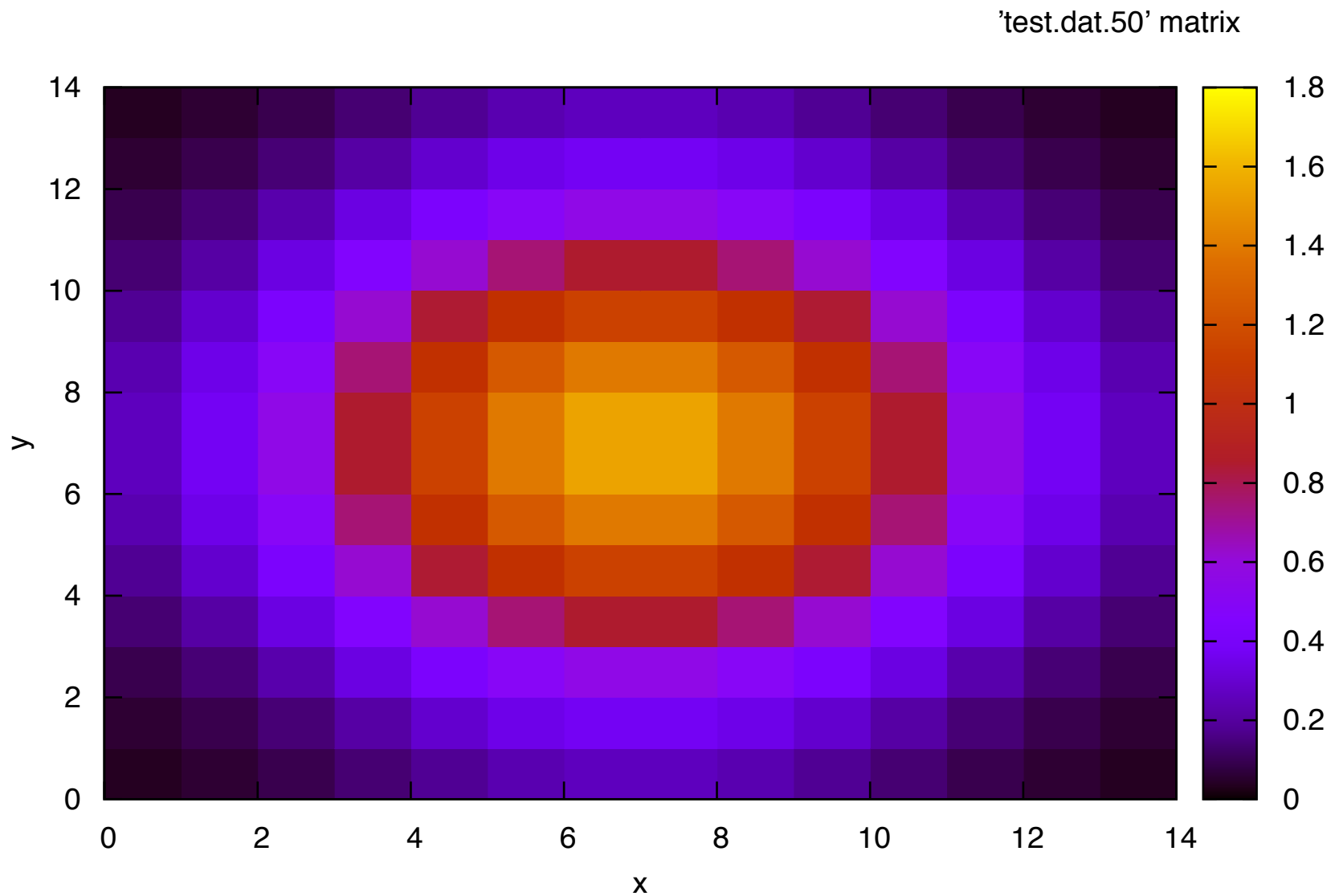




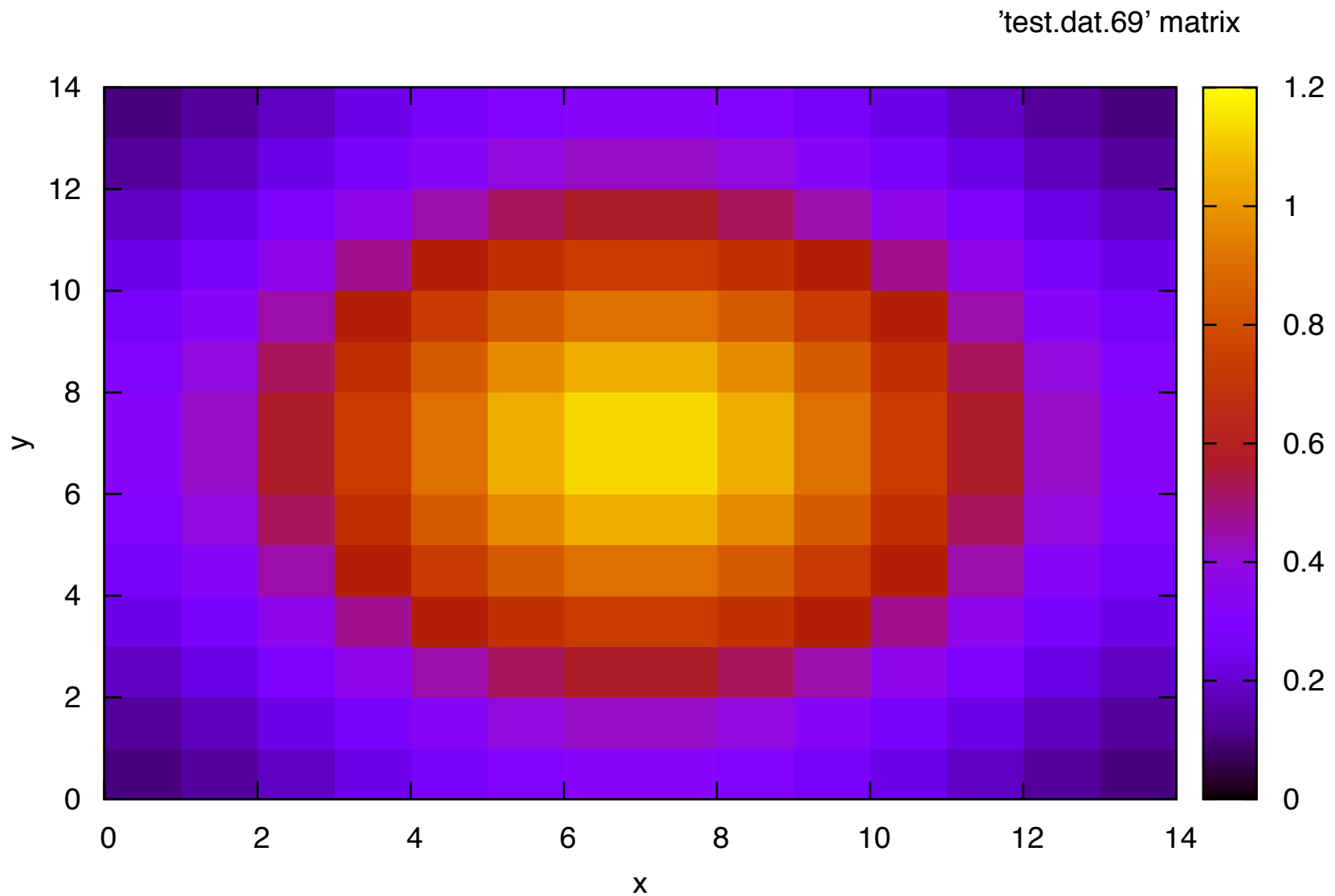
## Ex3: DIFFUSION - 2D8 NEIGHBOURHOOD



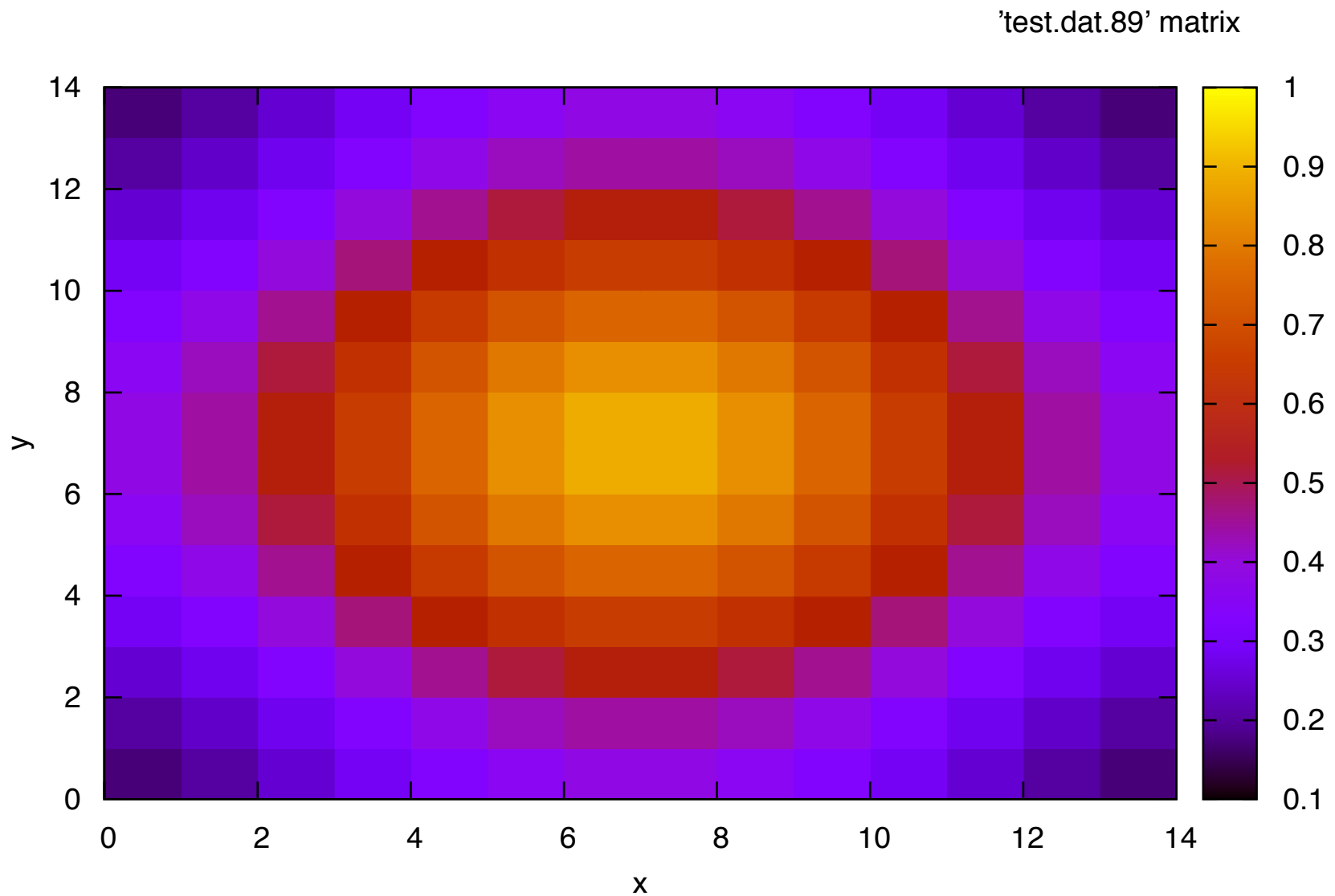
## Ex3: DIFFUSION - 2D8 NEIGHBOURHOOD

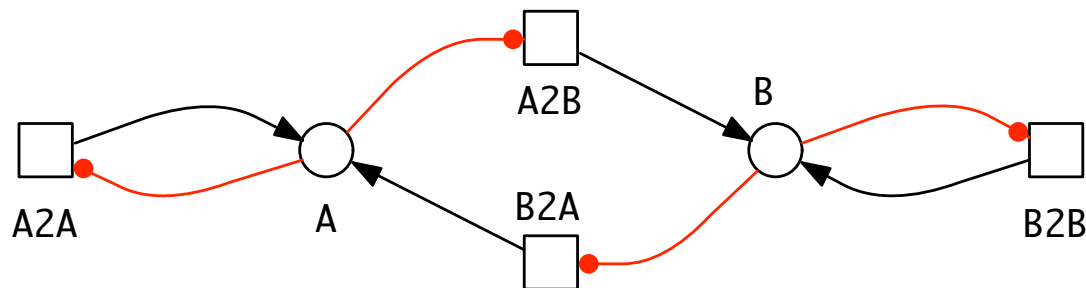
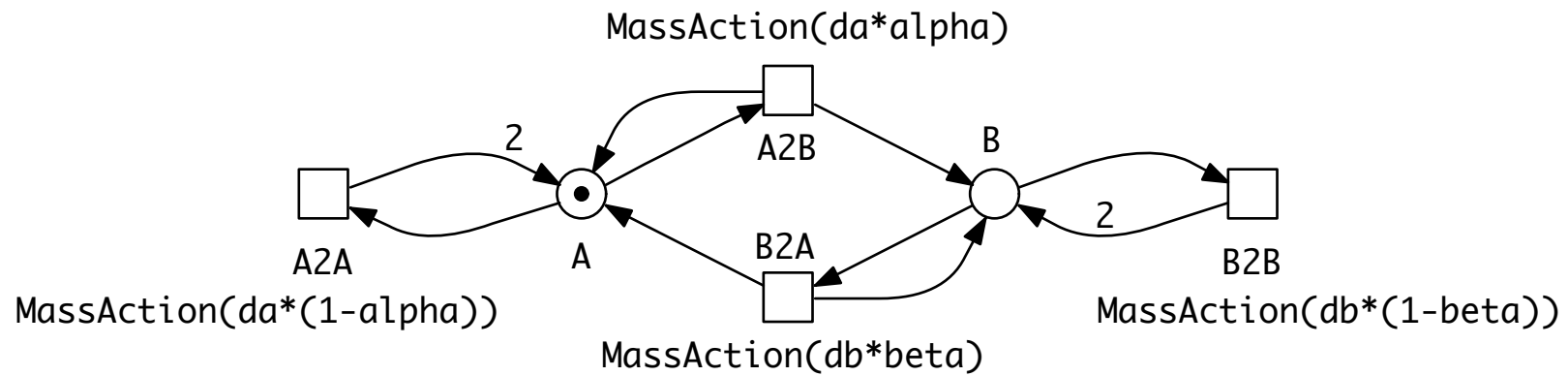


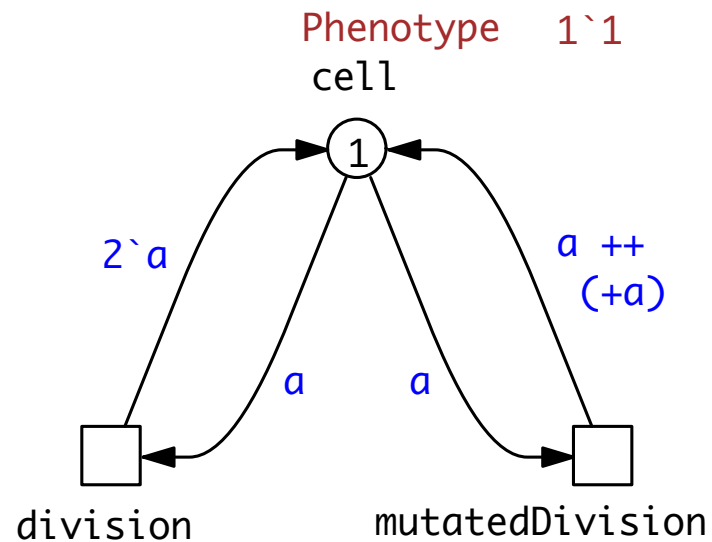
## Ex3: DIFFUSION - 2D8 NEIGHBOURHOOD



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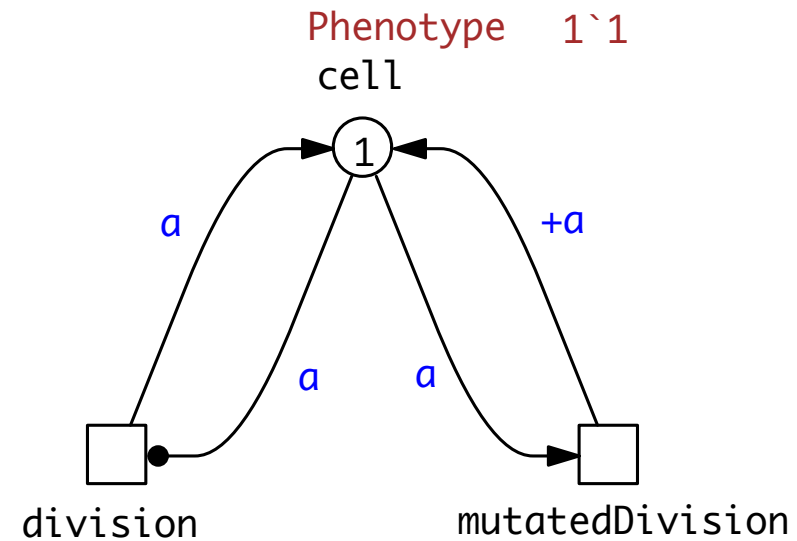






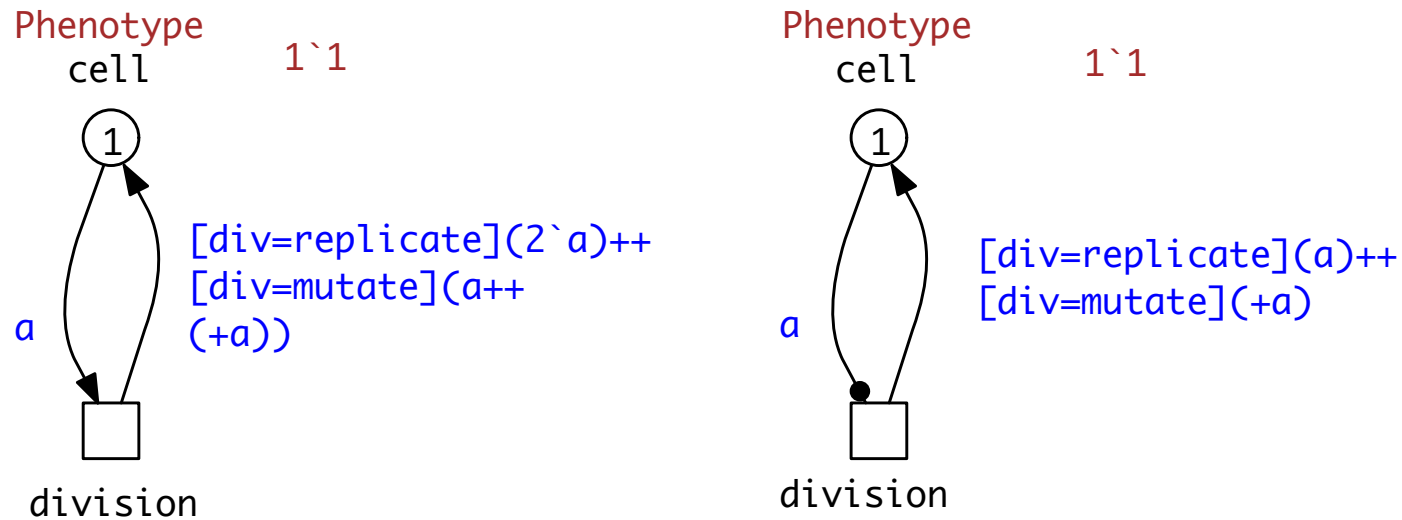
$$a=1 : da*(1-\alpha)*cell$$

$$a=2 : db*(1-\beta)*cell$$

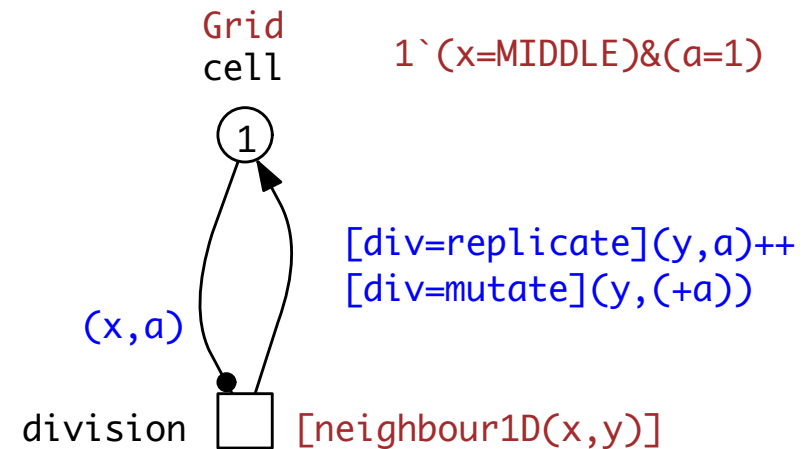
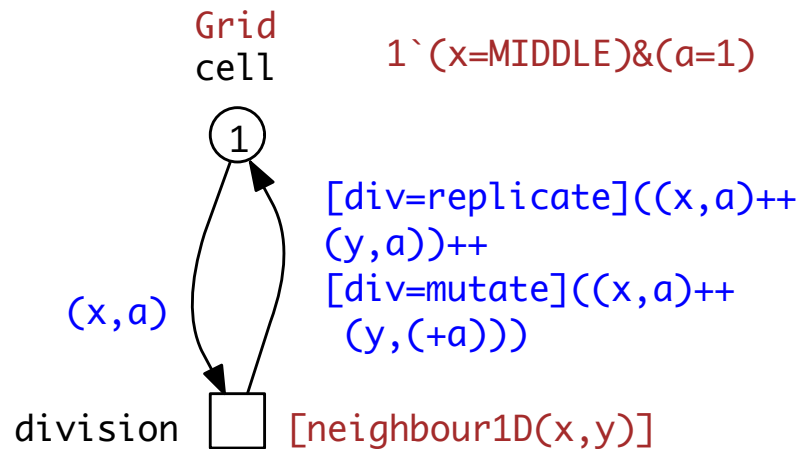


$$a=1 : da*\alpha*cell$$

$$a=2 : db*\beta*cell$$

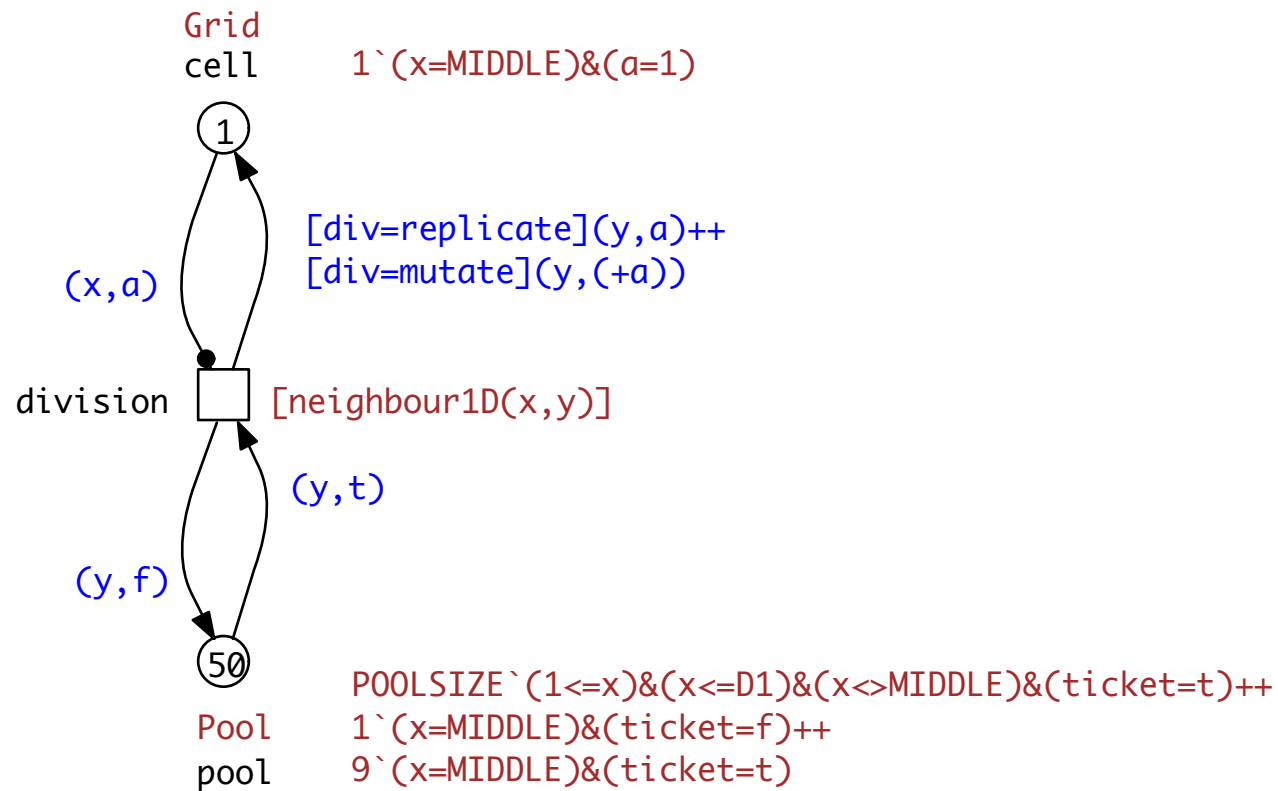


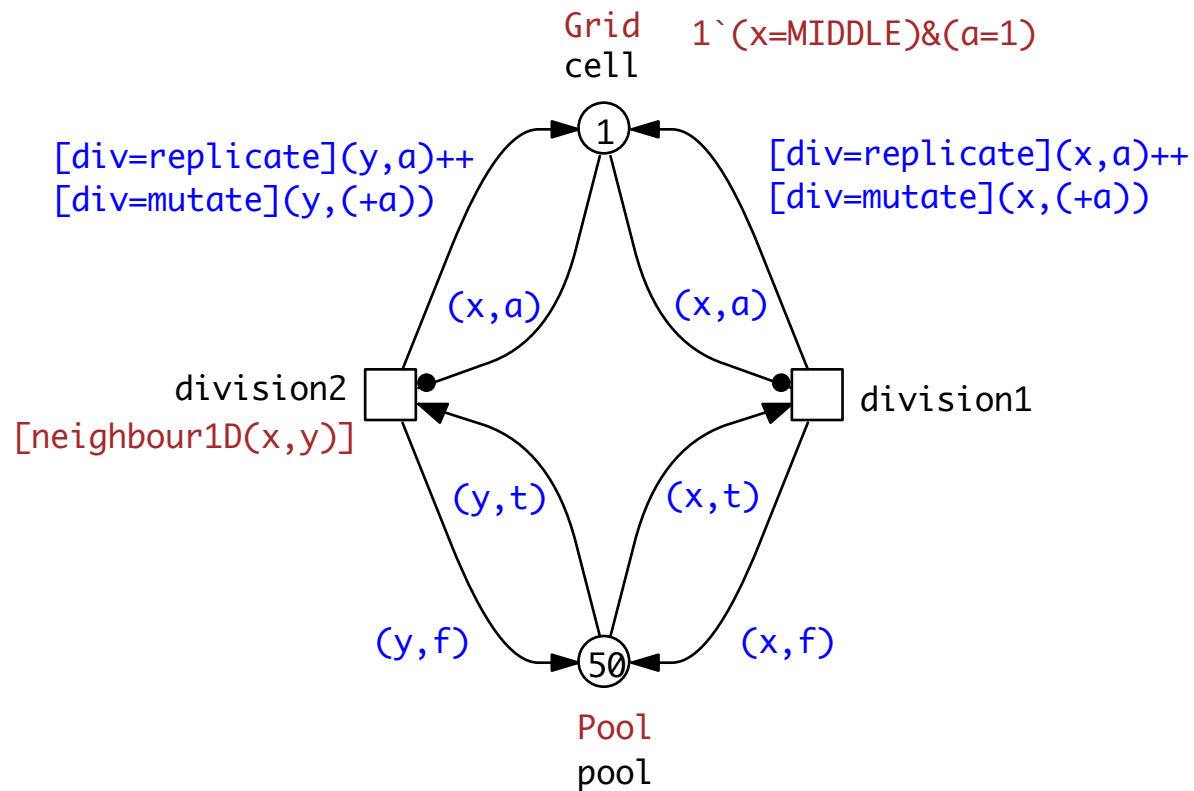
```
(a=1) & (div=replicate) : cell*da*(1-alpha)
(a=1) & (div=mutate) : cell*(da*alpha)
(a=2) & (div=replicate) : cell*(db*(1-beta))
(a=2) & (div=mutate) : cell*(db*beta)
```



$(a=1) \& (div=replicate) : cell*da*(1-\alpha)$   
 $(a=1) \& (div=mutate) : cell*(da*\alpha)$   
 $(a=2) \& (div=replicate) : cell*(db*(1-\beta))$   
 $(a=2) \& (div=mutate) : cell*(db*\beta)$

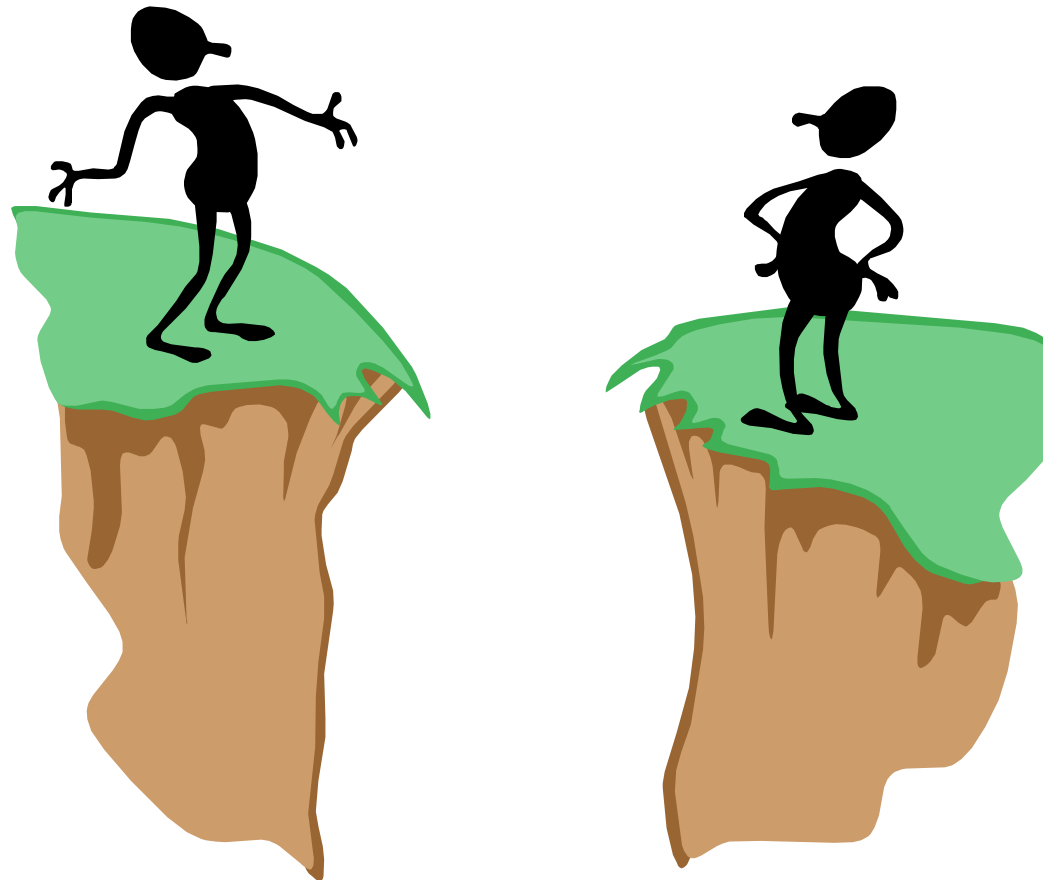






```

POOLSIZE `(1<=x)&(x<=D1)&(x<>MIDDLE)&(ticket=t)++
1 `(x=MIDDLE)&(ticket=f)++
9 `(x=MIDDLE)&(ticket=t)
    
```



**THANKS !**

**[HTTP://WWW-DSSZ.INFORMATIK.TU-COTTBUS.DE](http://www-dssz.informatik.tu-cottbus.de)**